

Ambient Noise Imaging and Monitoring,
Cargese (Corsica), on April 22nd-27th, 2013

Wave Methods for Structural System Identification and Health Monitoring of Buildings

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http://www.usc.edu/dept/civil_eng/Earthquake_eng/

Outline

- **The problem**
- **Similarities and differences with the similar problem in geophysics**
- **Examples using earthquake excitation**
- **What is being done and can be done with noise?**

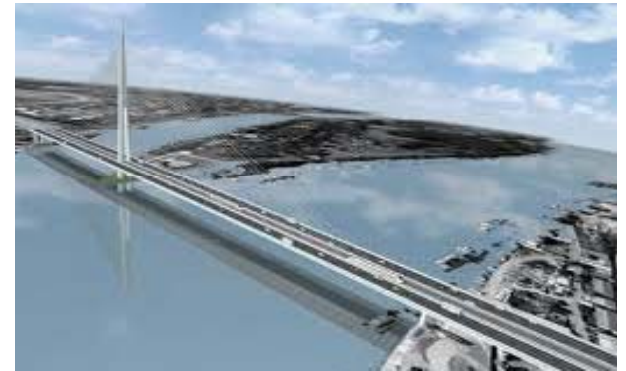
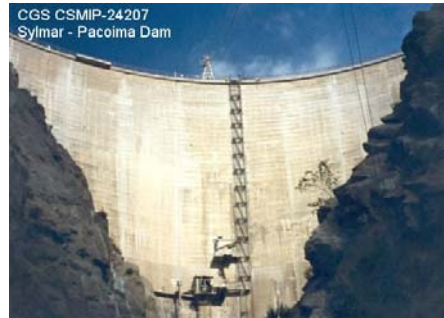


The Problem

- Determine if a structure has been damaged, **during or soon after** the earthquake, before physical inspection is possible.
- Such information is useful for **timely** decision making on **evacuation**; and also **emergency response** (help will be sent where most needed).
- Benefits to society: **prevent loss of life and injuries** caused by potential collapse of the weakened structure during shaking from aftershocks/ **avoid needless** evacuation (San Francisco Occupancy Redemption Program).
- What is needed: sensors, data communication network, and **methodology for damage detection** (what physical parameter should be monitored, what change means damage, etc.).

The Structures

- Bridges
- Dams
- **Buildings**



Height:

$$h = 4\text{m/floor}; \quad H=10\text{--}300 \text{ m}$$

Shear wave velocity:

$$V_s = 100 - 400 \text{ m/s}$$

Fundamental period of vib.:

$$T \sim n/10 \text{ (roughly)}$$

Data:

$$0.02 - 25 \text{ Hz} \quad (50 \text{ Hz})$$

Buildings

Materials:

Reinforced concrete: nonlinear elastic behavior
Steel: much more linear behavior.

Lateral force resisting system:

Moment resisting frame, Shear walls, bracing.

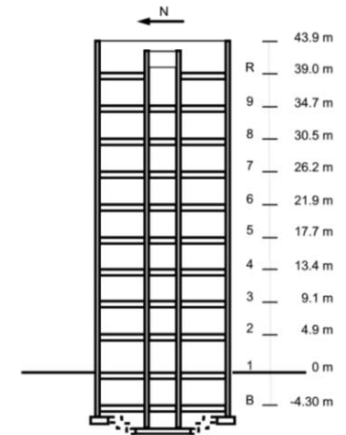
Type of deformation:

The elements (beams and columns) -
deform more in bending (dispersive w.p.)

Building as a whole -
deforms more like a **shear beam** (nondispersive w.p.).

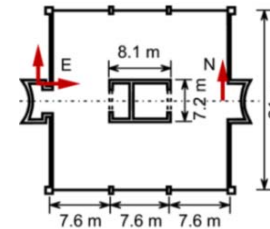
Evidence:

ratios of modes of vibration (1:3:5:7.... vs. 1:6.27:17.5...)

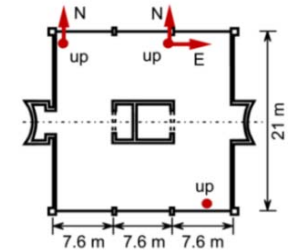


(a)

(b)



(c)



(d)

Structural Health Monitoring

Definition: tracking the state of health of a structure based on some instrumental data

Vibrational methods:

- NDT – local; determine the location of damage (within an element); excitation – actuator; not practical for buildings (need access to the element; expensive).
- Seismic – use earthquake excitation, ambient noise or shaker.

Modal - frequencies of vibration or mode shapes - global

Wave - velocities of wave propagation through the structure – intermediate scale (?)

Historical Perspective – ambient noise tests

- Review article by Ivanovic, Trifunac and Todorovska, ISET 2000.

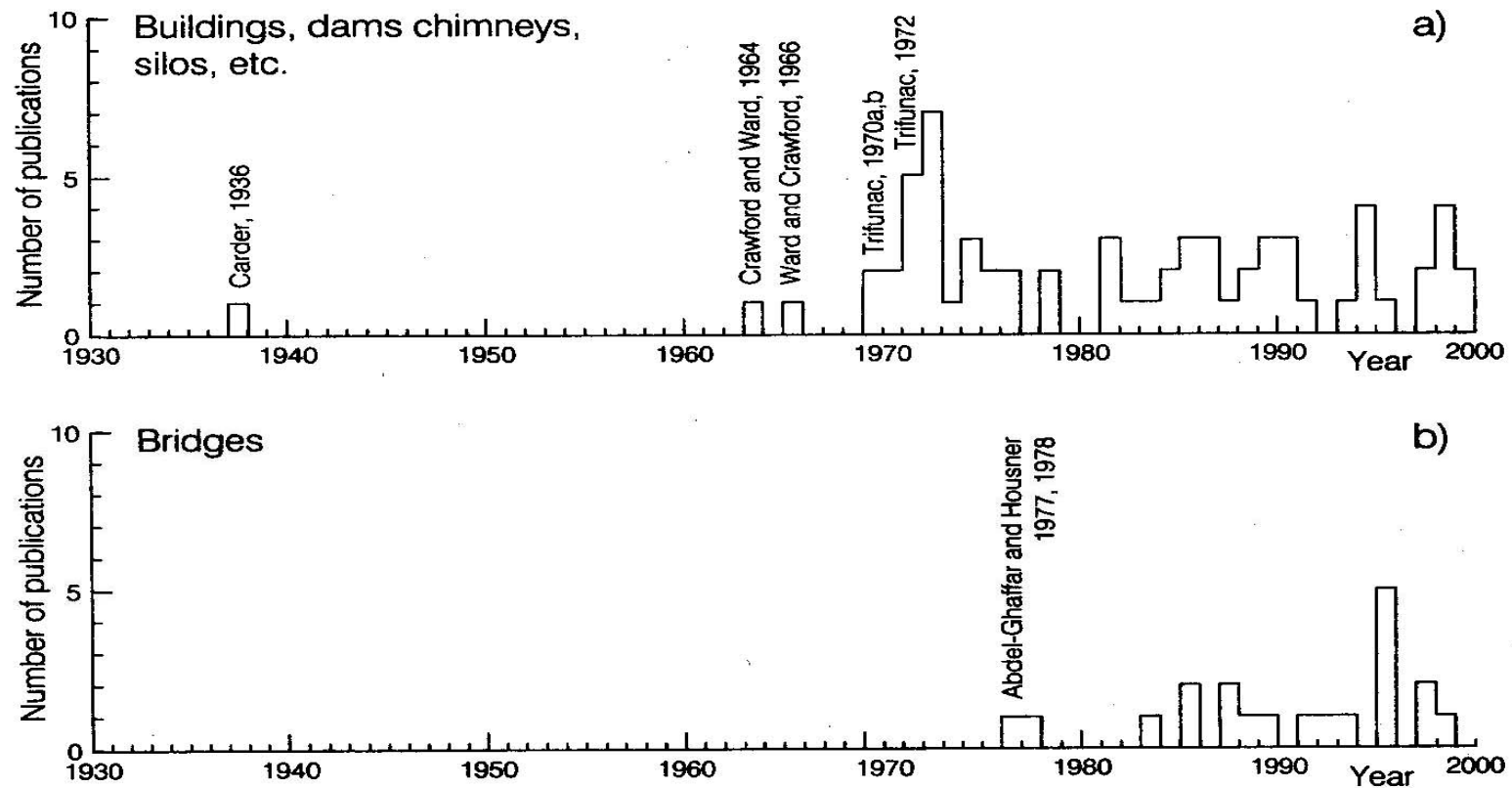


Fig. 1 Frequency of occurrence of published contributions to the subject of ambient vibration testing of full-scale structures: (a) buildings, dams, chimneys, silos,... (b) bridges

Historical Perspective – earthquake records

Some Milestones in Earthquake Engineering (Trifunac et al., 2001):

- 1906: San Francisco earthquake, California.
- 1923: Great Kanto earthquake, Japan.
- 1924: ERI is established in Japan.
- 1932: Suyehiro gives lectures in the U.S. In his lectures he mentions ambient vibration studies of ERI building etc.
- 1933: Long Beach earthquake, California (M=5.4).
- 1940: Imperial Valley earthquake, California.
- 1948: EERI established in U.S.
- 1956: 1WCEE held in San Francisco (every 4 years since then)
- 1971: San Fernando earthquake, California. Many records in structures
- 1994: Northridge earthquake, California. Many records in structures.

Earthquake Records in Structures

Hollywood Storage Building:

Longest history of recording in U.S. – 80 years.
First record in 1933 (So. California earthquake).

Intrumentation Programs:

National Strong Motion Program (USGS)

California Strong Motion Instrumentation Program (CGS)

Buildings ~ 225 (1-62 stories high); bridges: 76; dams: 28

Ground: > 800 stations; 30 geotechnical (downhole) arrays; etc.

Code Buildings: instrumented by owner



Structural Health Monitoring

- Assessment must be **reliable** and **accurate** to be useful:
 - **No failures** to detect significant damage.
 - **No false alarms** – imagine e.g. needless evacuation of a hospital.
- Method must be
 - **Robust**
 - **Sensitive** to damage and **Not sensitive** to other factors (SSI, weather, etc.)
 - **Accurate**
- Robust Methods:
 - Parameter estimation – can track changes
 - Performance based – check if design forces have been exceeded; check for correlation of damage with interstory drift.
– cannot track changes
 - Damage probability matrices - rough, good for large stock prediction.

Wave Propagation Method

- Damage sensitive parameter – **velocity of wave propagation**
- Uses information on **phase** rather than amplitudes
- **Shear and Torsional** wave velocities identified

- Physical basis:

$$V = \sqrt{\mu / \rho}; \quad \mu = \text{shear modulus}; \quad \rho = \text{mass density}$$

$$V = h / \tau; \quad \tau = \text{travel time}; \quad h = \text{distance travelled}$$

- **Data: vibrationalal (e.g. accelerations)**
- **Moving window analysis** – to detect changes

Wave Propagation Method

- Advantages of the method:
 - **Robust** when applied to **actual buildings** and **large amplitude response data**
 - **Local in nature** - **more sensitive to local damage** than the modal methods
 - **Not sensitive** to foundation rocking and **SSI**, the weakness of the natural frequencies of vibration
 - Does not require prior measurement

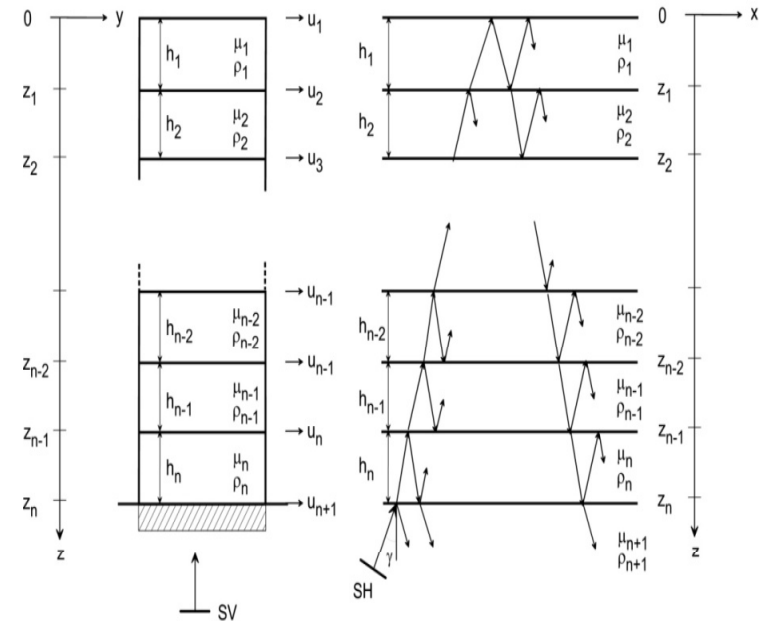
Wave Propagation Method

- Historical perspective:
 - Kanai and Yoshizawa, 1963; Kanai, 1965: Shows the equivalence of representation of response as sum of modes and sum of bouncing waves.
 - Safak, 1999: Proposes use of travel time for damage detection. Argues it is more local than freq. of vibration.
 - Kawakami and Oyunchimeg, 2003; Oyunchimeg and Kawakami, 2003: NIOM method, damaged and undamaged buildings.
 - Ivanovic et al. 2006: Cross-correlation, Van Nuys damaged building.
 - Snieder and Safak, 2006: Impulse response functions, Millikan library small response.
 - Kohler et al., 2007: Impulse response functions, Factor bldg.
 - Todorovska and Trifunac, SDEE 2008; SCHM 2008: Impulse response functions, damage detection in two severely damaged buildings (ICS, Van Nuys).
 - Todorovska, BSSA 2009a,b: demonstrates insensitivity to SSI on a model; explains wondering of frequency of Millikan library.
 - Todorovska and Rahmani, SCHM 2013; Rahmani and Todorovska 2013a,b,c: waveform inversion.....

Model

How to measure travel time:

- **Impulse response functions = normalized cross-correlations = Green's functions for modified boundary conditions (Snieder and Safak, 2006)**
- Layered shear beam model - **analytic TF and IRFs adopted from geophysics** (propagator matrix approach; Trampert et al., 1993; Todorovska and Rahmani, SCHM 2012).
- Building is NOT a borehole; specific issues .

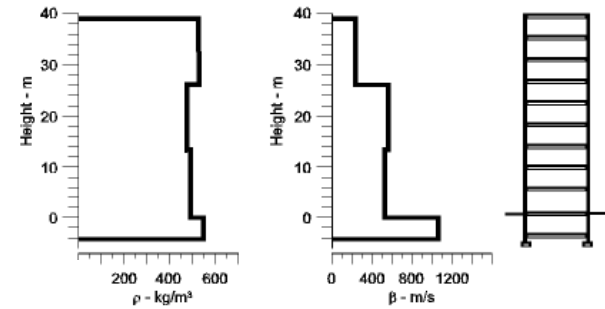


$$TF \equiv \hat{h}_i(\omega) = FT \left\{ \frac{\hat{u}_i(\omega)}{\hat{u}_{\text{ref}}(\omega)} \right\}$$

$$IRF \equiv h_i(t) = FT^{-1} \left\{ \hat{h}_i(\omega) \right\}$$

$$\text{Regularized } IRF = FT^{-1} \left\{ \frac{\hat{u}_i(\omega) \overline{\hat{u}_{\text{ref}}(\omega)}}{|\hat{u}_{\text{ref}}(\omega)|^2 + \varepsilon} \right\}, \quad |\omega| \leq \omega_{\text{max}}$$

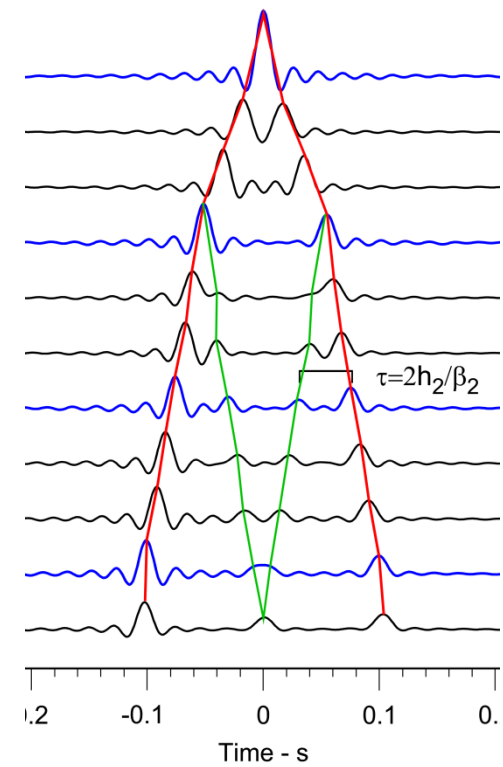
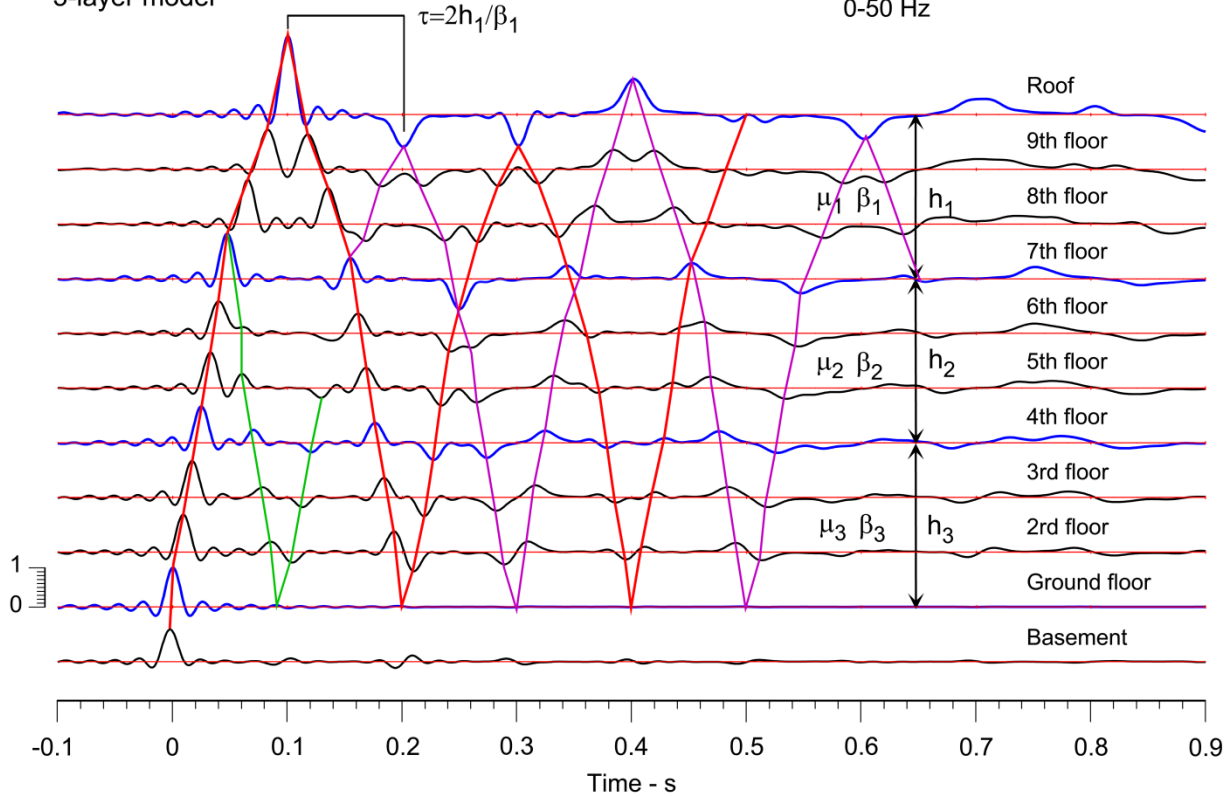
Layered Model IRFs: (Millikan NS)



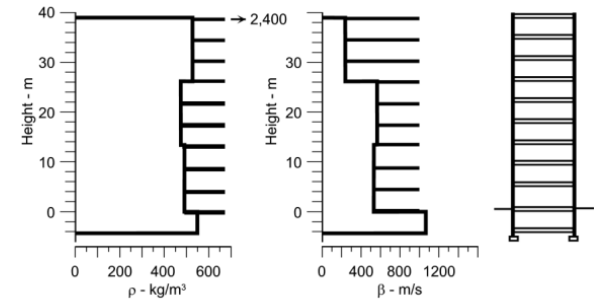
Impulse Response Functions for virtual source at ground floor

3-layer model

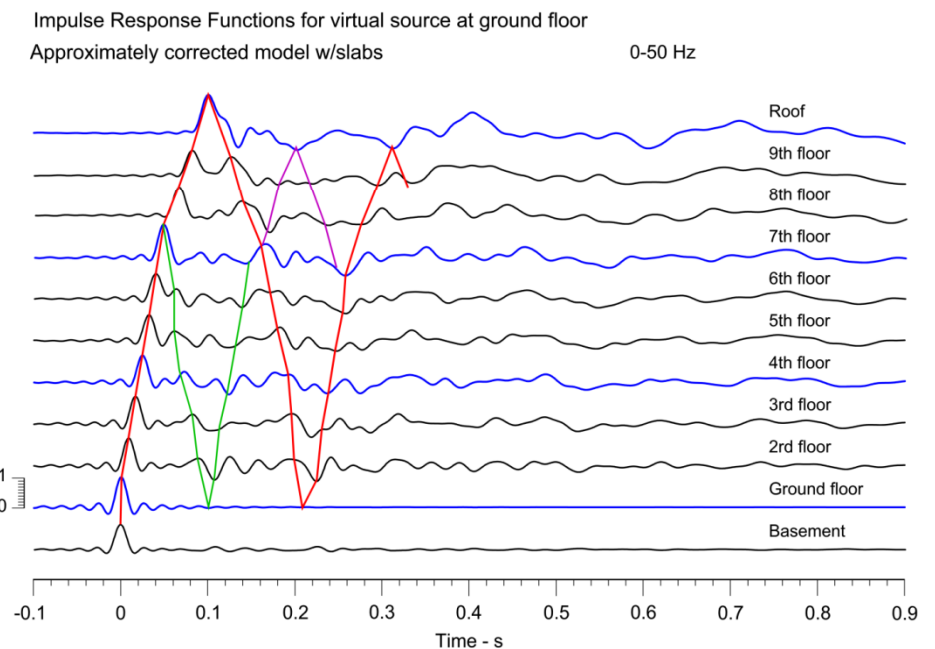
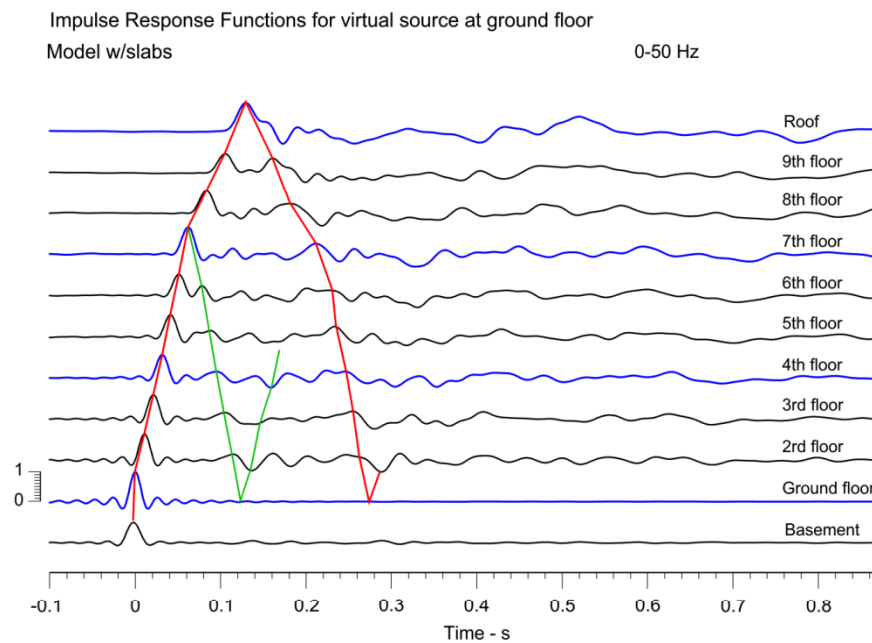
0-50 Hz



Layered Model IRFs: slabs

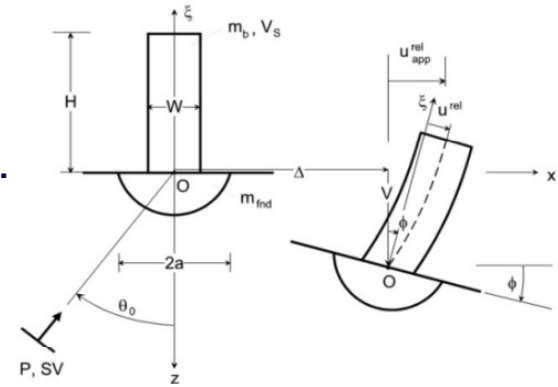


- Additional phase delay due scattering from the slabs – ray theory does not work for this case.



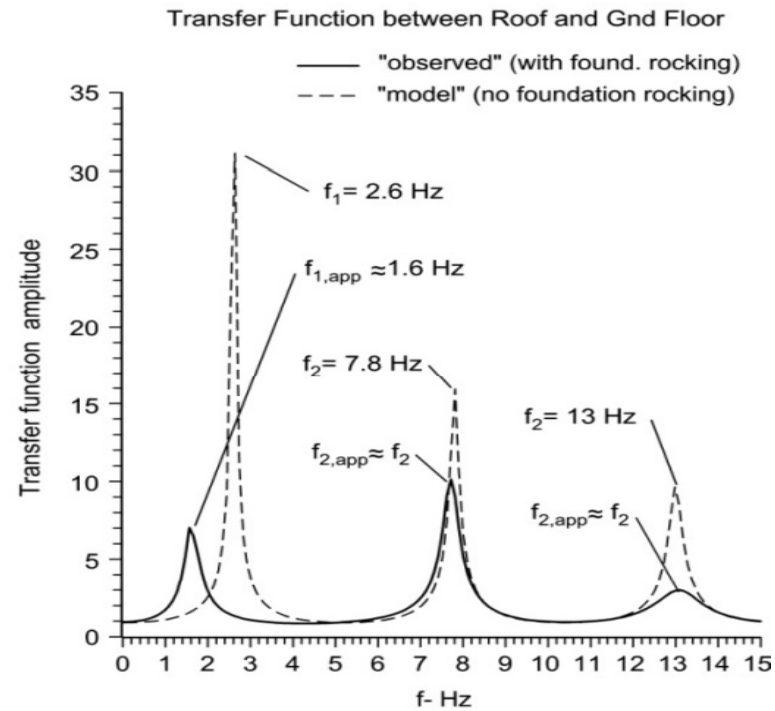
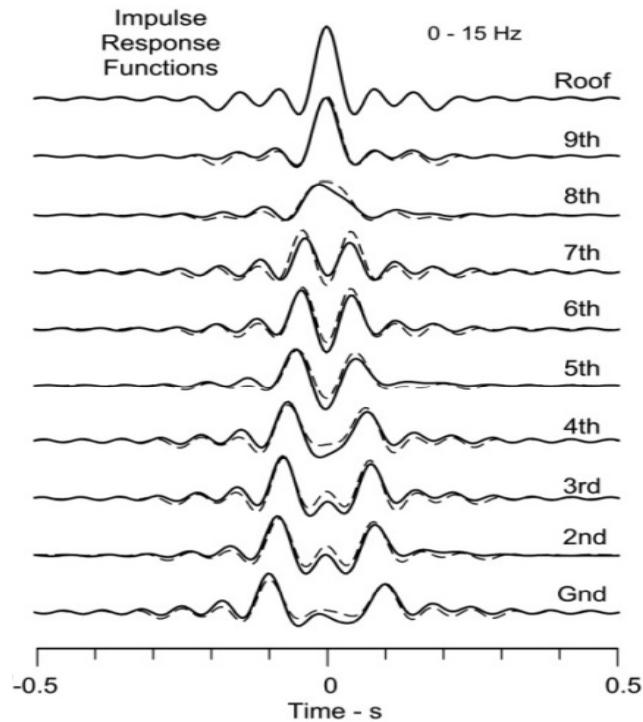
SSI Model IRFs and TF

SSI Model of Millikan library NS response – uniform s.b.
(Todorovska, BSSA 2009a,b)



$$\frac{1}{f_{1,sys}^2} \approx \frac{1}{f_H^2} + \frac{1}{f_R^2} + \frac{1}{f_1^2}$$

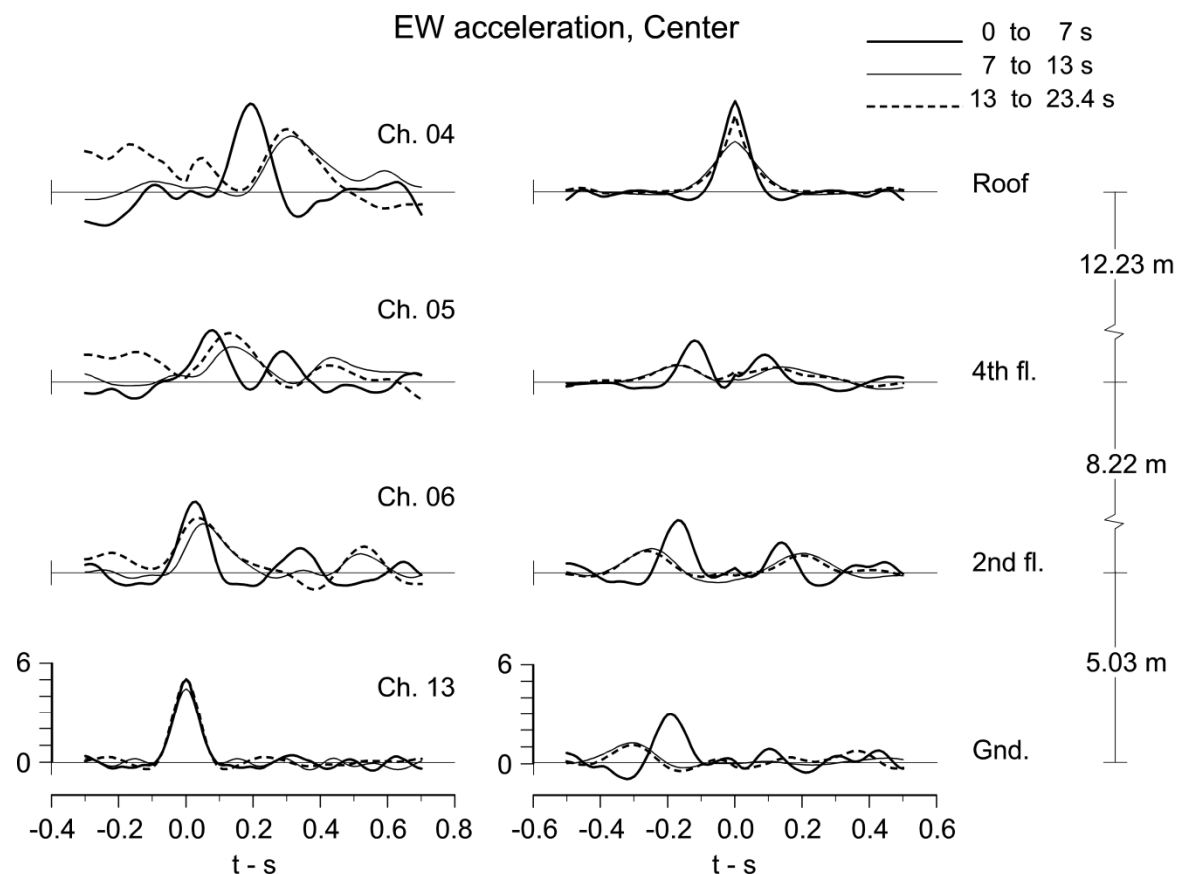
$$\frac{1}{f_{1,app}^2} = \frac{1}{f_1^2} + \frac{1}{f_R^2}$$



Proof of Concept Studies

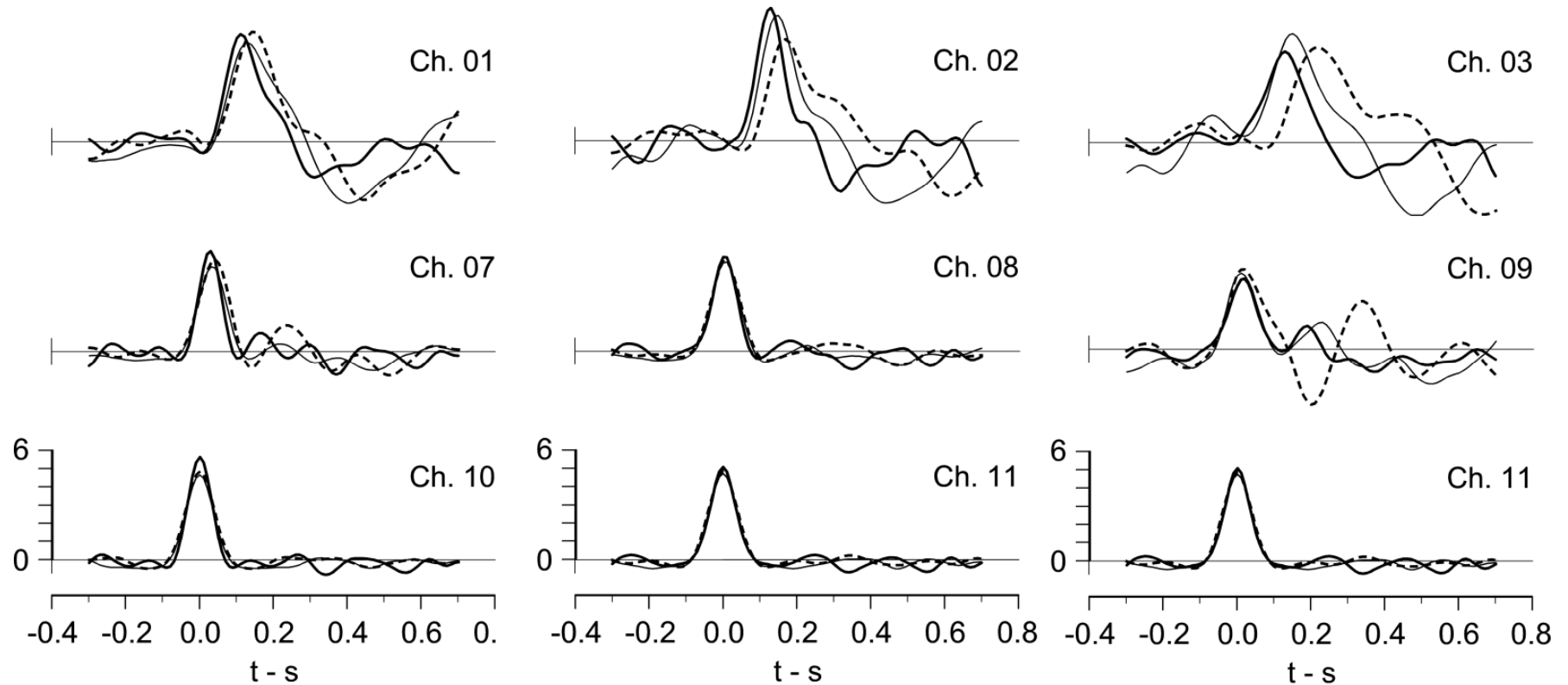
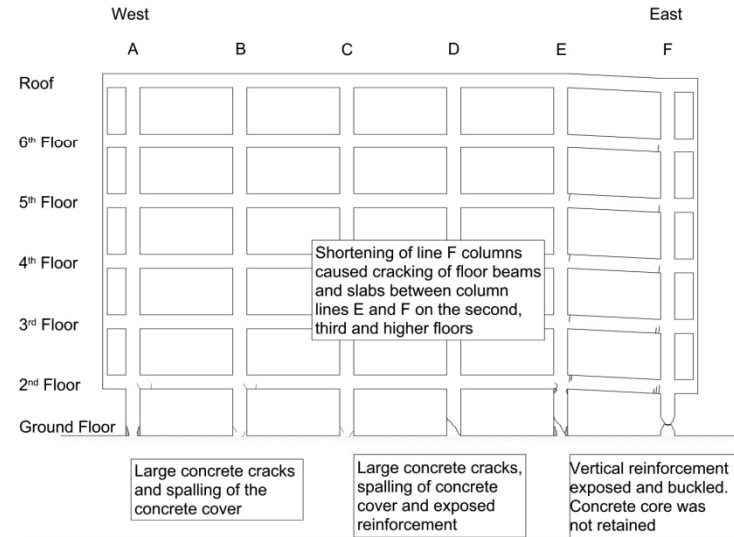
- Two severely damaged buildings (ISC and Van Nuys bldgs; Todorovska and Trifunac, 2008ab)
- **Direct algorithm:** based on ray theory interpretation of IRFs

$$V = h / \tau$$

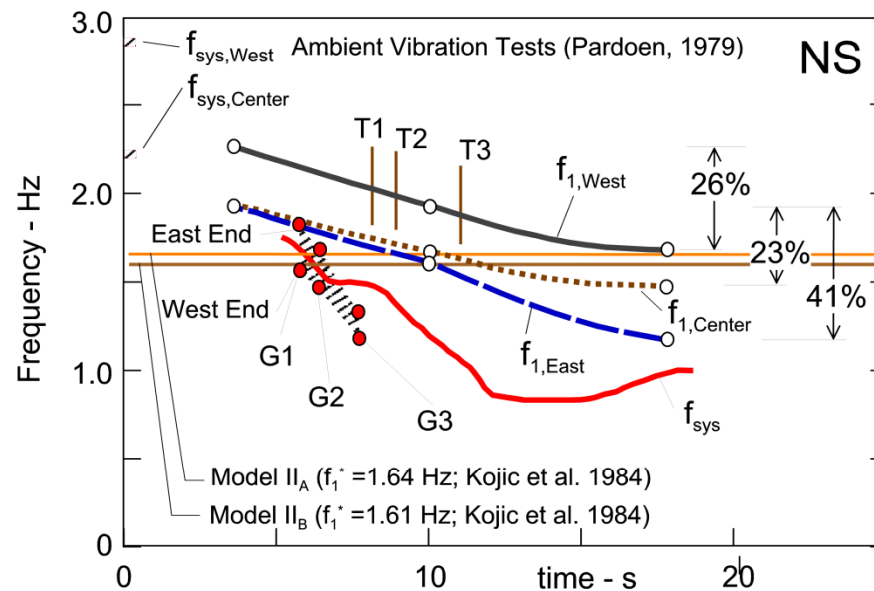
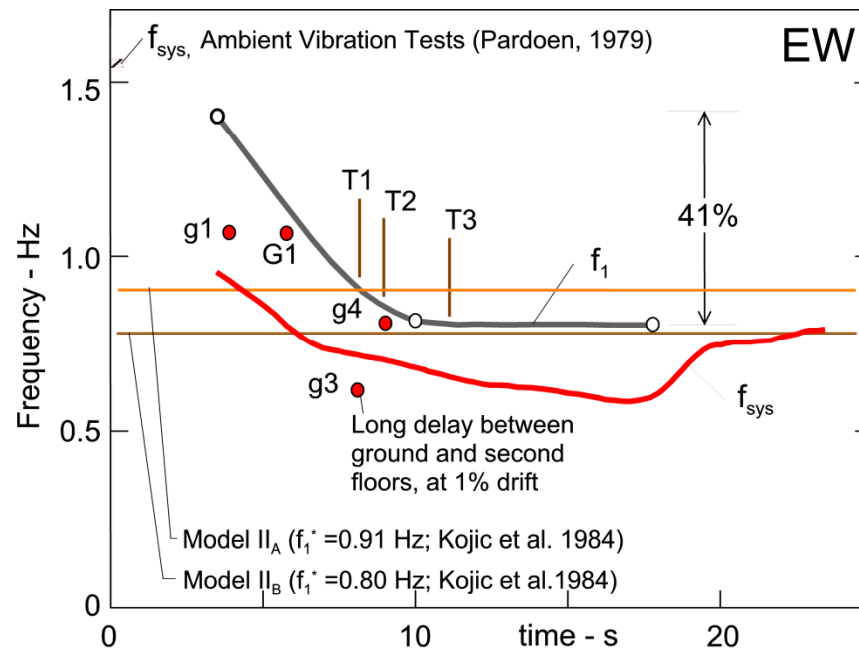
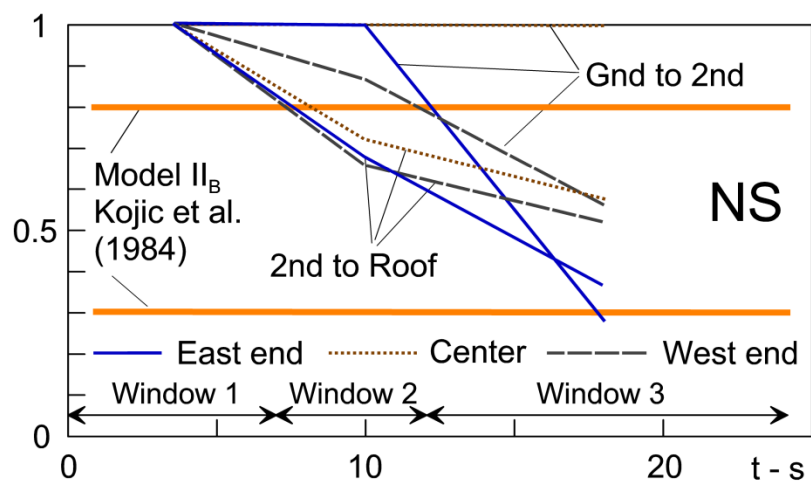
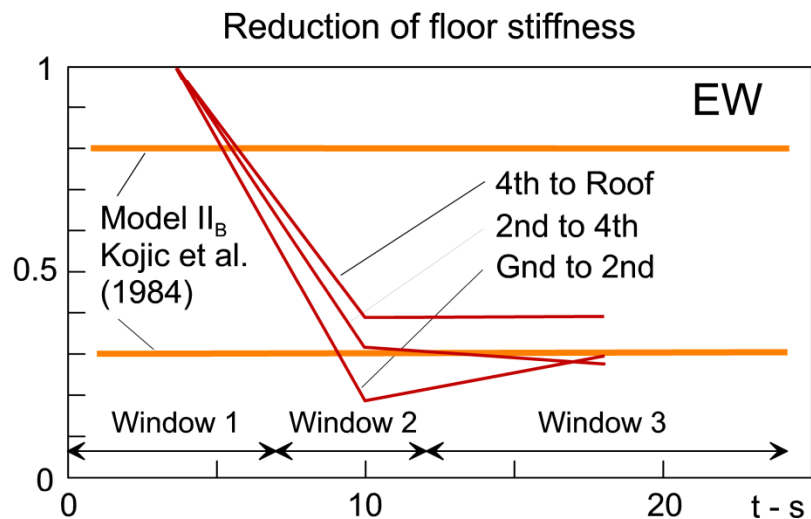


ICS building

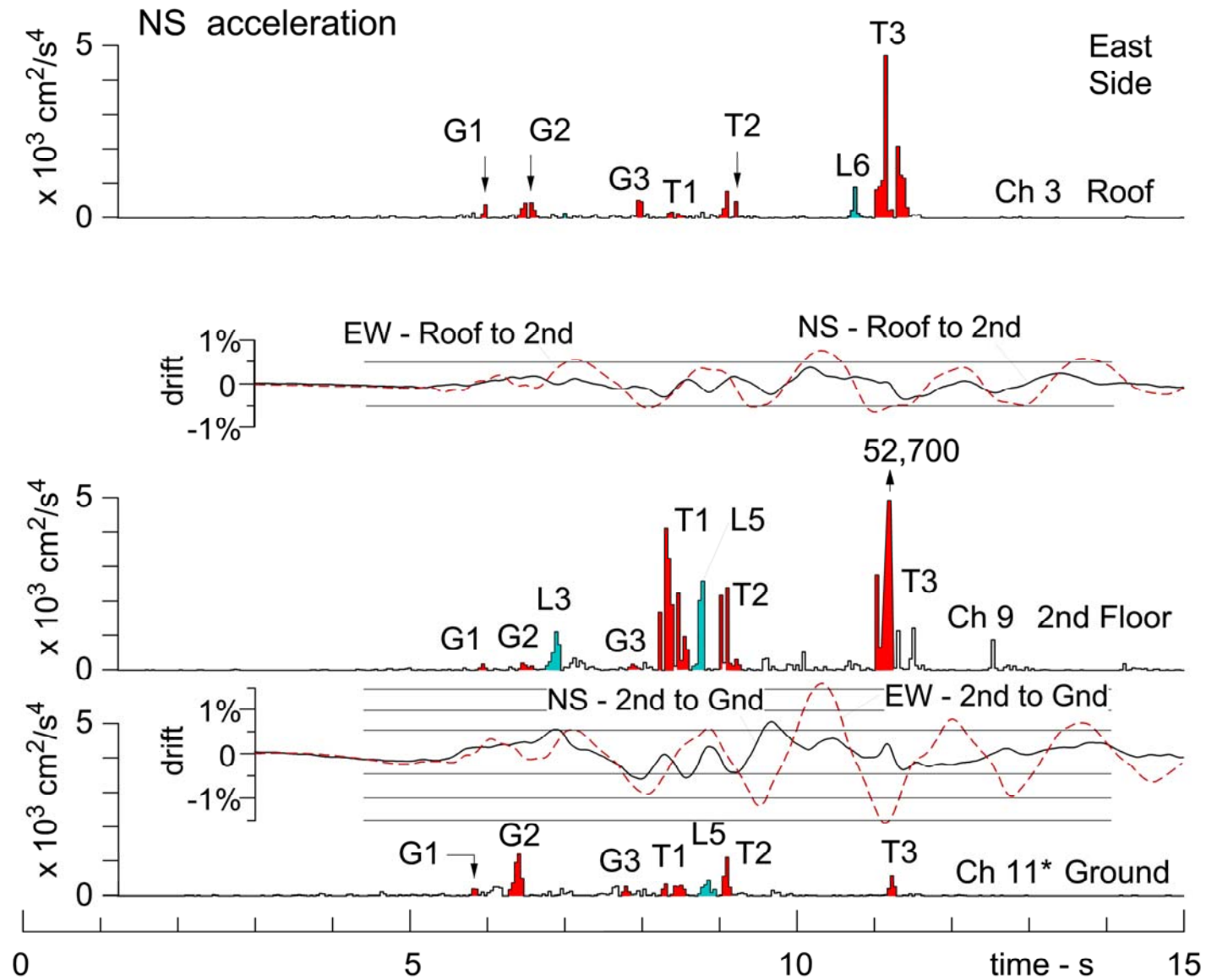
Change in travel time consistent with spatial distribution and degree of damage



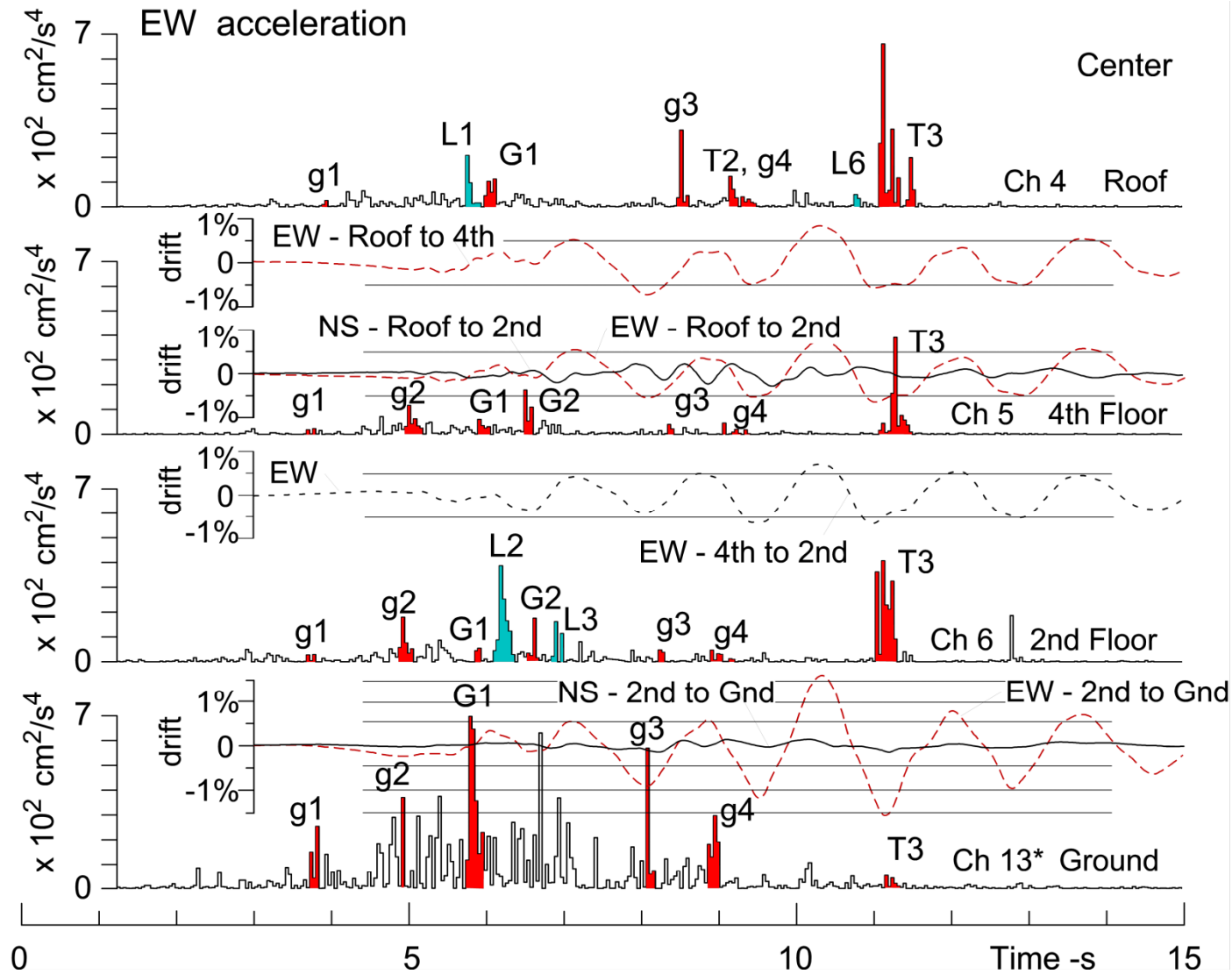
ICS building



ICS building - Novelties Analysis



ICS building - Novelties Analysis



Van Nuys building

7-story, RC, EW, 11 earthquakes and 5 ambient vibration tests in 24 years)

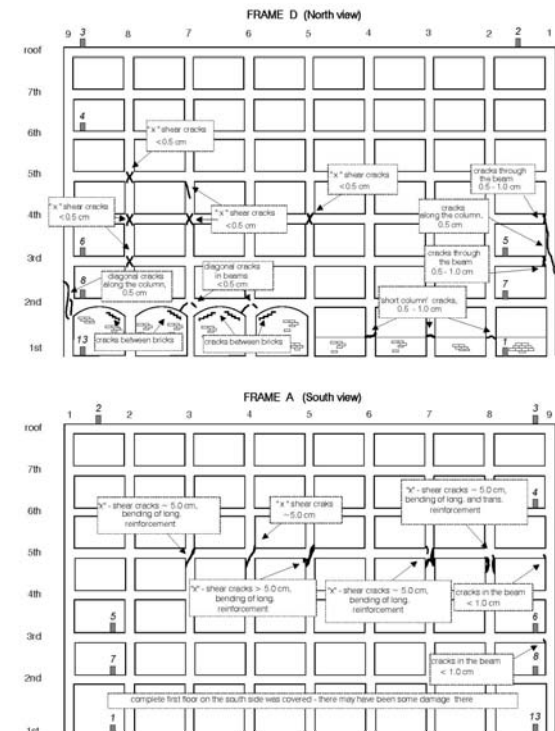
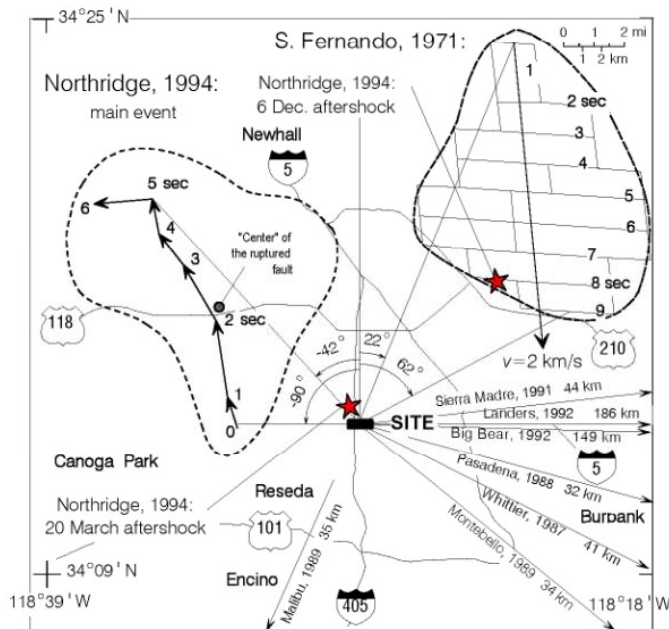


Fig. 3 Schematic representation of the damage: (top) frame D—North view, and (bottom) frame A—south view. The sensor locations for channels 1–8 and 13 (oriented towards North), are also shown.

USC Report No. CE 01-05, Trifunac and Hao, 2001

http://www.usc.edu/dept/civil_eng/Earthquake_eng/CE_Reports/01_05/index01_05.html

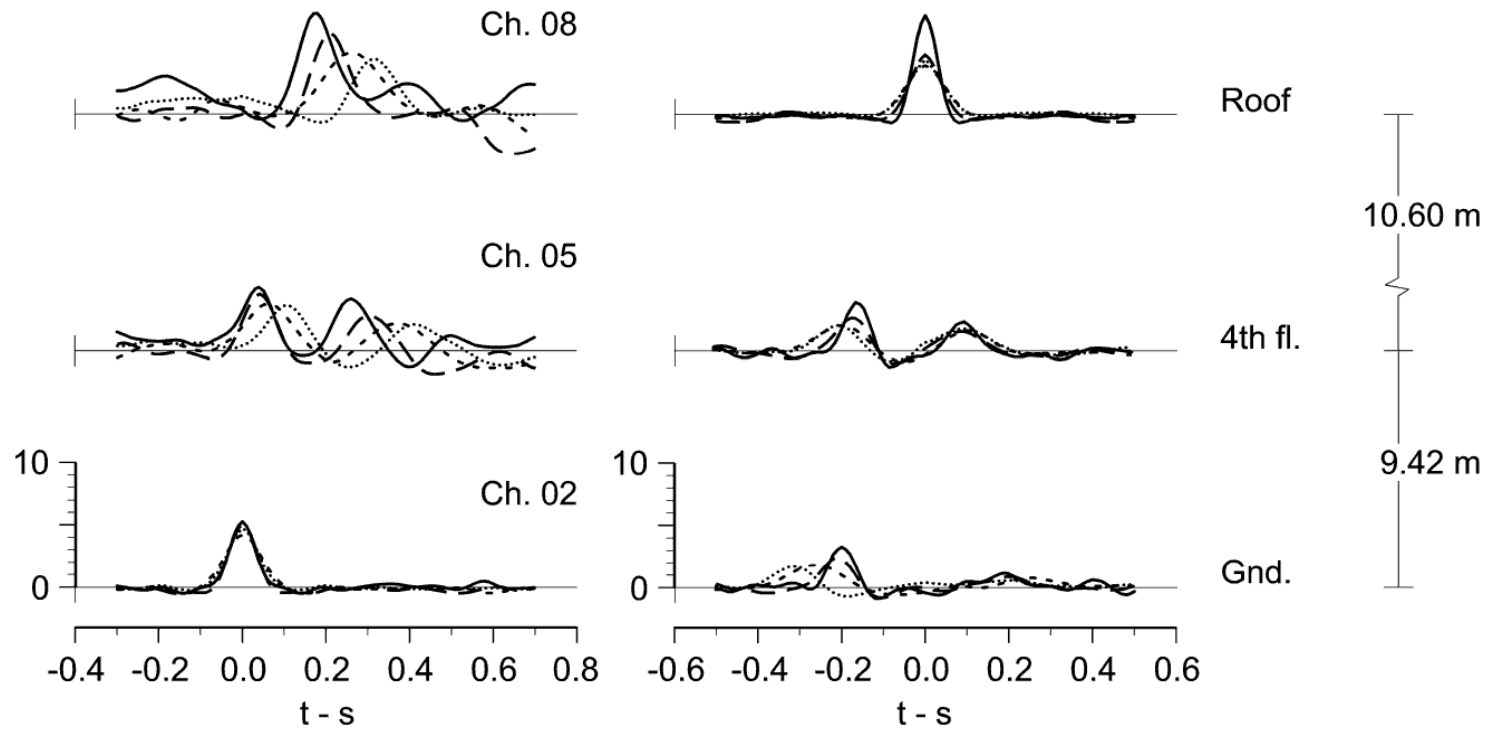
Van Nuys building



EW acceleration

San Fernando, 02/09/1971

— 0 to 5 s
- - - 5 to 11 s
· · · · 11 to 25 s
· · · · · 25 to 40 s



Todorovska and Trifunac, SCHM, 2008

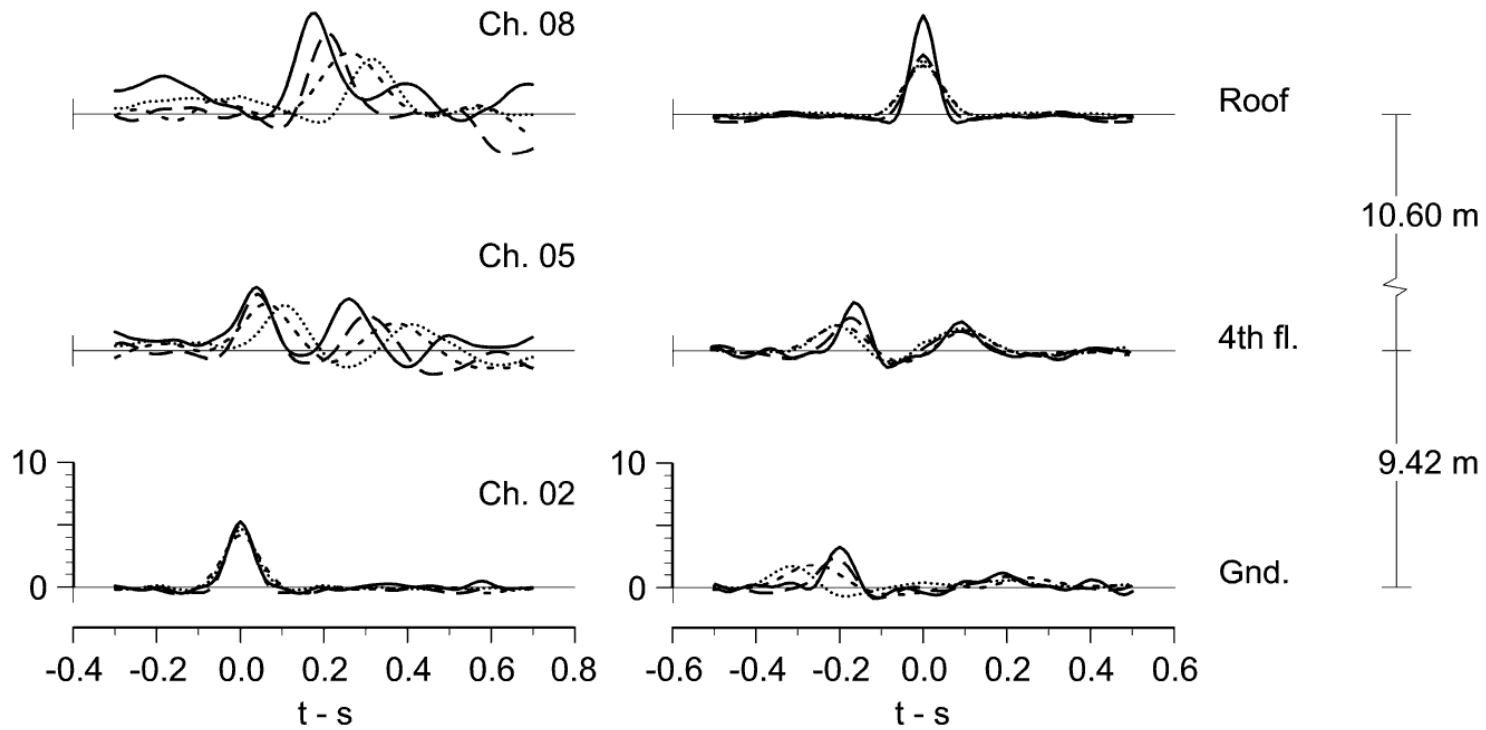
Van Nuys building



EW acceleration

San Fernando, 02/09/1971

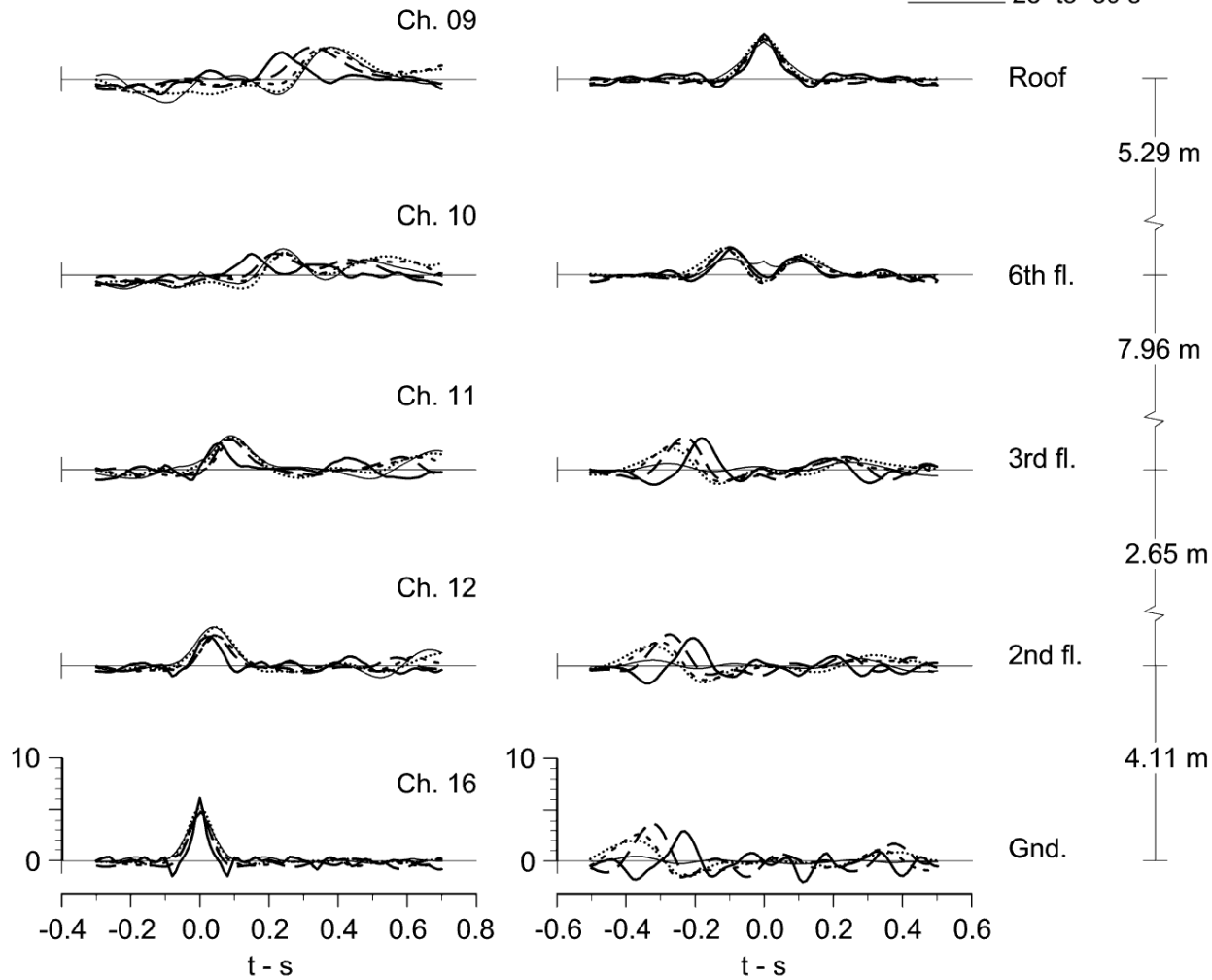
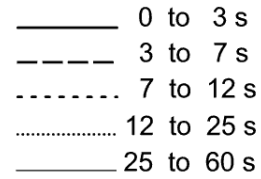
— 0 to 5 s
- - - 5 to 11 s
· · · · 11 to 25 s
· · · · · 25 to 40 s



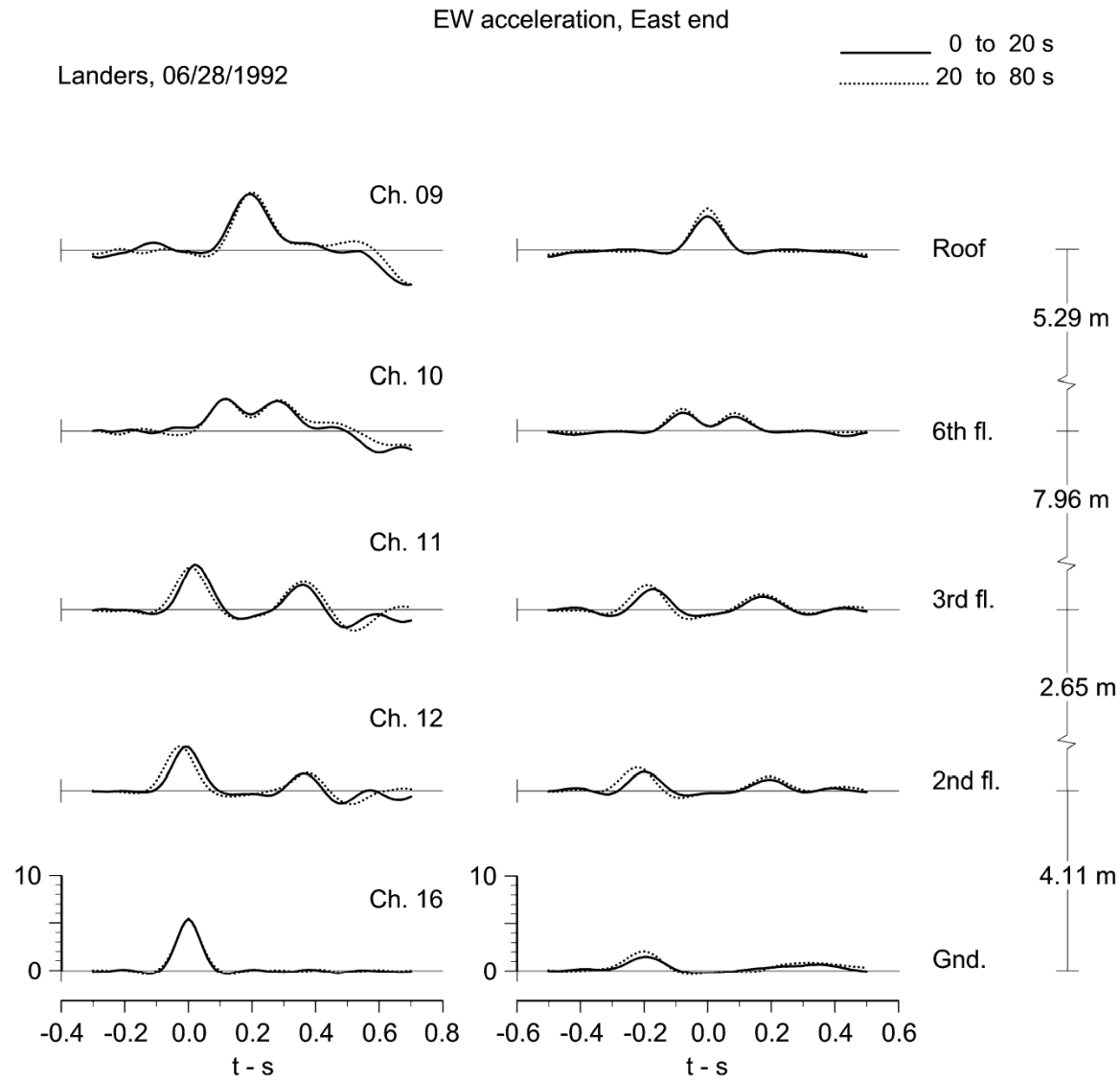
Van Nuys building

EW acceleration, East end

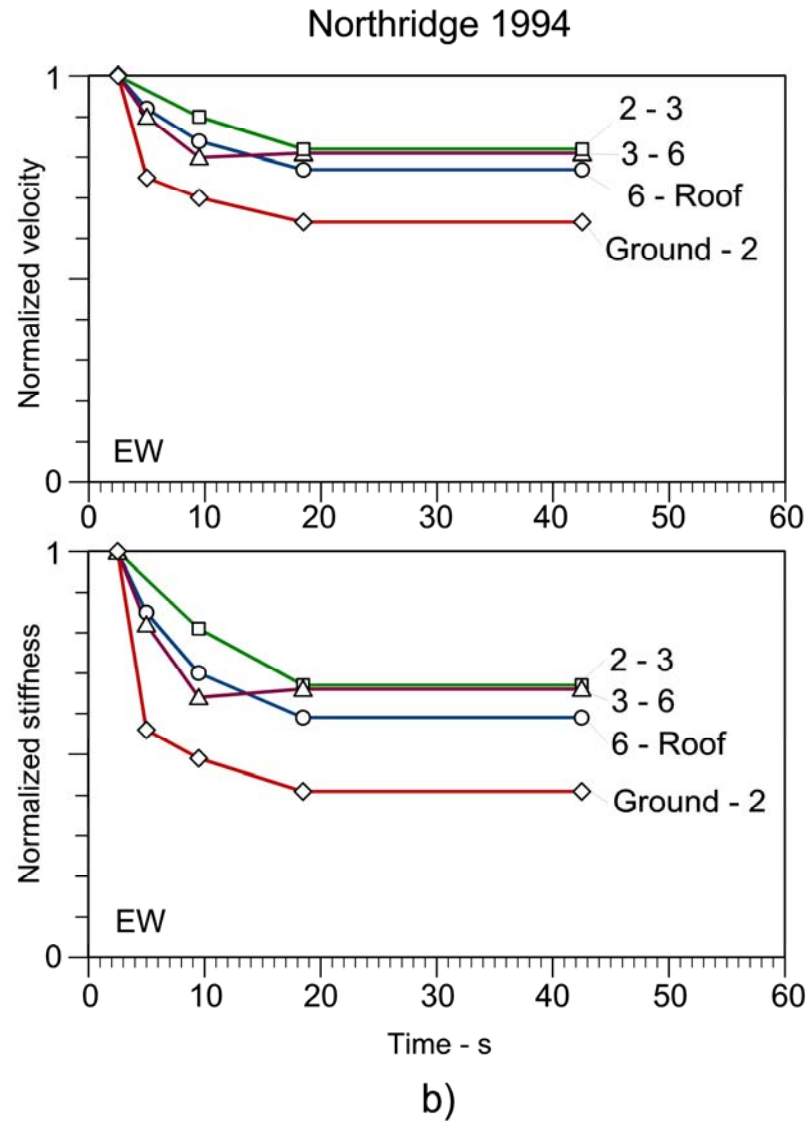
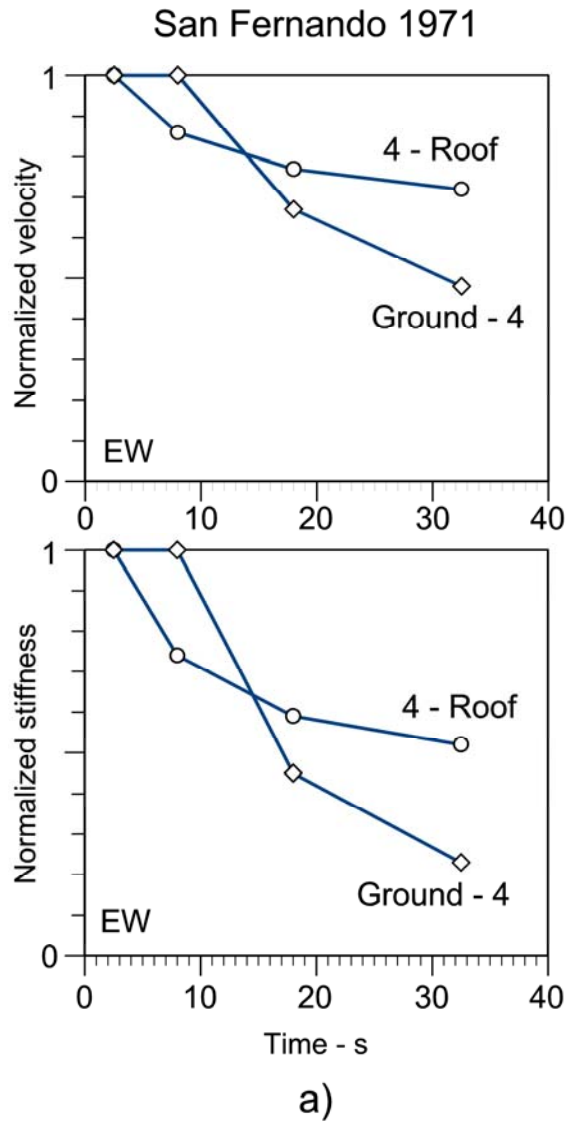
Northridge, 01/17/1994



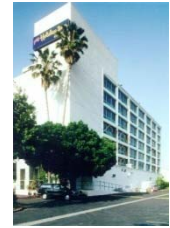
Van Nuys building



Van Nuys building



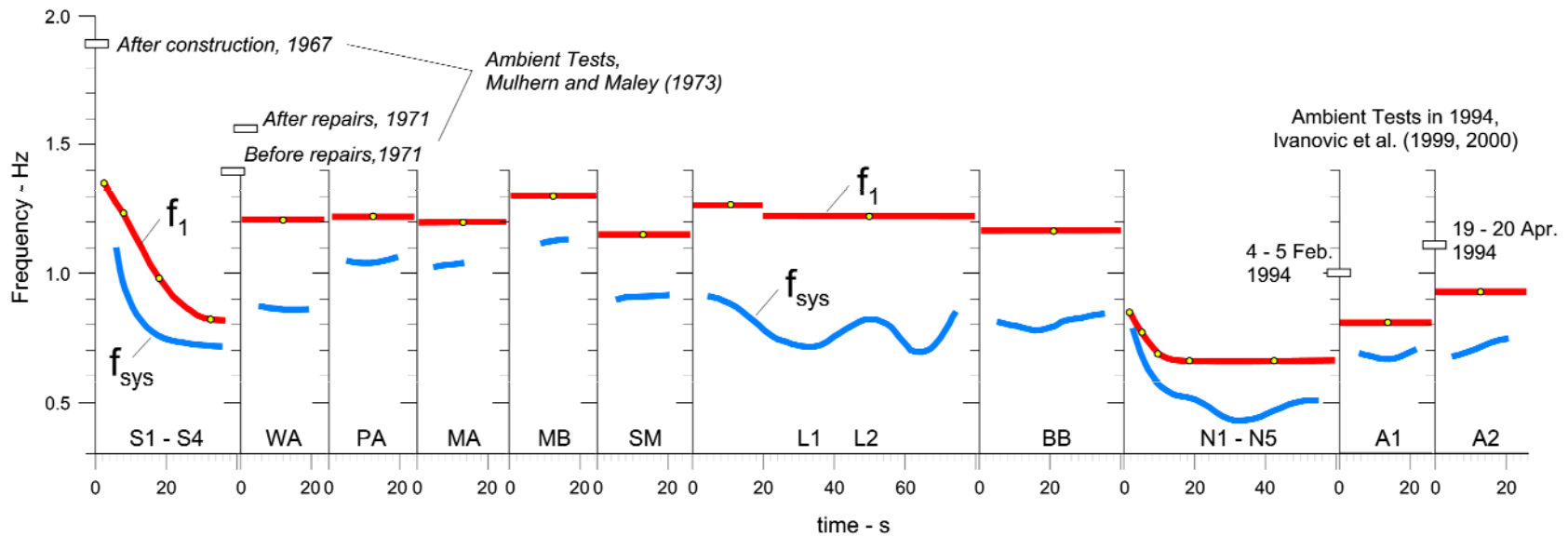
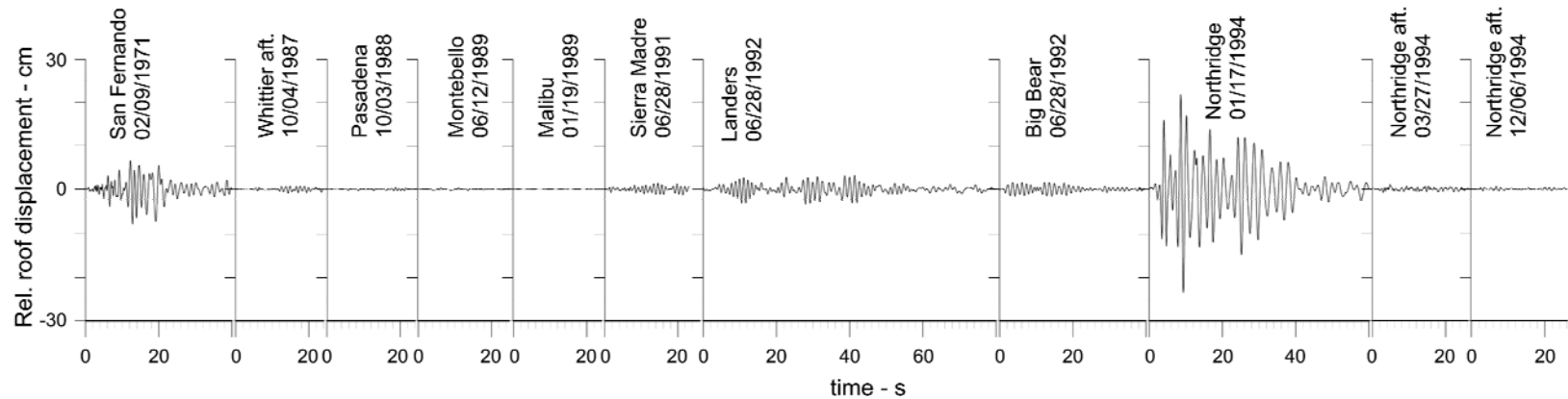
Van Nuys building



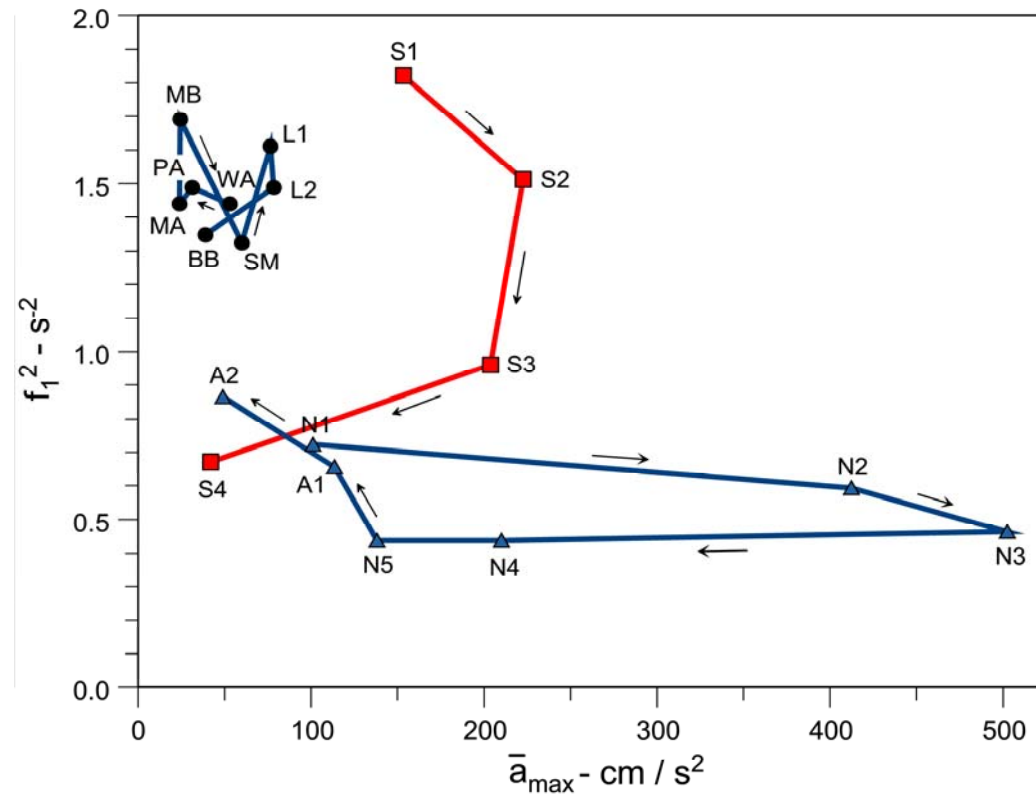
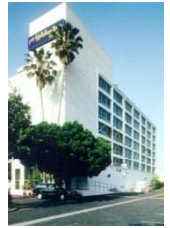
f_{sys} – form time-freq. energy distribution, f_1 – from wave travel times.

f_1 decrease: 1971 San Fernando - by ~40%. 1994 Northridge - by ~22%.

Difference between f_1 and f_{sys} is not constant (see Landers and Big Bear).



Van Nuys building



Estimation Error of the Direct Algorithm

- Infinite bandwidth:

$$\hat{h}(\omega) = 1 \Leftrightarrow h(t) = \delta(t) = \text{Dirac Delta-function}$$

- Finite bandwidth:

$$\hat{h}(\omega) = 1, \quad |\omega| \leq \omega_{\max} \Leftrightarrow h(t) = \frac{\sin \omega_{\max} t}{\pi t} = \text{sinc function}$$

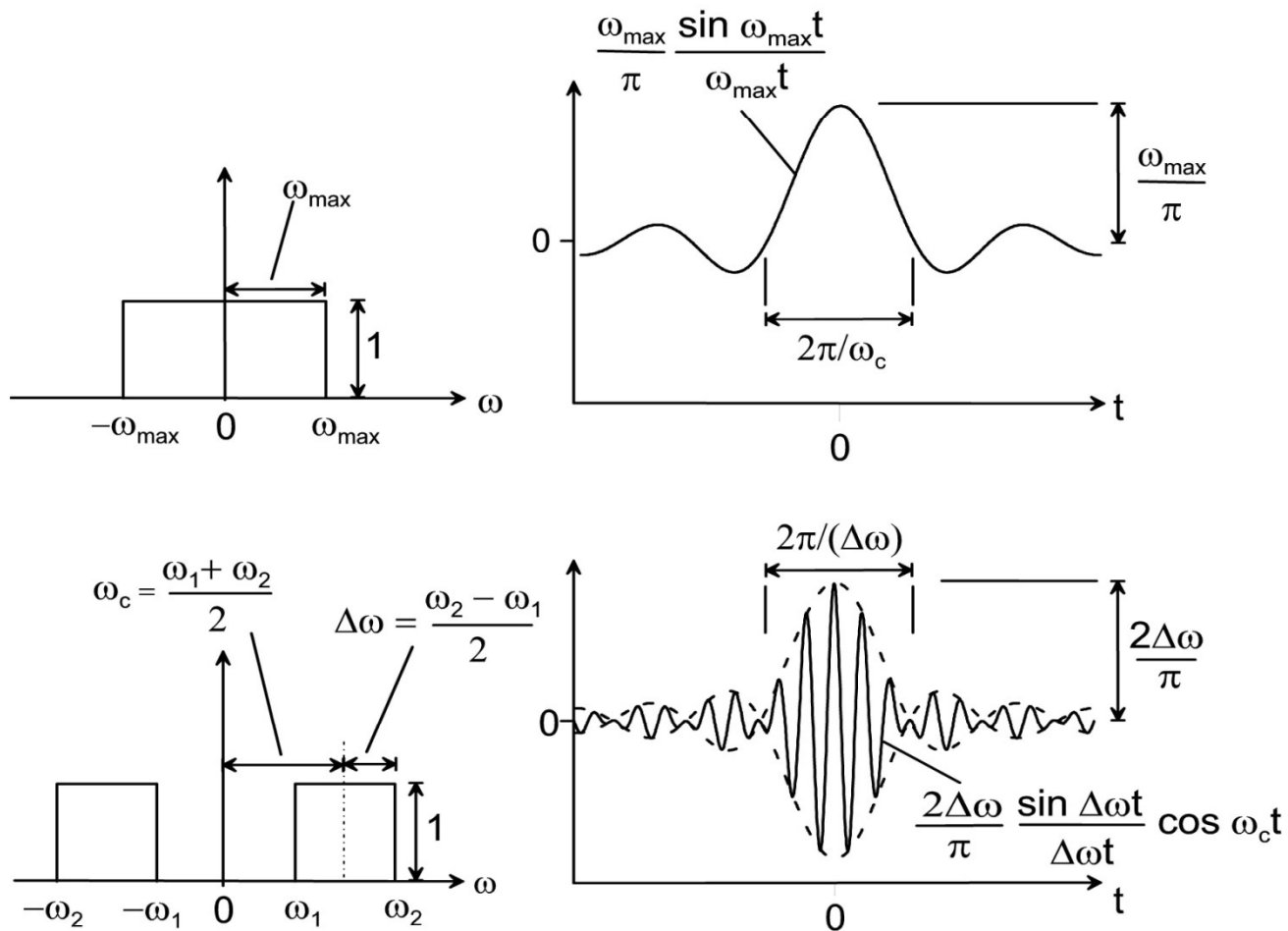
- Spread in time:

$$\text{Pulse half-width} = \Delta t = \pi / \omega_{\max} = 1 / (2 f_{\max})$$

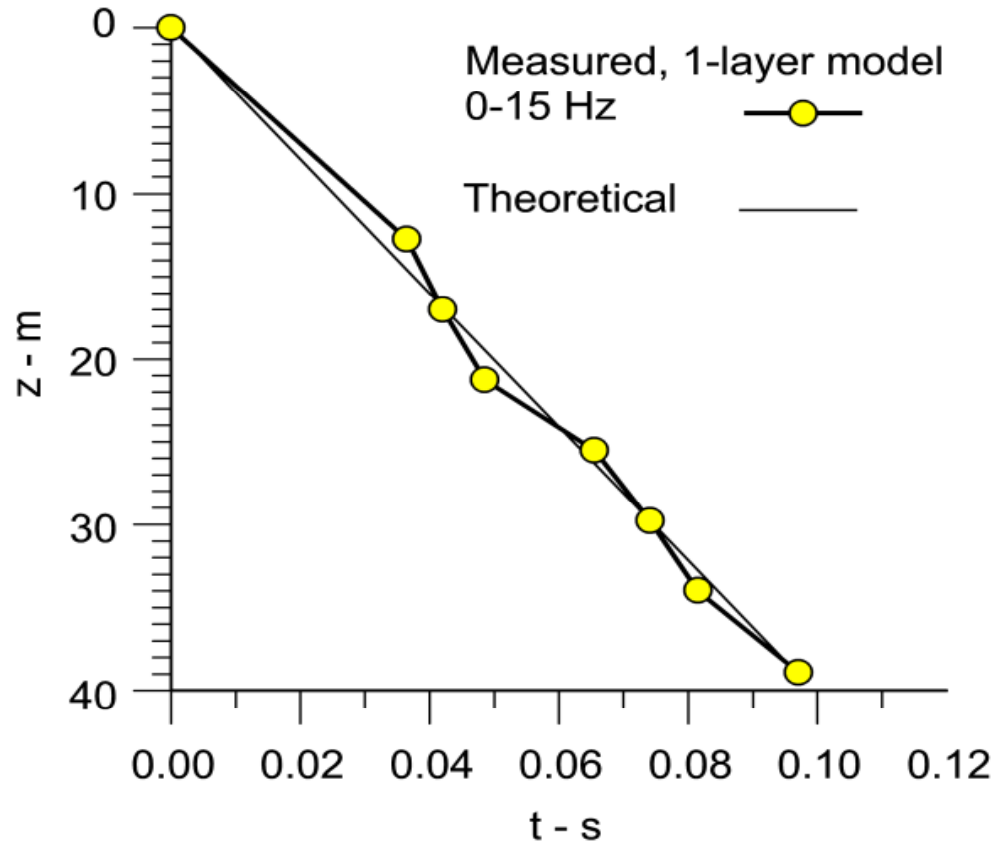
- Heisenberg-Gabor uncertainty principle implies:

$$\text{Relative error} = \frac{\Delta\beta}{\beta} = \frac{\Delta t}{\tau}$$

Estimation Error of the Direct Algorithm



Example: Uniform Shear Beam



Waveform Inversion Algorithm

- We fit by **waveform inversion** of IRFs
- Nonlinear LSQ fit: Levenberg-Marquardt Method; Simulated annealing
- **Much more accurate** estimation
- **Not limited by ray theory assumptions**
- **Uses information on pulse amplitude**, which is primarily governed by the impedance contrast - additional information
- **Frequency band – key parameter for the fit**
(It controls the pulse width)
- **Resolution**

$$h_{min} = \lambda_{min} / 4 = 1 / (4 f_{max})$$

Results

- Three buildings chosen for detailed analysis:
 - **54-story steel frame.** Is layered shear beam appropriate for such a building? What is the variability of the identified wave velocities during 5 events, none of which caused damage?
 - **9-story RC** with shear walls (NS) and central core (EW), densely instrumented. Resolution and dispersion analyzed
 - **12 story RC, lightly damaged.** Is the method sensitive to light damage?

LA 54-story office building

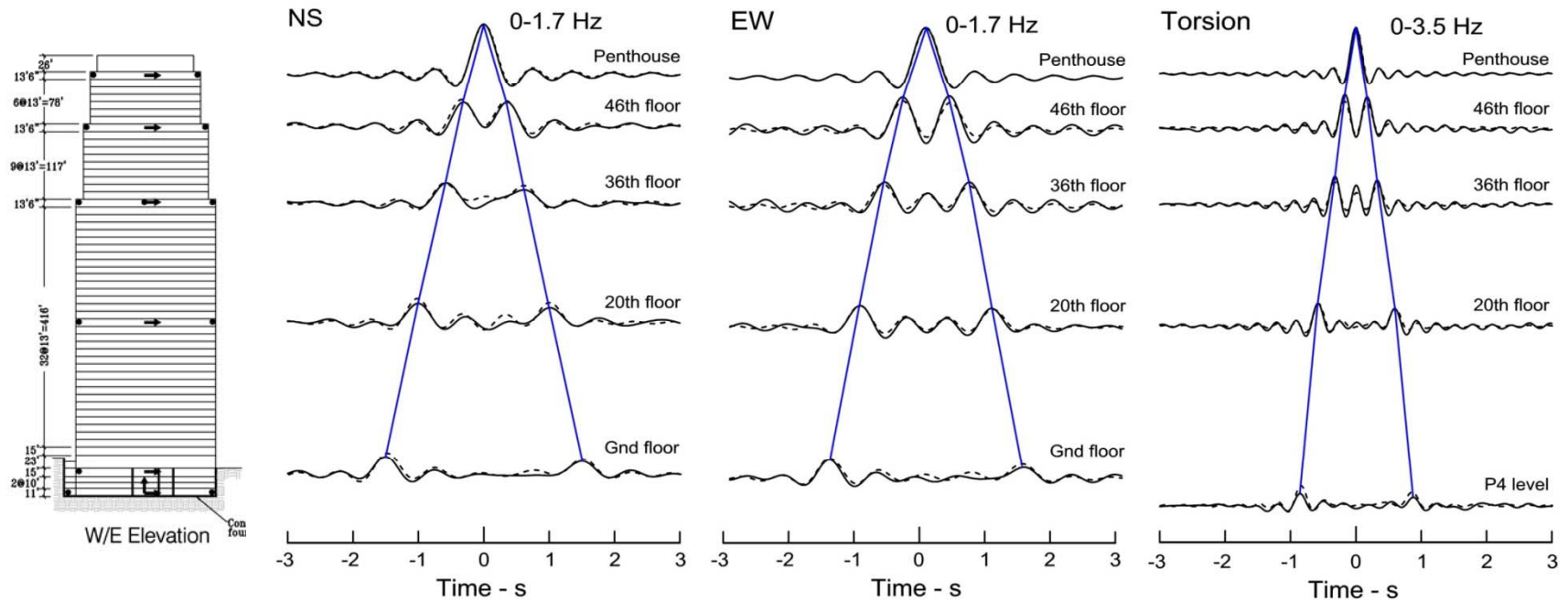
54-story, moment resisting **perimeter steel frame**, on concrete mat foundation; alluvium over sedimentary rock



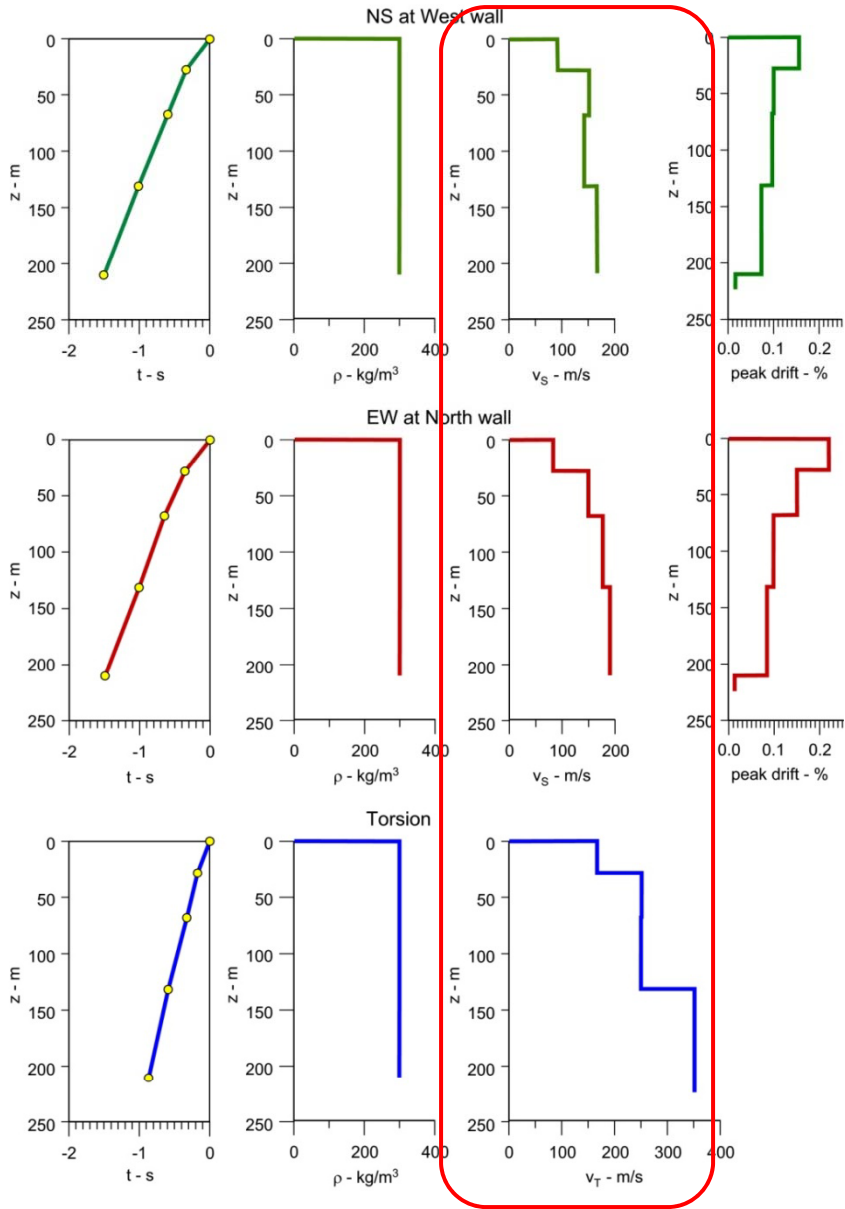
CSMIP Station 24629

Impulse Response Functions

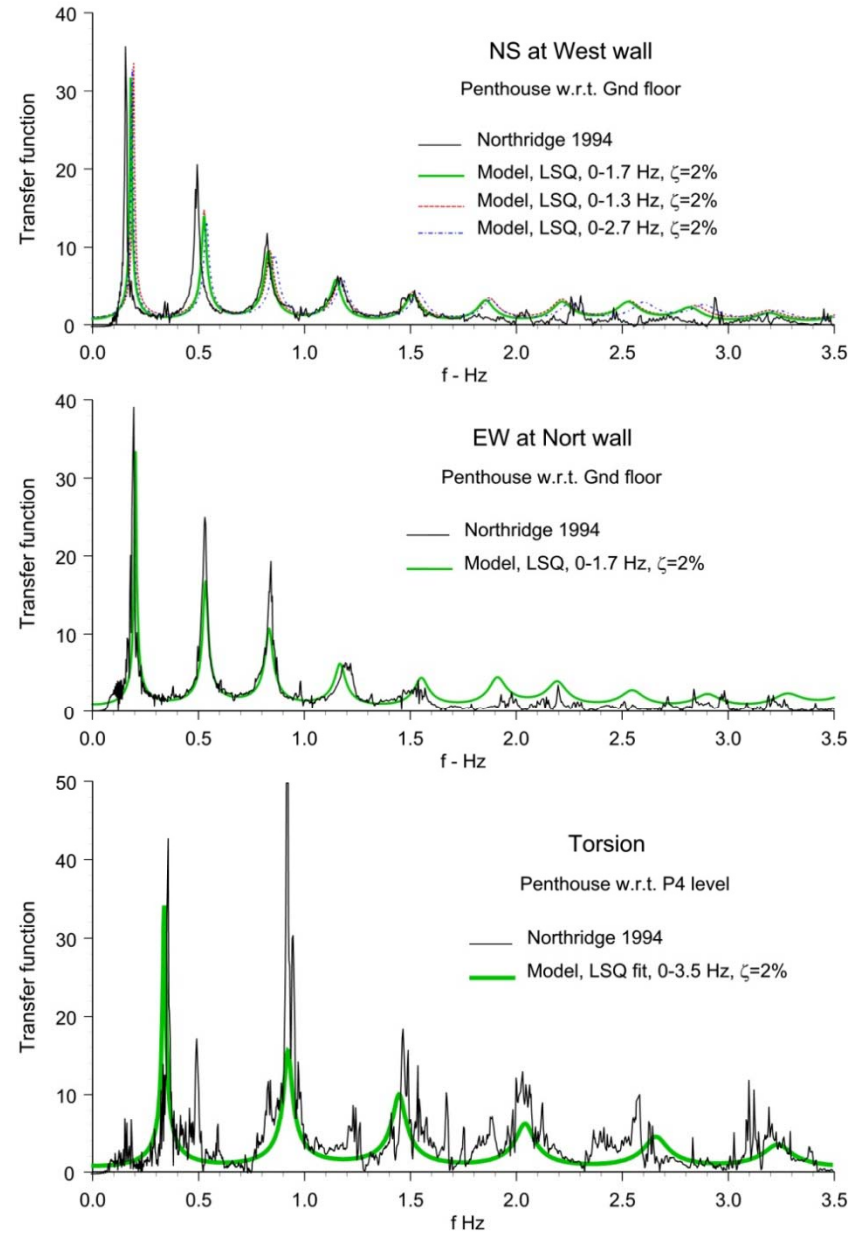
— Observed
- - - Model, LSQ fit, $\zeta = 2\%$



Identified Velocity Profiles
Los Angeles 54-story Office Bldg., Northridge, 1994



Comparison of Observed and Model Transfer Functions

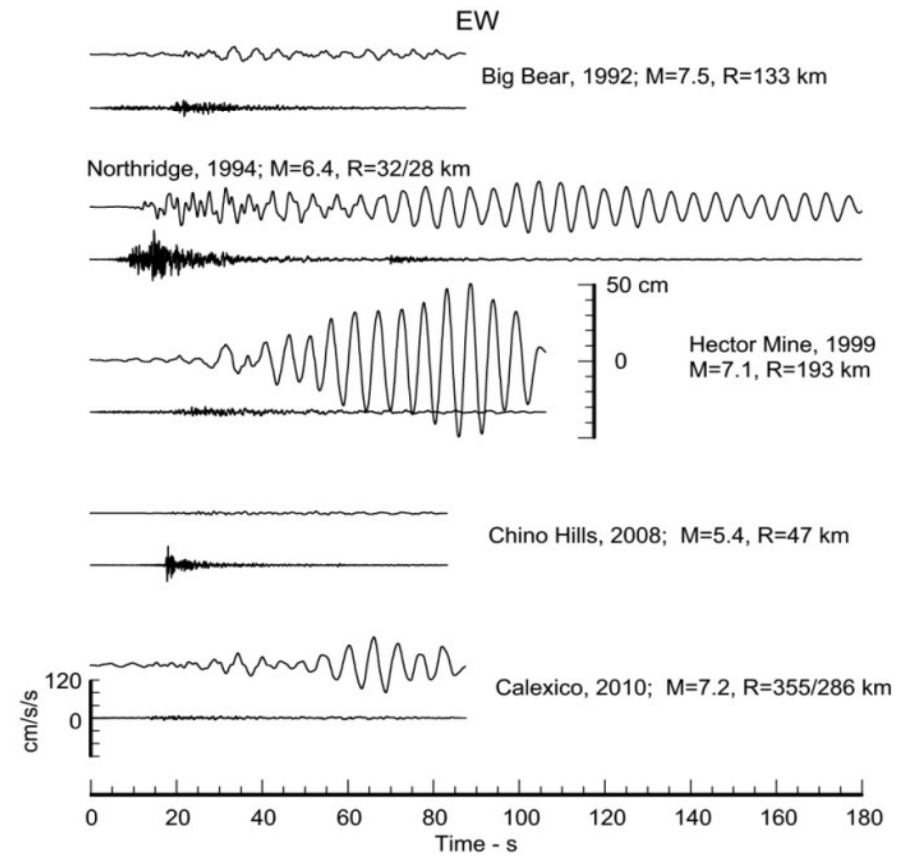
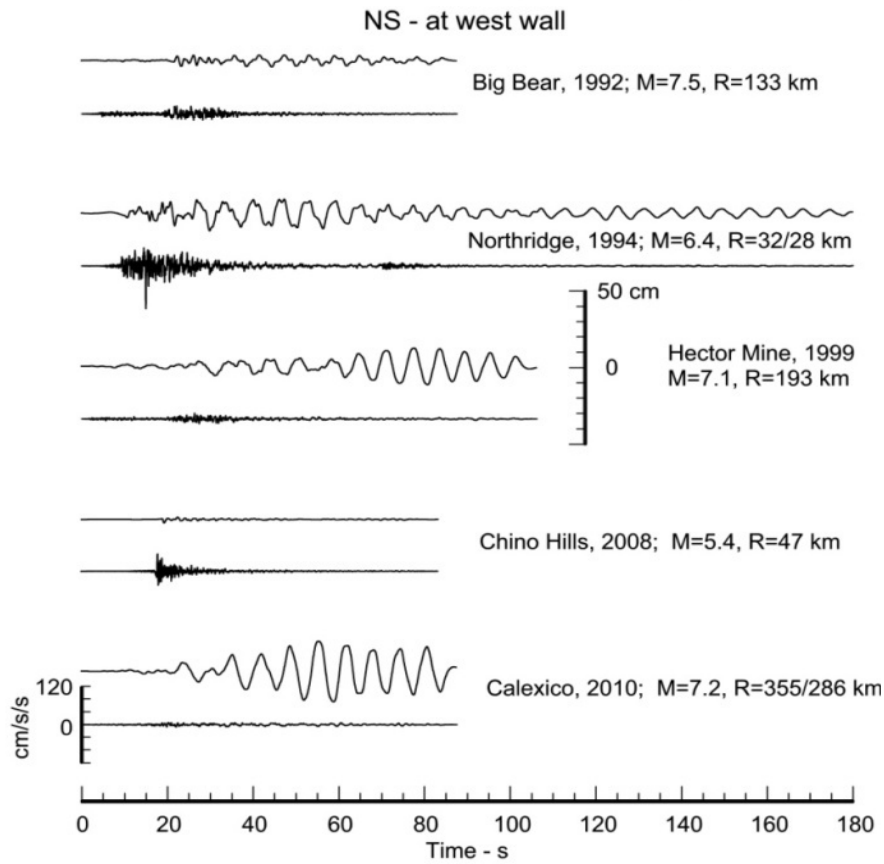


Recorded Earthquakes 1992-2010



No.	Event name	Date	ML	H - km	Epic/Fault dist - km	Gnd amax - g	Struct. amax - g	Data avail.
1	Landers	06/28/1992	7.3	1	170/158	0.040	0.130	no
2	Big Bear	06/28/1992	6.5	10	133	0.030	0.067	yes
3	Northridge	01/17/1994	6.4	19	32/28	0.140	0.190	yes
4	Hector Mine	10/16/1999	7.1	6	193	0.019	0.082	yes
5	Chino Hills	07/29/2008	5.4	14	47	0.063	0.086	yes
6	Whittier Narrows	03/16/2010	4.4	18	18	0.020	0.022	no
7	Calexico	04/04/2010	7.2	32	355/286	0.009	0.038	yes

Base acceleration (bottom) and Roof displ. (bottom)



Interstory Drift



NS - at west wall

Big Bear, 1992; M=7.5, R=133 km



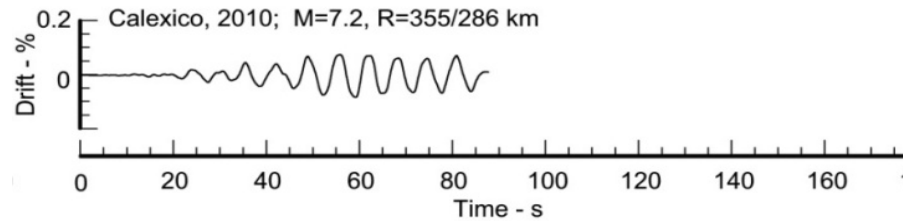
Northridge, 1994; M=6.4, R=32/28 km



Hector Mine, 1999; M=7.1, R=193 km



Chino Hills, 2008; M=5.4, R=47 km

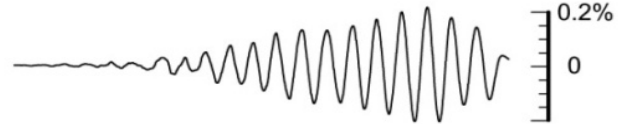


EW

Big Bear, 1992; M=7.5, R=133 km

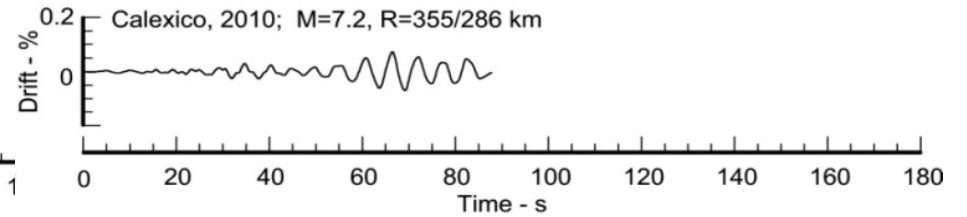


Northridge, 1994; M=6.4, R=32/28 km

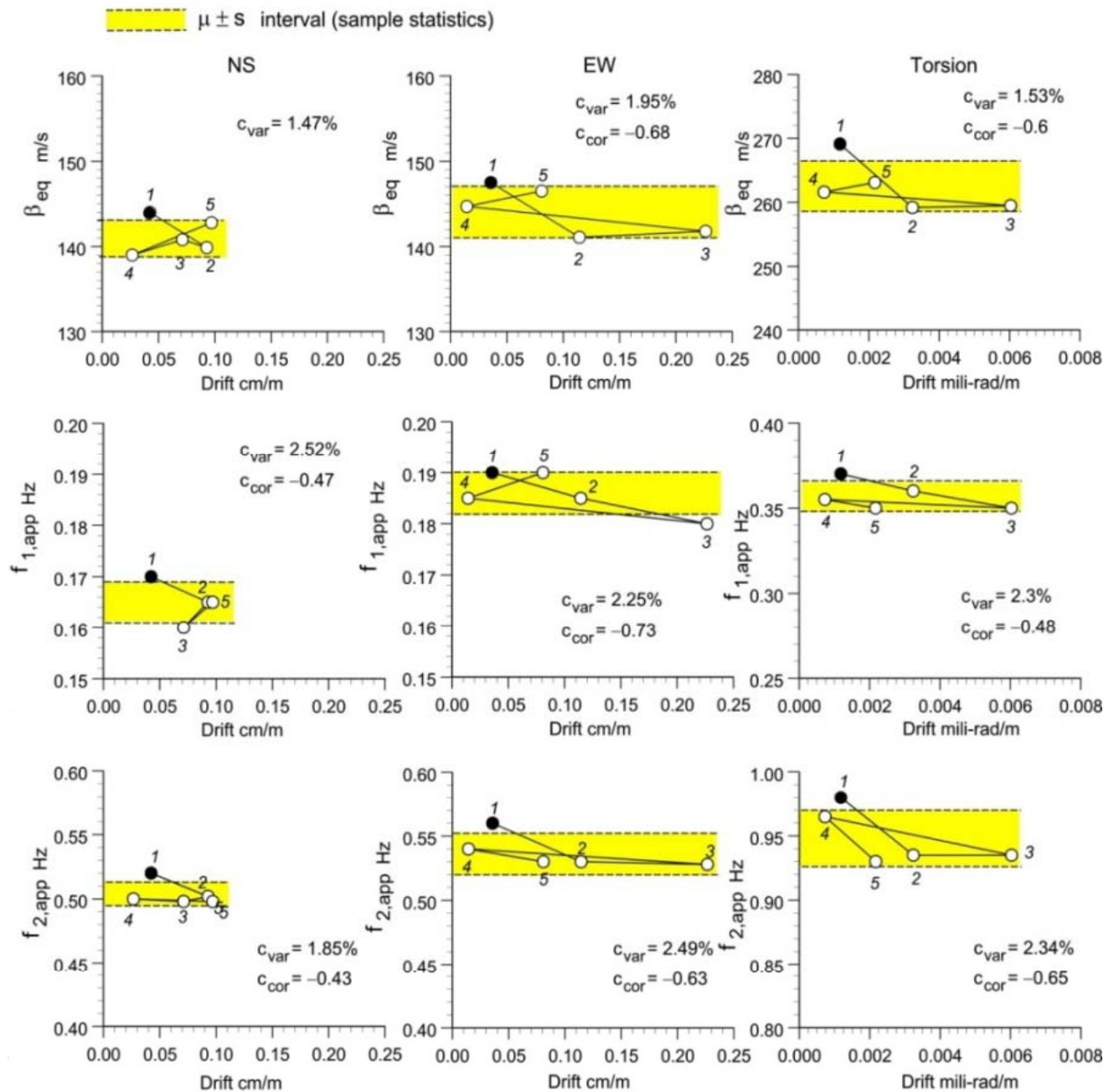


Hector Mine, 1999
M=7.1, R=193 km

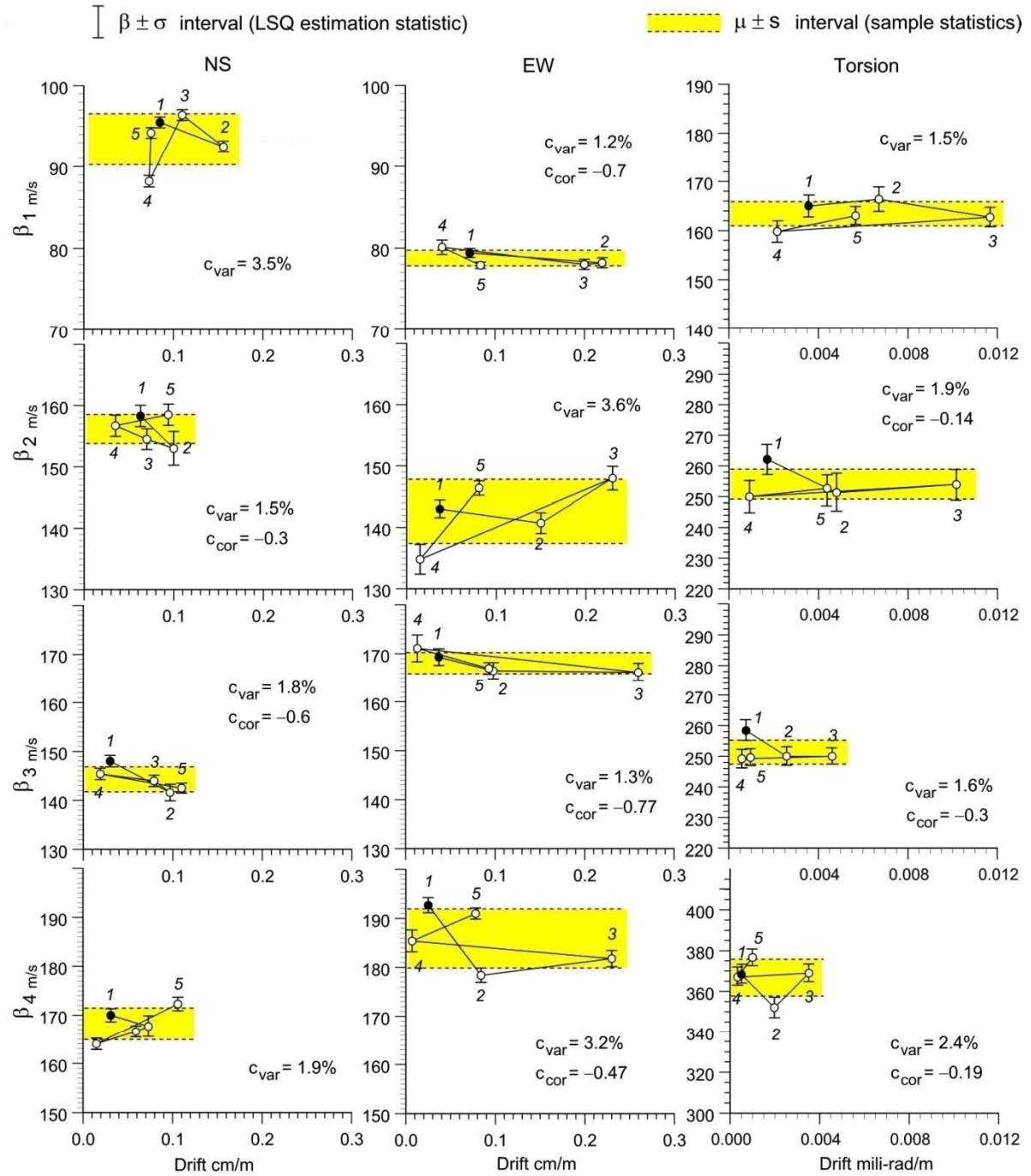
Chino Hills, 2008; M=5.4, R=47 km



Change in global parameters



Change in local (layers) parameters

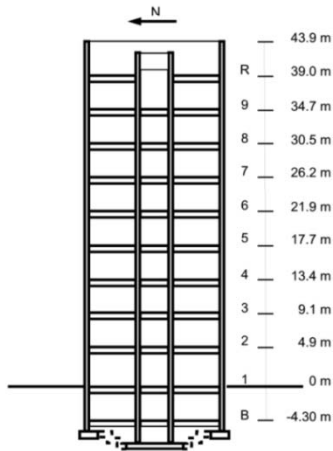


Millikan Library

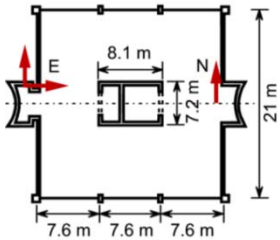
9-story, RC structure
NSMIP Station 5407



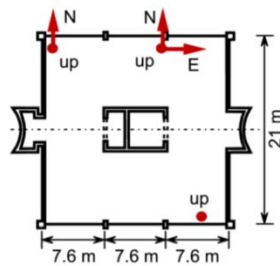
(a)



(b)



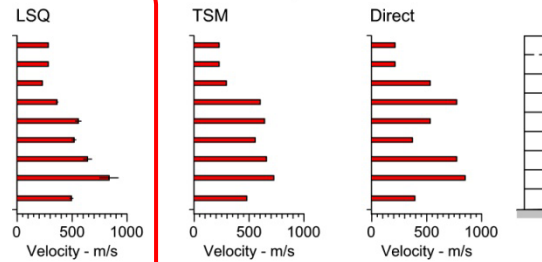
(c)



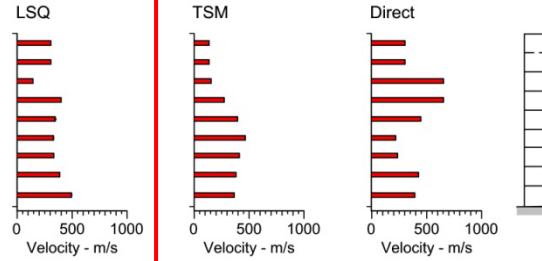
(d)

Comparison of different fitting algorithms

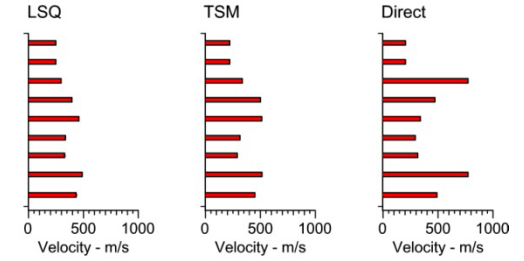
NS: 0-15 Hz; 8-layer model



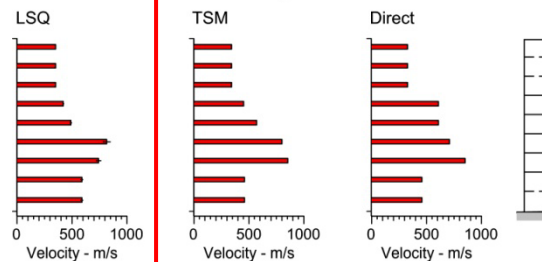
EW: 0-7.5 Hz; 8-layer model

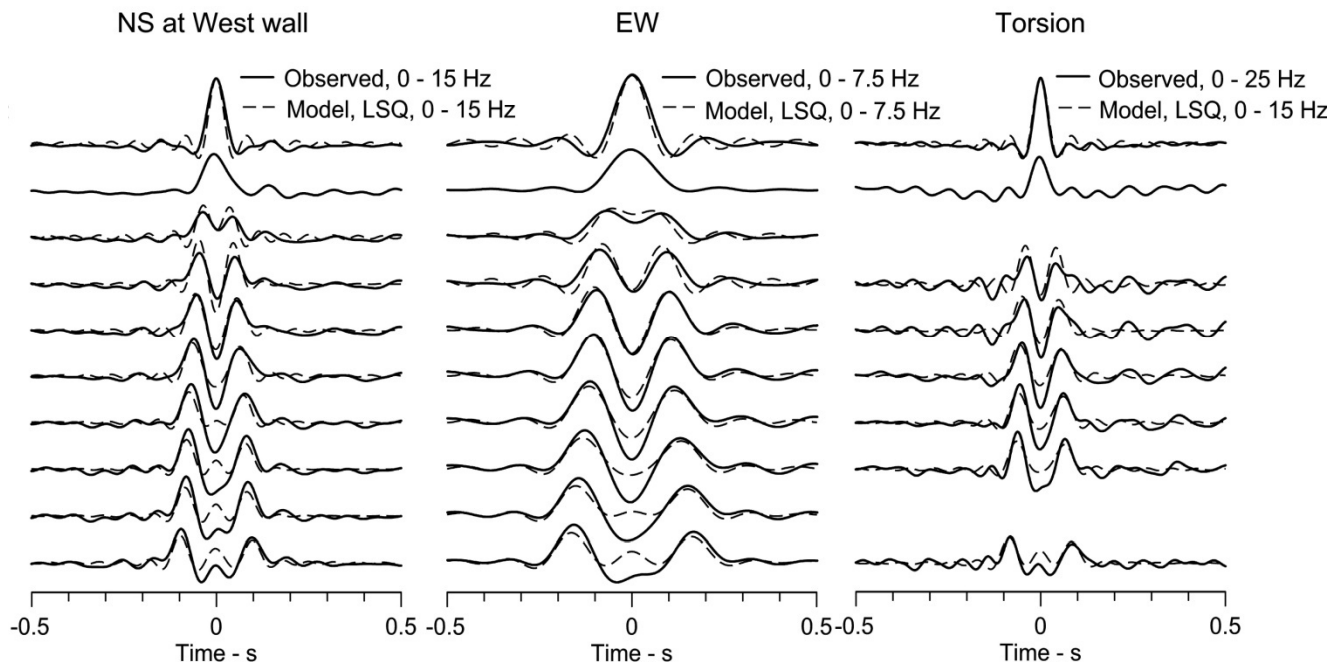


EW: 7-15 Hz; 8-layer model

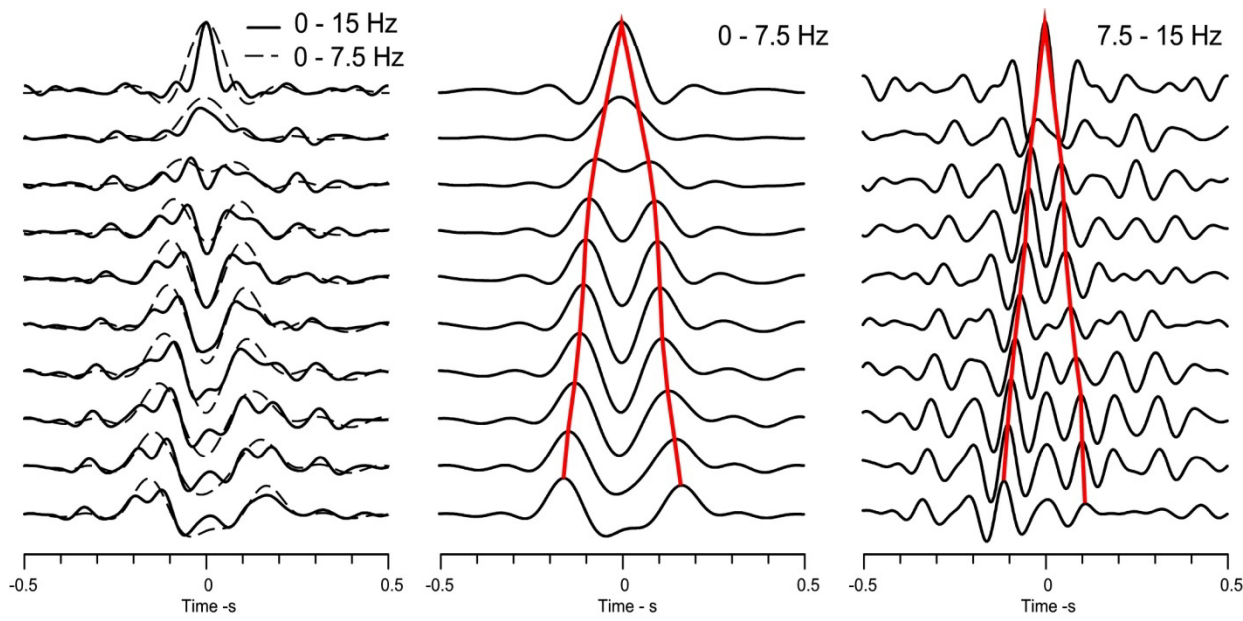


Tor: 0-25 Hz; 6-layer model

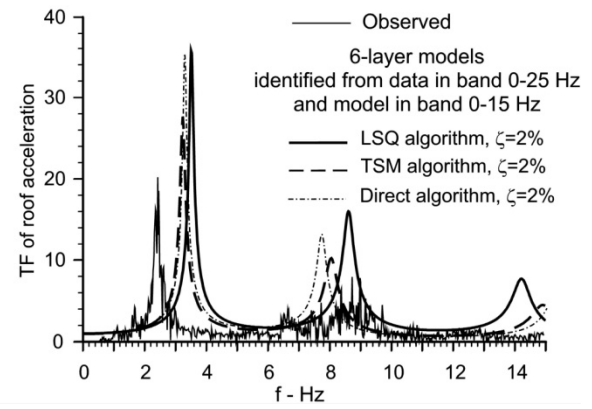
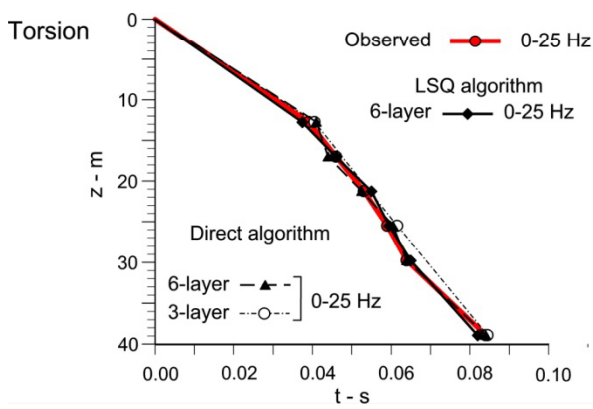
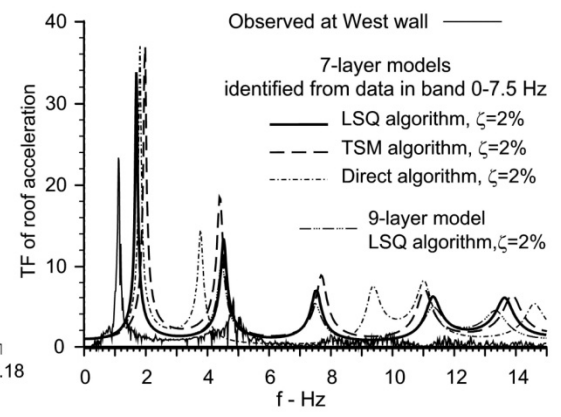
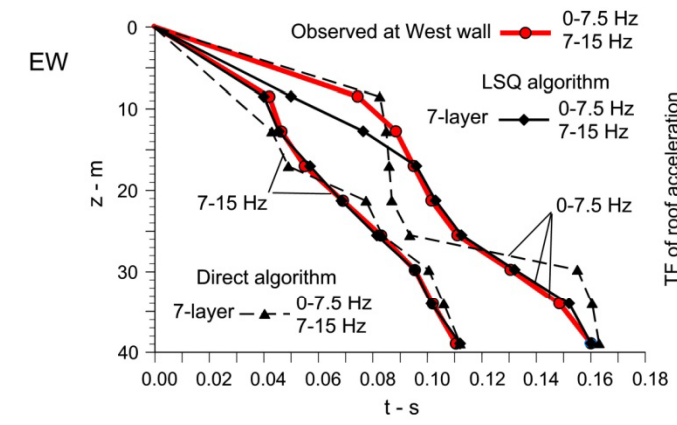
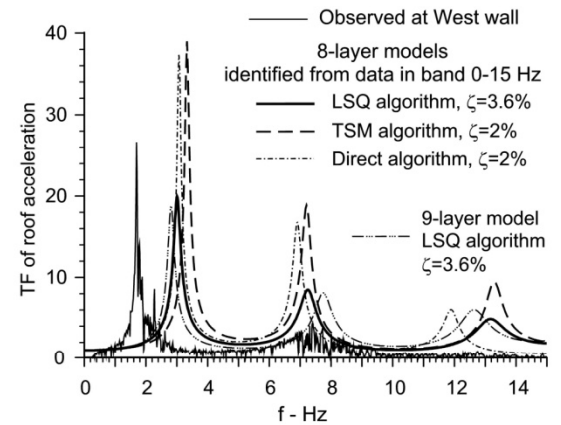
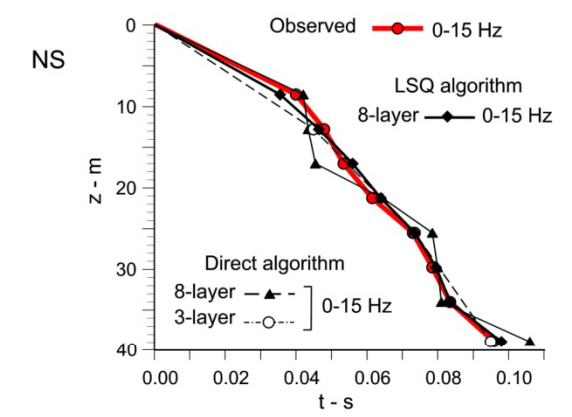




Agreement of IRFs: NS, EW and Tor



Evidence of dispersion in EW response

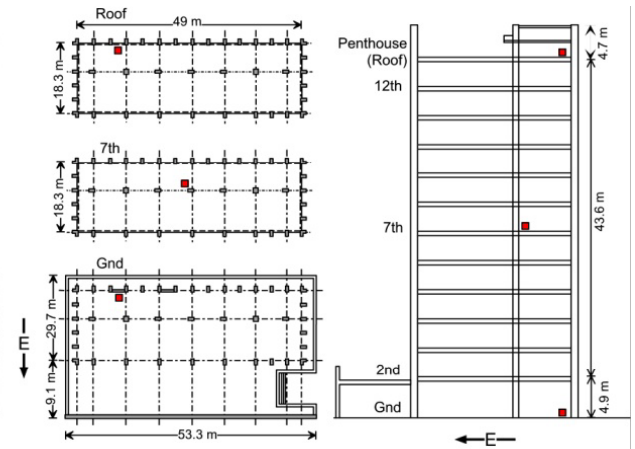


Agreement of Pulse Arrival Times and TFs

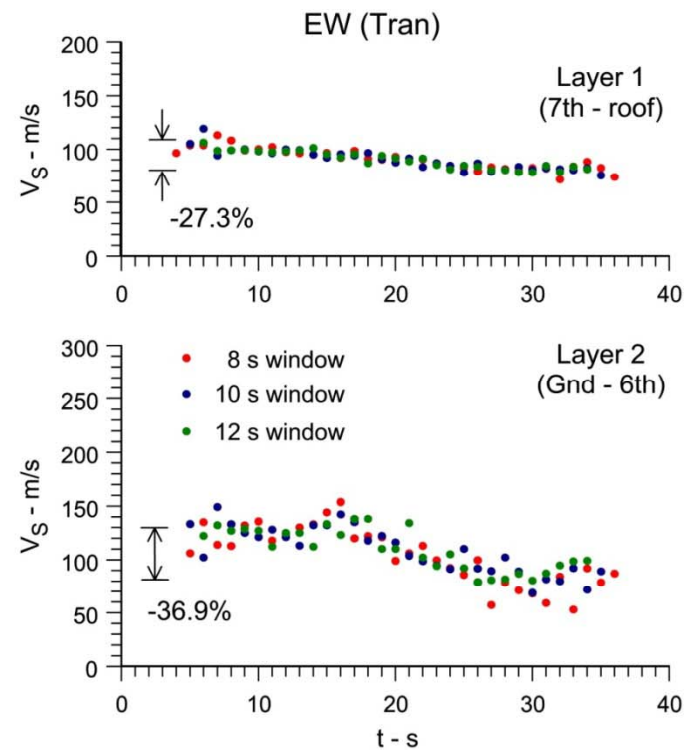
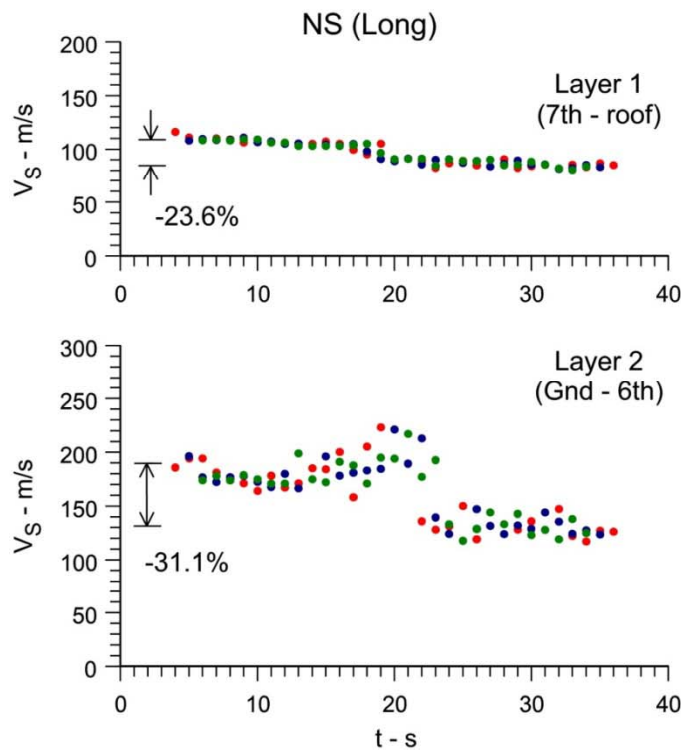
Sherman Oaks 12-story, RC bldg

NSMIP 0466

Lightly damaged in 1971

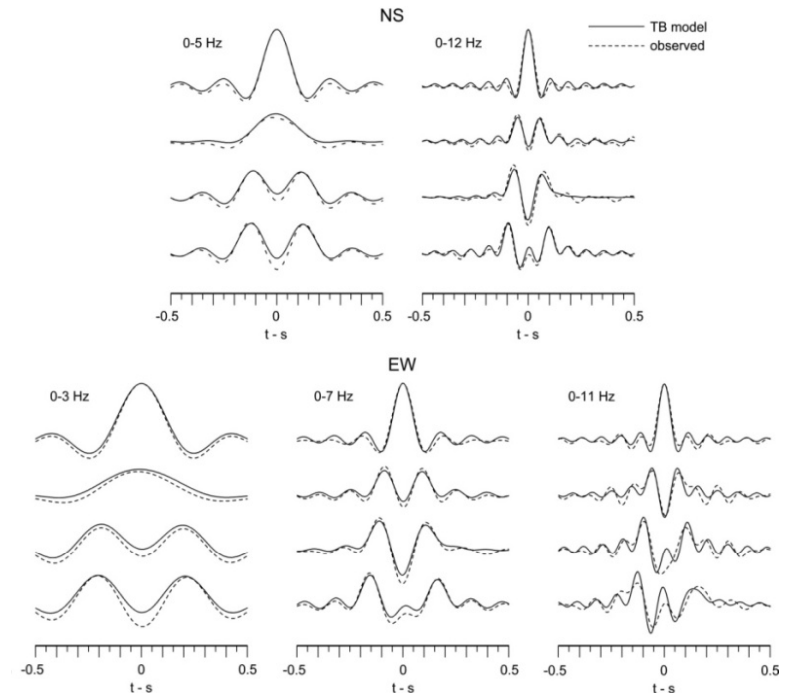
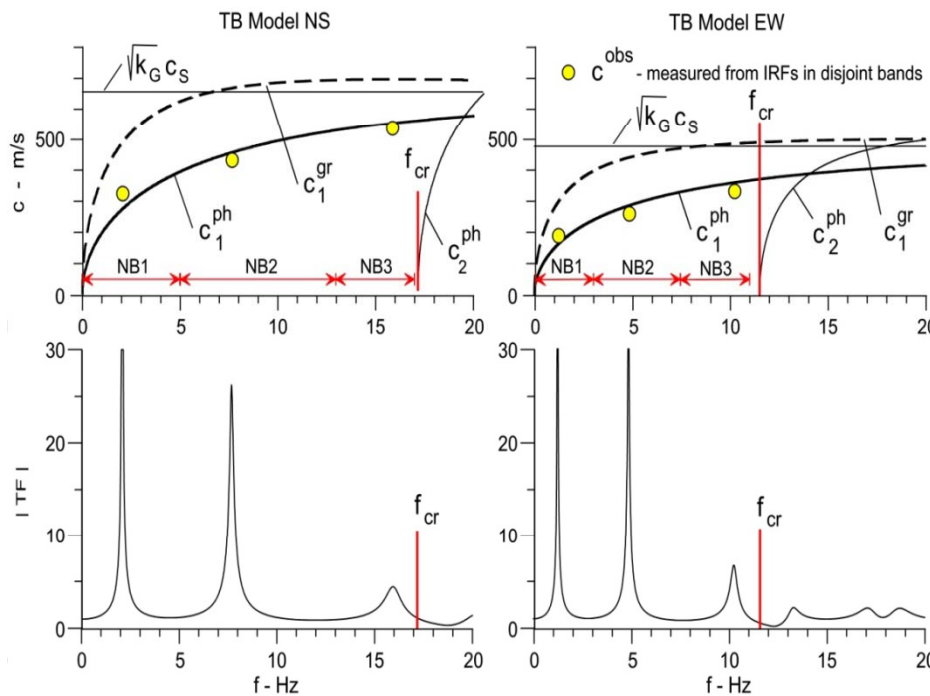
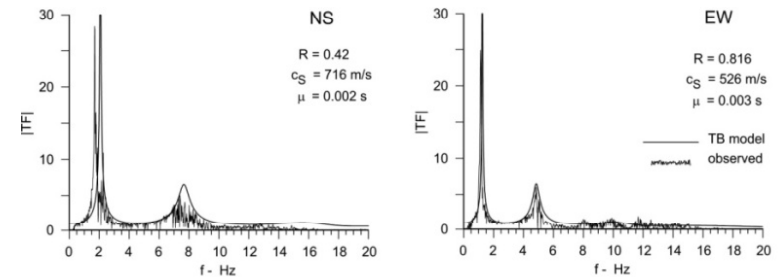
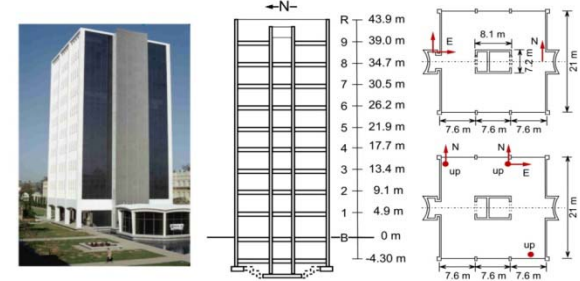


Moving window waveform inversion (Levenberg-Marquardt)



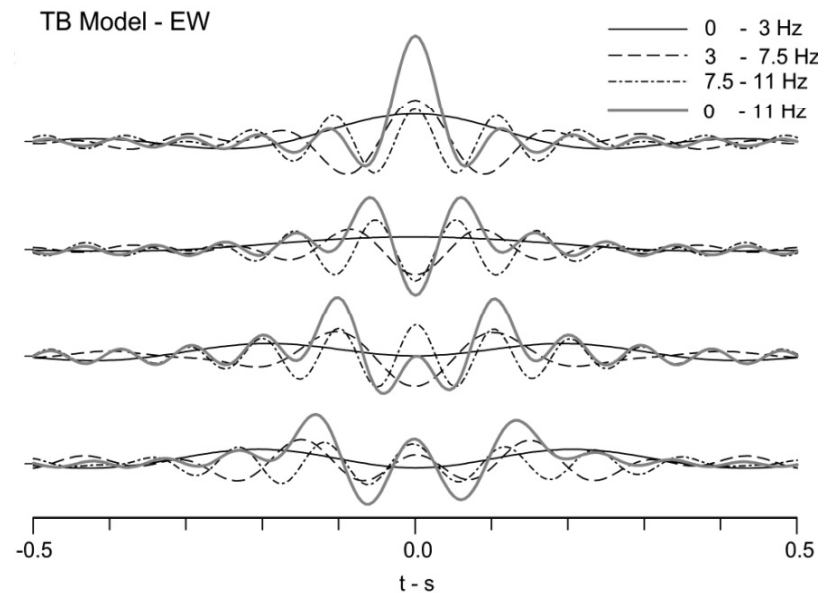
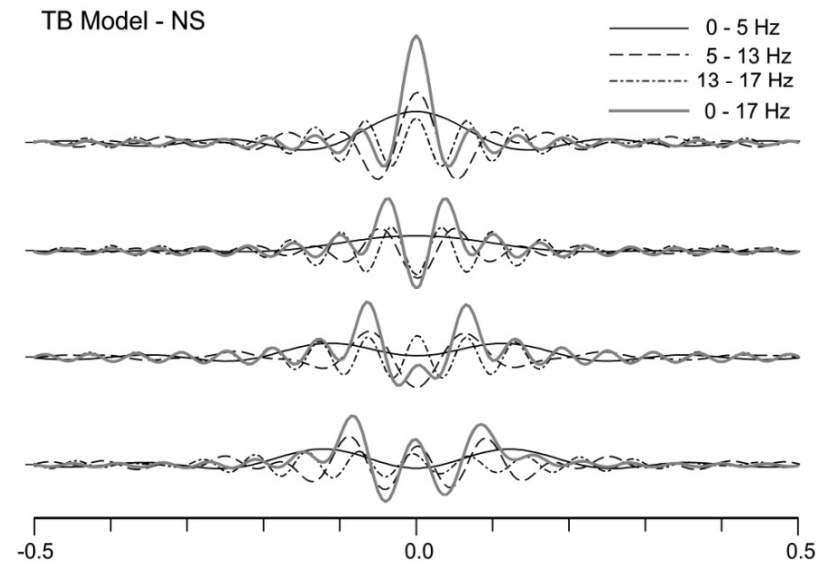
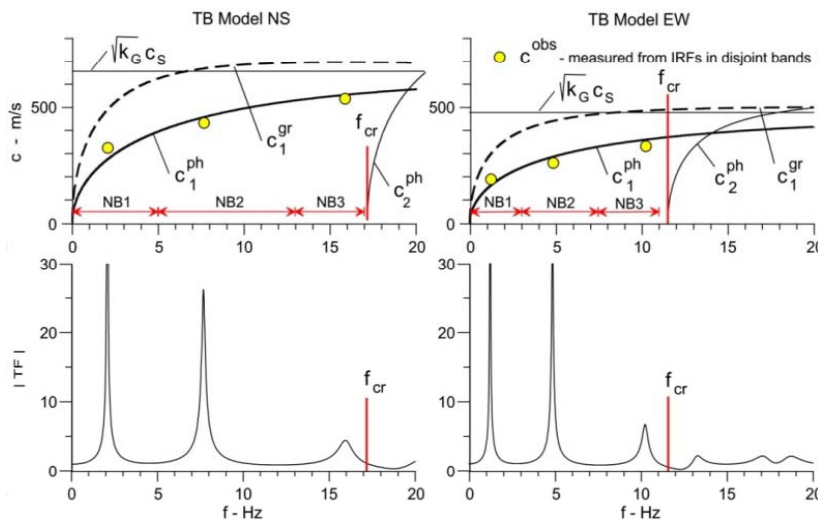
Dispersion due to Bending

- Timoshenko beam model of Millikan library : shear, bending, rotatory inertia; (Timoshenko, 1921; Ebrahimiyan and Todorovska, 2013a,b)



Dispersion due to Bending

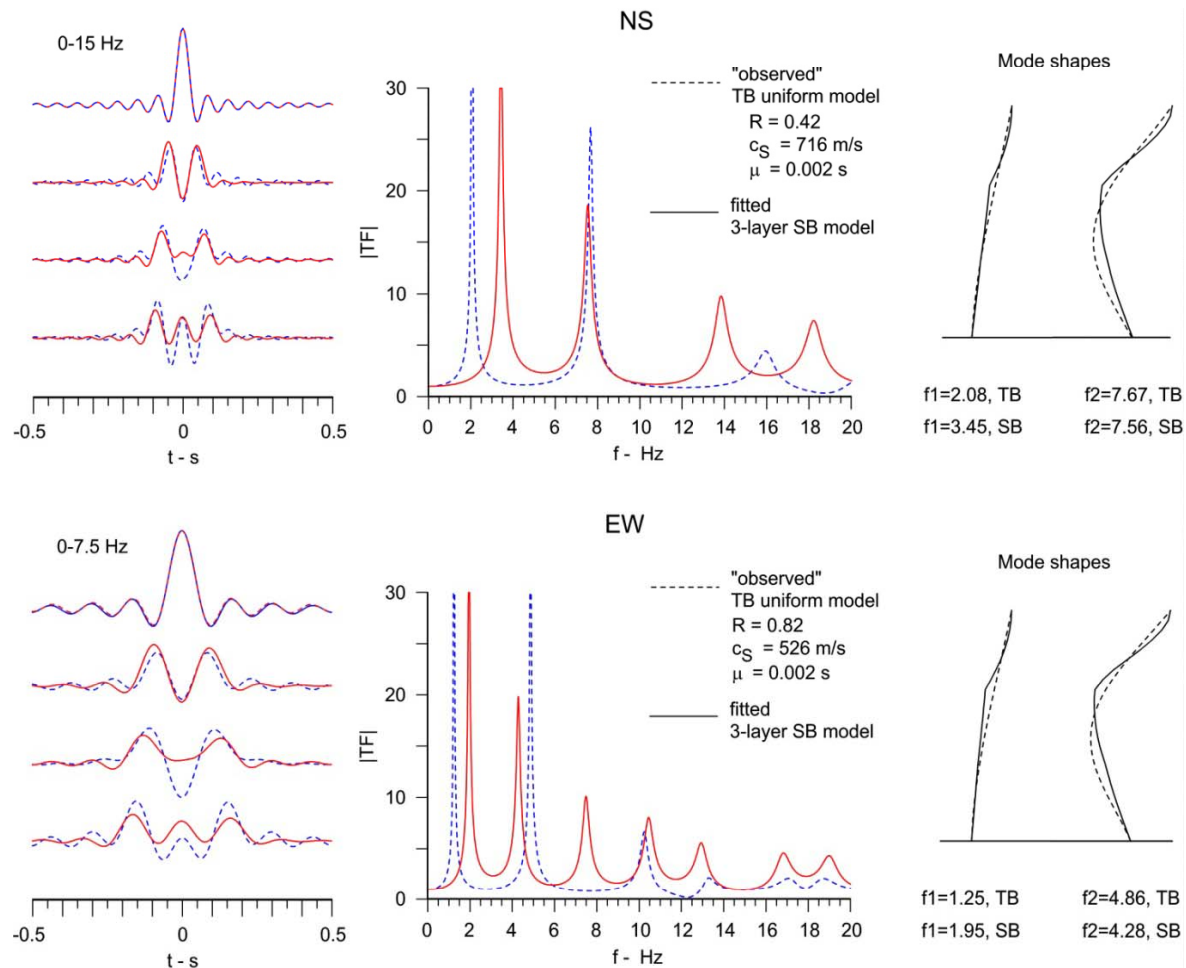
- Timoshenko beam model of Millikan library: superposition of IRFs;
- Why estimate is not sensitive to SSI?
- What velocity does broad band inversion give?



(Ebrahimian et al., 2013)

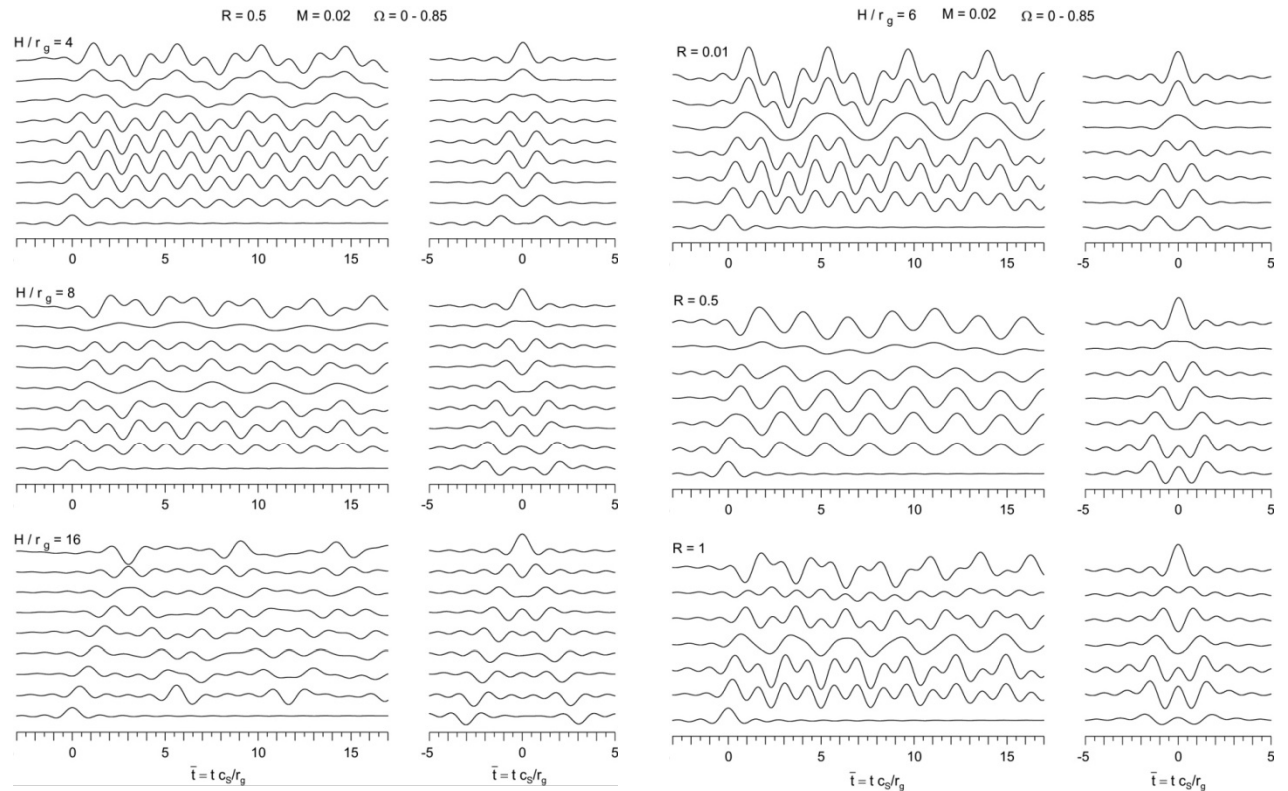
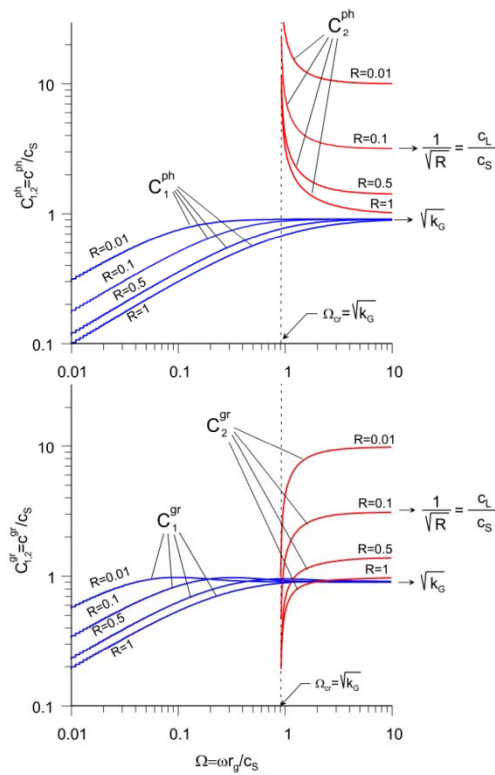
Dispersion due to Bending

- 3-layer shear beam fit in Timoshenko beam response: artifacts due to ignoring dispersion.



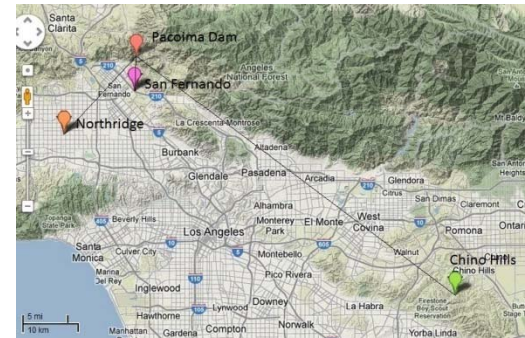
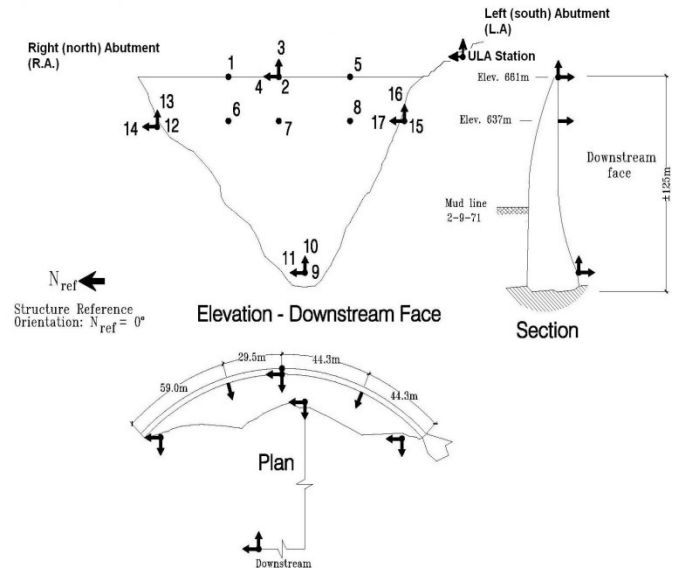
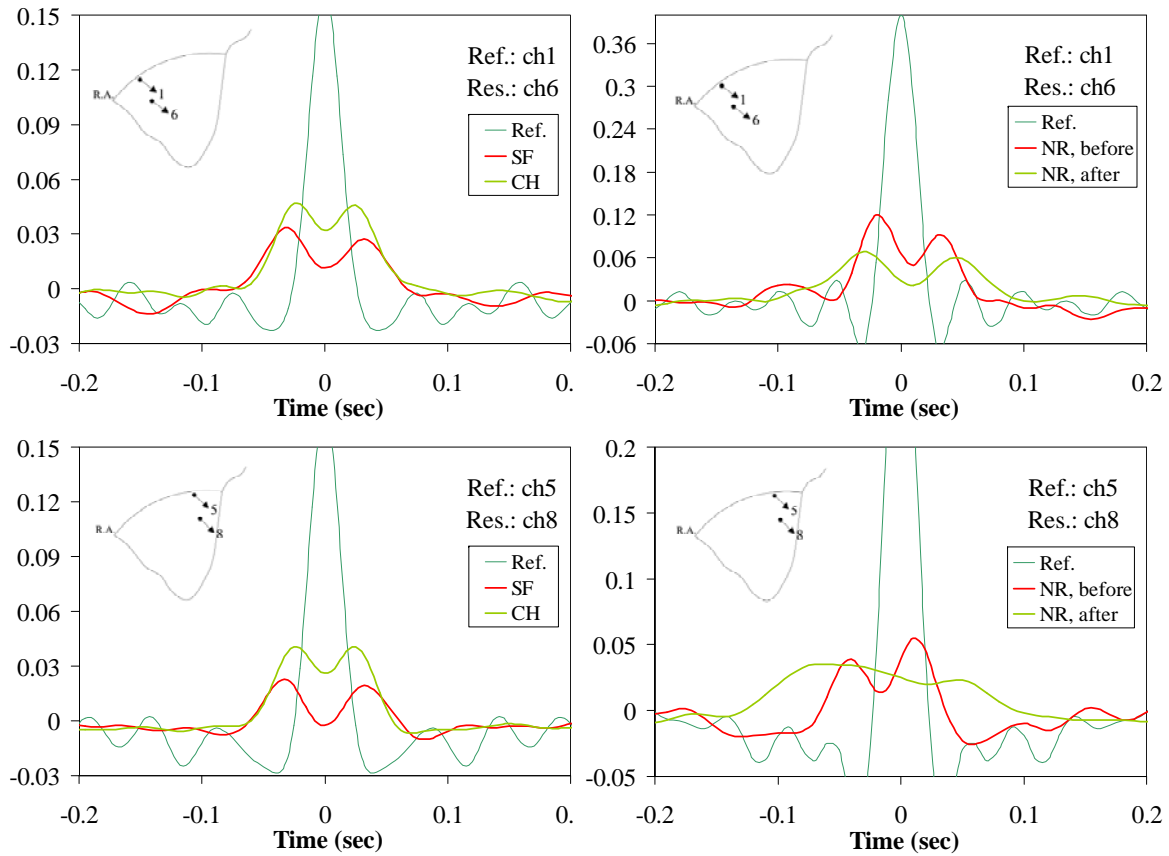
(Ebrahimian et al., 2013)

More Timoshenko Beam IRFs



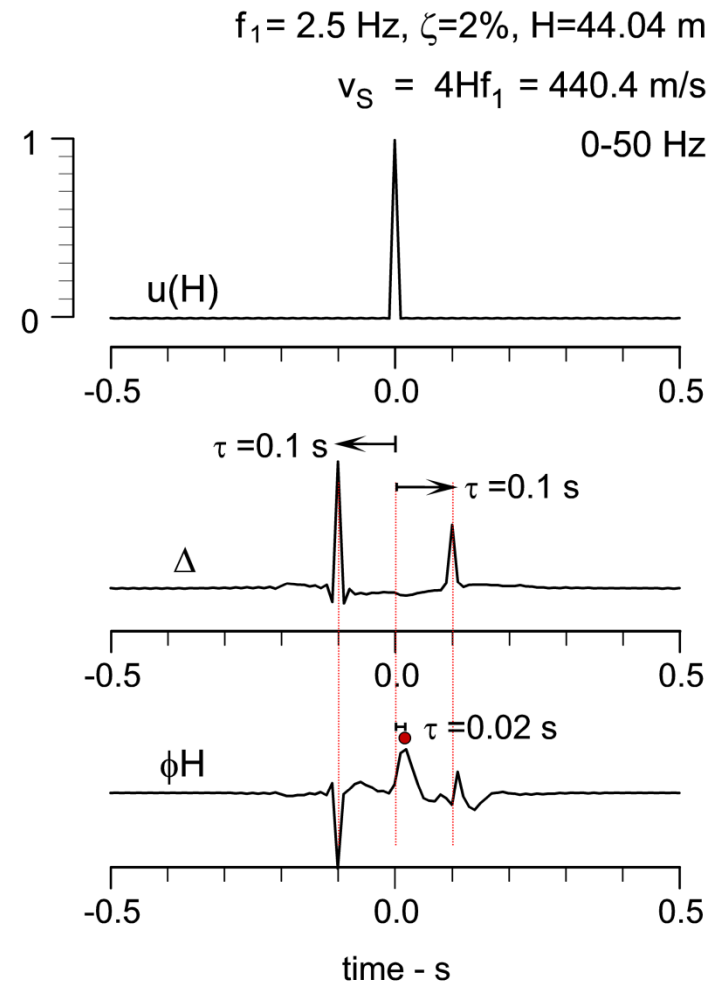
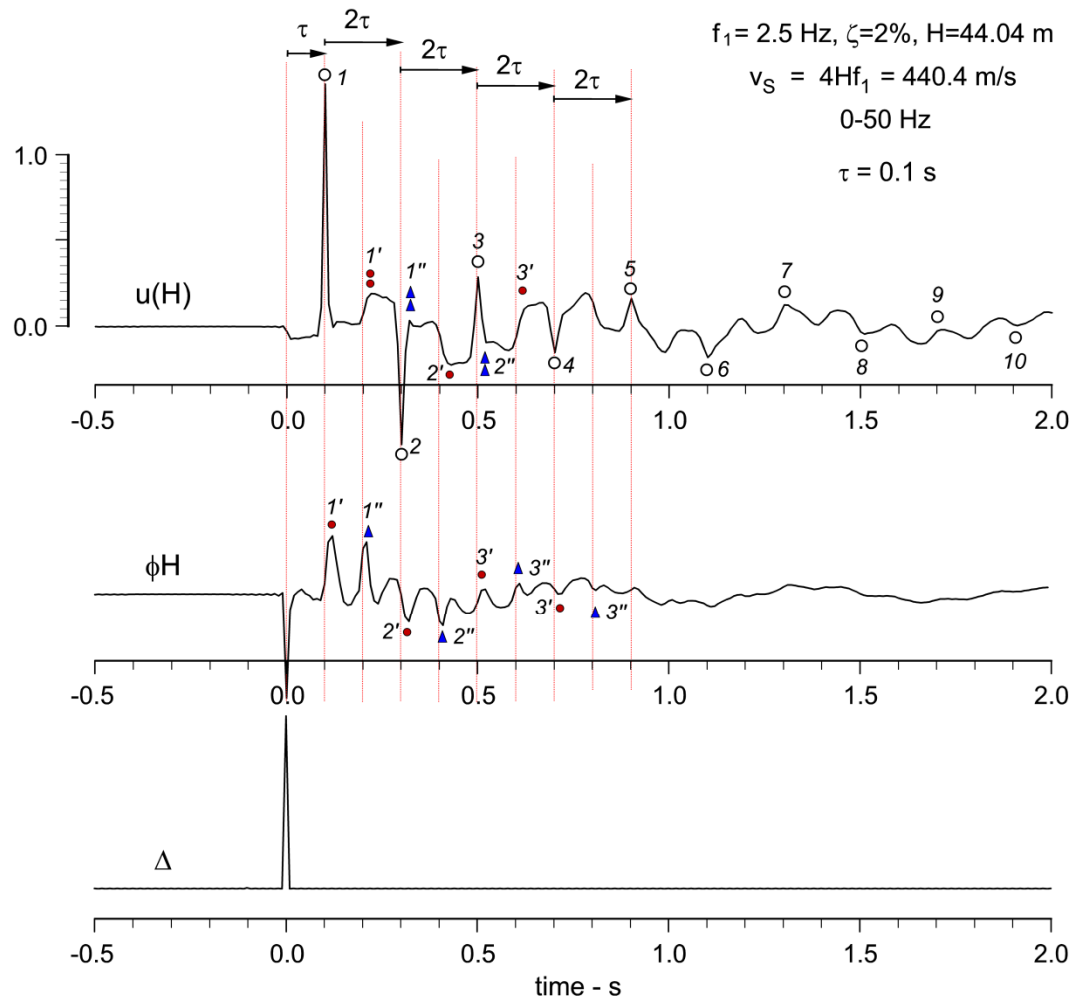
(Ebrahimián and Todorovska, 2013)

Pacoima Dam-Concrete Arch Dam

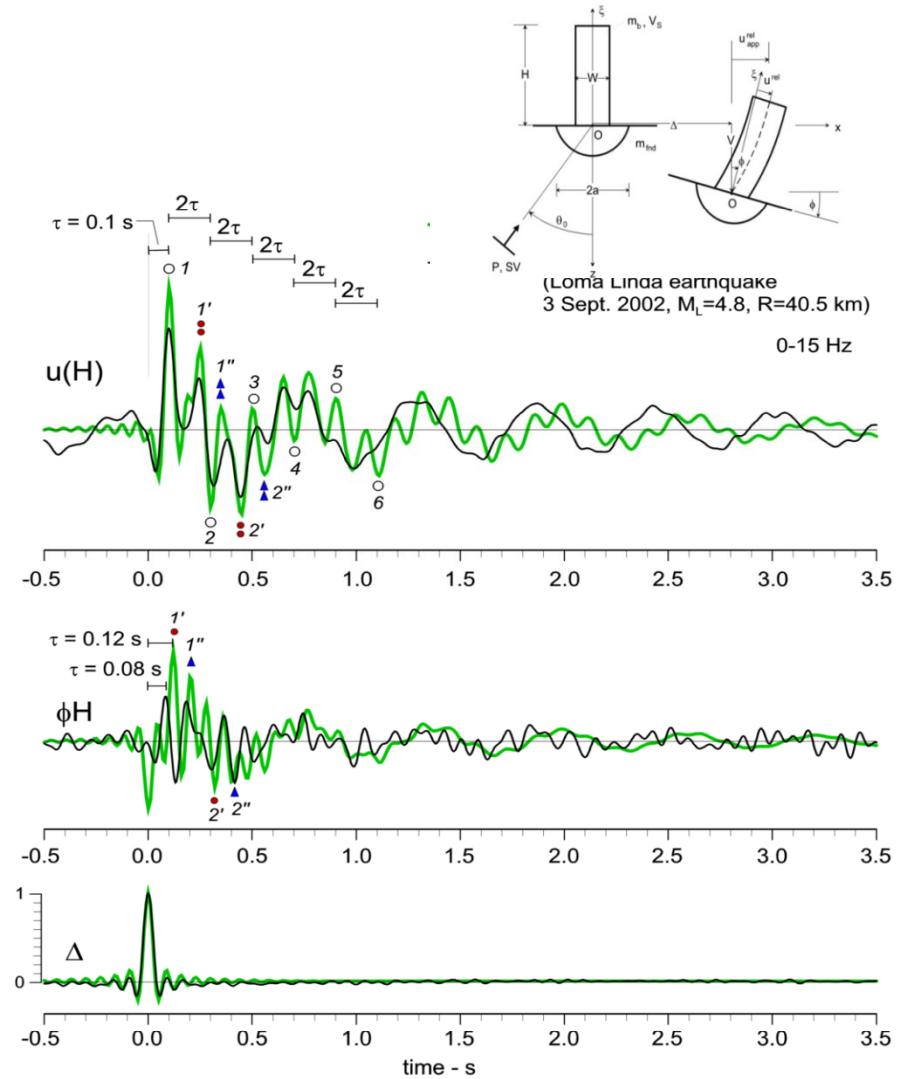
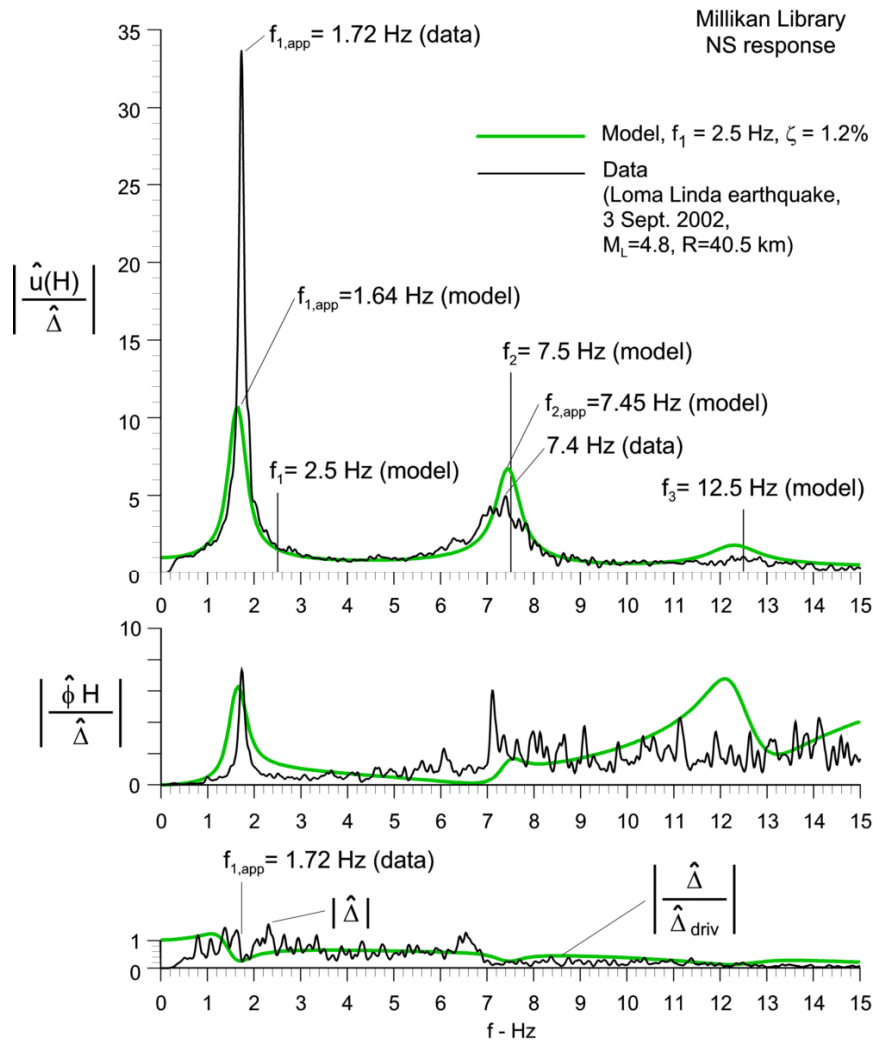


M. Alembagheri et al., 2013

Impulse Responses of SSI Model of Millikan



Cause of Millikan Frequency Wondering – Solved!



Todorovska, BSSA 2009b

What cause Wondering of Millikan Frequency

$$\frac{1}{f_{1,sys}^2} \approx \frac{1}{f_H^2} + \frac{1}{f_R^2} + \frac{1}{f_1^2}$$

$$\frac{1}{f_{1,app}^2} = \frac{1}{f_1^2} + \frac{1}{f_R^2}$$

Rotation angle - milli radians

0.5 - 25 Hz

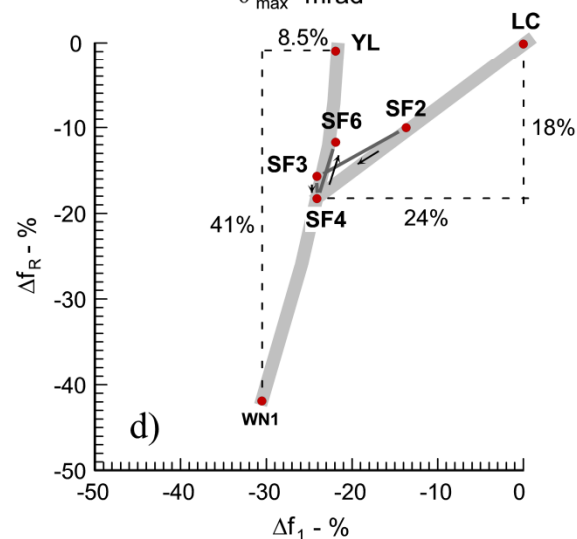
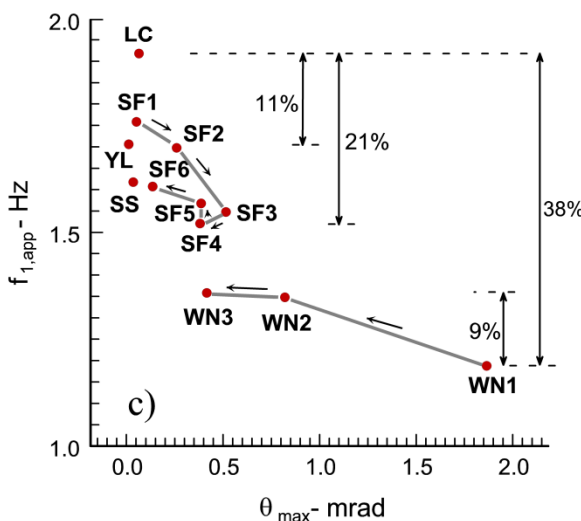
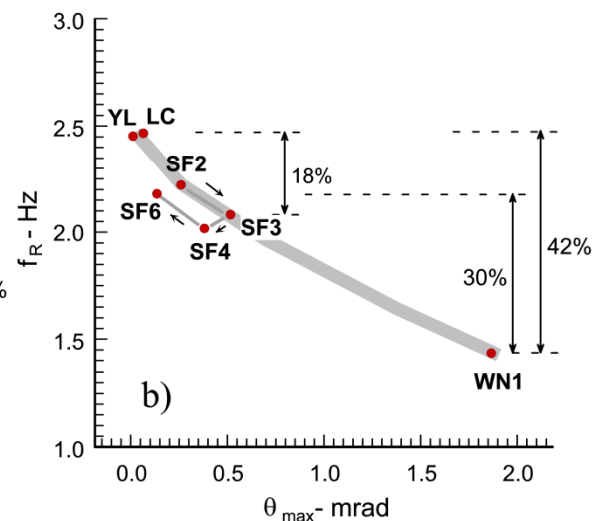
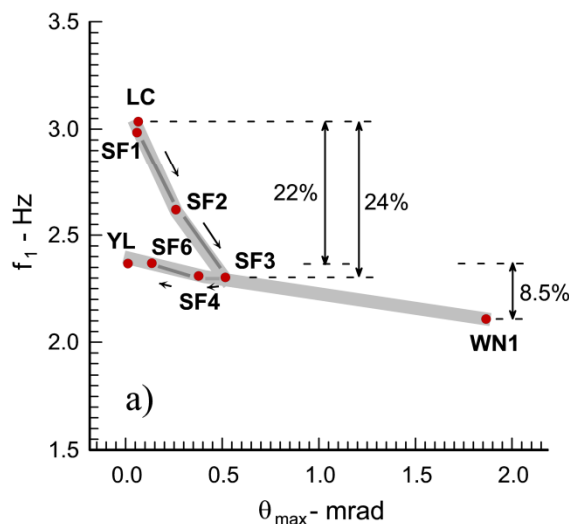
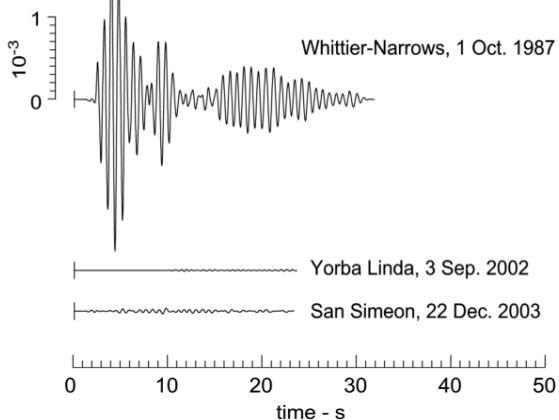
Lytle Creek, 12 Sep. 1970

San Fernando, 9 Feb. 1971

Whittier-Narrows, 1 Oct. 1987

Yorba Linda, 3 Sep. 2002

San Simeon, 22 Dec. 2003



Todorovska, BSSA 2009b

Conclusions

- The wave method is promising.
- It is robust, not sensitive to SSI effects, sensitive to damage.
- May be appropriate for many buildings, within carefully chosen frequency bands, specific for the building.

Publications

- Todorovska MI, Rahmani M (2013). System identification of buildings by wave travel time analysis and layered shear beam models - spatial resolution and accuracy, *Struct. Control Health Monit.*, DOI: 10.1002/stc.1484, preview published online 6 March 2012, in press.
- Rahmani M, Todorovska MI (2013). 1D system identification of buildings from earthquake response by seismic interferometry with waveform inversion of impulse responses – method and application to Millikan Library, *Soil Dyn. and Earthqu. Engrg*, Jose Roësset Special Issue, E. Kausel and J. E. Luco, Guest Editors, 47, 157-174, DOI: 10.1016/j.soildyn.2012.09.014.
- Rahmani M, Todorovska MI (2013). 1D system identification of a 54-story steel frame building by seismic interferometry, *Earthquake Eng. and Struct. Dynamics*, conditionally accepted for publication.
- Rahmani M, Todorovska MI (2013). Structural health monitoring of a 54-story steel frame building - wave and vibrational characteristics during five earthquakes, *Earthquake Spectra*, conditionally accepted for publication.
- Rahmani M, Dehaghani ME, Todorovska MI. (2012). Comparative earthquake damage detection in a full scale 12-story RC building using wave travel time, time-frequency and novelties analyses, in preparation
- Ebrahimian M, Todorovska MI (2013). Wave propagation in a Timoshenko beam building model, *J. Eng. Mech.*, ASCE, submitted for publication.
- Alembagheri M, Todorovska MI, Trifunac MD, Ghaemian M (2013). Structural system identification and health monitoring of a concrete arch dam using strong motion records, in preparation.

Publications

- Todorovska MI (2009). Seismic interferometry of a soil-structure interaction model with coupled horizontal and rocking response, *Bull. Seism. Soc. Am.*, 99(2A), 611-625, doi: 10.1785/0120080191.
- Todorovska MI (2009). Soil-structure system identification of Millikan Library North-South response during four earthquakes (1970-2002): what caused the observed wandering of the system frequencies?, *Bull. Seism. Soc. Am.*, 99(2A), 626-635, doi: 10.1785/0120080333.
- Todorovska MI, Trifunac MD (2008). Earthquake damage detection in the Imperial County Services Building III: analysis of wave travel times via impulse response functions, *Soil Dynamics and Earthquake Engrg*, 28(5), 387–404, doi:10.1016/j.soildyn.2007.07.001.
- Todorovska MI, Trifunac MD (2008). Impulse response analysis of the Van Nuys 7-story hotel during 11 earthquakes and earthquake damage detection, *Structural Control and Health Monitoring*, 15(1), 90-116; DOI: 10.1002/stc.208.
- Trifunac MD, Todorovska MI, Manić MI, Bulajić BĐ (2010). Variability of the fixed-base and soil-structure system frequencies of a building – the case of Borik-2 building, *Structural Control and Health Monitoring*, 17(2), 2010, 120–151, published online 2008, DOI: 10.1002/stc.277.
- Ivanovic SS, Trifunac MD, Todorovska MI (2001). On identification of damage in structures via wave travel times, in M. Erdik, M. Celebi, V. Mihailov, and N. Apaydin (Eds.), *Proc. NATO Advanced Research Workshop on Strong-Motion Instrumentation for Civil Engineering Structures*, June 2-5, 1999, Istanbul, Turkey, Kluwer Academic Publishers, 2001, pp. 21.

Publications

- Ivanovic SS, Trifunac MD, Todorovska MI (2000). Ambient vibration tests of structures - a review, Bull. Indian Soc. Earthquake Tech., 37(4), 165-197.
- Trifunac MD, Todorovska MI, Hao TY (2001). Full-scale experimental studies of soil-structure interaction - a review, Proc. 2nd U.S.-Japan Workshop on Soil-Structure Interaction, March 6-8, 2001, Tsukuba City, Japan, pp. 52.

Some publications downloadable from:

Project web site:

www.usc.edu/dept/civil_eng/Earthquake_eng/Earthquake_damage_detection_NSF_2008/

Strong Motion Research Group web site:

www.usc.edu/dept/civil_eng/Earthquake_eng/

Acknowledgements

- Some of this work was supported by a grant from the U.S. National Science Foundation (CMMI-0800399).
- Strong motion data for Los Angeles 54-story building was obtained from Engineering Centre for Strong Motion Data (www.strongmotioncenter.org/); for Millikan Library, from the U.S. Geological Survey Strong Motion Instrumentation Project (<http://nsmp.wr.usgs.gov/>); and for Sherman Oaks 12-story building, from M. Trifunac.

A photograph of a city skyline, likely Los Angeles, with several prominent skyscrapers. In the foreground, there are buildings with red-tiled roofs. The text "Thank You!" is overlaid in the center of the image.

Thank You!