Changes in effective stress during the 2003-2004 Ubaye seismic swarm, France

Running title: Changes in effective stress during the Ubaye swarm

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Abstract

We study changes in effective stress (normal stress minus pore pressure) that occurred in the French Alps during the 2003-2004 Ubaye earthquake swarm. Two complementary datasets are used. Firstly, a set of 974 relocated events allows us to finely characterize the shape of the seismogenic area and the spatial migration of seismicity during the crisis. Relocations are performed by a double-difference algorithm. We compute difference in travel-times at stations both from absolute picking times, and from cross-correlation delays of multiplets. The resulting catalogue reveals a swarm alignment along a single planar structure striking N130°E, and dipping 80°W. This relocated activity displays migration properties consistent with a triggering by a diffusive fluid overpressure front. This observation argues in favor of a deep-seated fluid circulation, responsible for a significant part of the seismic activity in Ubaye. Secondly, we analyze time series of earthquake detections at a single seismological station, located just above the swarm. This time series forms a dense chronicle of +16,000 events. We use it to estimate the history of effective stress changes during this sequence. For this purpose, we model the rate of events by a stochastic Epidemic-Type Aftershock Sequence model (ETAS) with a non-stationary background seismic rate $\lambda_0(t)$. This background rate is estimated in discrete time windows. Windows lengths are optimally determined according to a new change-point method, based on the inter-event times distribution. We propose that background events are directly triggered by a transient fluid circulation at depth. Then, using rate-and-state constitutive friction laws, we estimate changes in effective stress for the observed rate of background events. We assume that changes in effective stress occurred under constant shear stressing rate conditions. We
finally obtain a maximum change in effective stress close to -8 MPa, which corresponds
to a maximum fluid overpressure of about 8 MPa under constant normal stress
conditions. This estimate is in good agreement with values obtained from numerical
modeling of fluid flow at depth, or with direct measurements reported from fluid
injection experiments.

**Keywords:** *Ubaye seismic swarm, Seismicity rate, Pore-pressure changes, Declustering,
Rate-and-State laws, Earthquake relocations.*
1. Introduction

Seismic swarms are dense and intensive episodes of microseismic activity. Generally, they do not consist in a simple succession of many larger shocks and their aftershocks. They rather exhibit a complex behavior, compared to typical seismic crisis, initiating with an increasing number of small events and ending after a variable term. The study of these phenomena is thus very challenging, as they question the very detailed behavior of seismicity. Seismic swarms also reflect transient changes of in-situ physical properties in the upper crust. Consequently, the analysis of swarm episodes is of importance, as it may potentially bear crucial information on the general earthquake preparation process at a human time scale.

This study focuses on the Ubaye valley area (Alpes-de-Haute-Provence, France; see Figure 1), which is the most seismically active region in the French western Alps [Thouvenot and Fréchet, 2006]. Seismic activity in this area is characterized both by moderate earthquakes (e.g. the historical M 5.5 Saint-Paul-sur-Ubaye earthquake in 1959) and episodic swarms. Using a temporary seismological network, Fréchet and Pavoni (1979) conducted the first study of a swarm in Ubaye. Subsequently, Guyoton et al. (1990) described another swarm episode in 1989, soon after the installation of the permanent seismological network Sismalp (http://sismalp.obs.ujf-grenoble.fr/). They located it 5 km NE of Saint-Paul. In the present study, we analyze the most recent swarm episode in this area, which started in January 2003 close to La Condamine-Châtelard, see Figure 1. This swarm consisted in a period of continuous seismic activity that lasted about two years. This sequence thus represents a new opportunity to improve our knowledge on the mechanics of swarm generation, and to study active faults in the Ubaye area.
In the literature, swarm occurrence is commonly related to the circulation of deep-seated fluids along, or in the vicinity of earthquake faults. Aseismic creep can also constitute an alternative trigger mechanism [Lohman and McGuire, 2007]. The close association between fluids and swarm relies either on direct observations of surface fluid flow accompanying the seismic activity (e.g. during the 1965-1967 Matsushiro swarm, Japan [Tsuneishi and Nakamura, 1970]), or on the close association of swarm episodes with areas of important gas outflow (e.g. the western Eger rift, Bohemia, Czech Republic [Weinlich et al., 1999; Hainzl and Ogata, 2005; Bräuer et al., 2009], the central Apennines, Italy [Chiodini et al., 2000]). Frequently, swarms occur in regions of geothermal or volcanic activity (e.g. swarms in the Long Valley caldera, California [Savage et al., 1984; Hill and Prejean, 2005]; at the Yellowstone volcanic field, western U.S. [Farrell et al., 2009]; or east of the Izu Peninsula, Japan [Ukawa and Tsukahara, 1996]). These peculiar settings suggest that stress perturbations associated with fluid overpressure at depth is a plausible mechanism for the driving of seismic swarms [e.g. Yamashita, 1999; Hainzl and Ogata, 2005].

During the Ubaye swarm, no fluid outflow was observed at the surface. However, the location of several hot springs located few tens of kilometers northwards and southwards from the study area reveals that current fluid circulations take place within the bedrock (Figure 1). According to these regional settings and to previous studies of swarms worldwide, we show here that a triggering of the Ubaye swarm by fluid overpressure is a very likely hypothesis. This hypothesis provides a coherent framework to explain the seismological observations. In section 2, we present the dataset elaborated for the Ubaye seismic swarm. We describe the spatio-temporal evolution of the relocated dataset in section 3, and present the characteristics of a diffusive migration pattern. In section 4 we model the rate of events and introduce a new
objective statistical procedure to estimate the non-stationary background-forcing rate in
discrete time-windows. In section 5 we estimate the amplitude of the effective stress changes
leading to the observed earthquake rate, deduced from the rate-and-state constitutive laws
[Dieterich, 1994]. We finally discuss our results in section 6.

2. Data

This study relies on the analysis of two complementary seismological datasets. The first one is
a relocated catalogue of micro-earthquakes, with magnitudes ranging between -0.3 and 2.7.
This dataset was originally located by the Sismalp seismological network [Thouvenot et al.,
1990]. The second dataset consists in a report of (hand-picked) event detections at JAUF, the
closest seismological station (Figure 1). This station was located right above the earthquake
swarm and allowed the detection of a large number of small events. This report constitutes a
chronicle of 16,147 detections with $M_L$ estimates ranging from -1.3 to 2.7 [Jenatton et al.,
2007].

2.1 Relocated catalogue

Less than 10% of the 16,147 microearthquakes that occurred in Ubaye during years 2003 and
2004 were detected by a sufficient number of stations to be located. We have reprocessed the
catalogue of earthquake relocations originally presented in Jenatton et al. (2007). For this
purpose, we have included phase picks at 5 supplementary stations (deployed in the area from
September 2003 to December 2004), and improved its accuracy by using travel-times
estimated from the cross-correlation of similar events (multiplets). All manual phase picks
and cross-correlation delays were merged in a double-difference algorithm using the
HYPODD software [Waldhauser and Ellsworth, 2000]. The main advantage of this relocation technique is that it allows the whole set of events to be located in a single operation. It also preserves the high accuracy of relative relocations within the multiplet. We obtain one single large multiplet of 799 events with a mean coherence greater than or equal to 90% on at least 3 stations. High-precision travel time delay measurements were performed by pair-wise cross-correlation of the first 1.28 second of seismic waveforms in the spectral domain.

The computation of relocation uncertainties by a Monte-Carlo analysis led to an average location error of 100 m. The relocated catalogue thus consists in 1058 events that occurred between years 1989 and 2004. Among these, 974 earthquakes occurred during the crisis in 2003-2004 and are displayed on Figure 2. We present a map view (Figure 2, top) and a cross-section (Figure 2, bottom) of the swarm, with events coordinates projected along a plane trend of azimuth N130°E and dip 80°W.

2.2 Detection time series at station JAUF

The permanent seismological station JAUF recorded 16,147 events that could be hand-picked. Differences in P- and S-waves arrival times were analyzed to select only events occurring within the swarm area. Unfortunately, most of them could not be located as they triggered too few or no other stations. Event magnitudes were estimated from peak amplitudes of seismograms and distances, according to a calibration based on located events of the sequence [Jenatton et al., 2007]. Magnitudes of this time-series span from -1.3 up to 2.7, leading to a total energy release equivalent to that of a magnitude 4 event. These authors also showed that magnitudes are consistent with a Gutenberg-Richter law [Gutenberg and Richter, 1956] with a b-value of 1.2 ± 0.03. The time-series contains 3546 events with magnitude greater than the
completeness threshold $M_L=0.2$. This threshold has been determined by visual inspection, based on the validity of Gutenberg-Richter law for higher magnitudes. We here use origin times at JAUF to calculate the swarm seismicity rate (Figure 3, grey line). For the sake of comparison, and in order to verify that both datasets present a similar temporal evolution, we displayed the rate of the 974 relocated earthquakes on Figure 3 (black curve).

3. Spatial evolution of the swarm

This section focuses on two main features of the relocated catalogue. First, it reveals a precise image of the fault zone geometry (section 3-1) and second, it suggests a peculiar temporal evolution of the seismic activity along this structure (section 3-2).

3-1. Geometry of the seismogenic structure

In map view (see Figure 2a), the Ubaye swarm appears as an elongated narrow cloud of micro-earthquakes. The seismicity is mainly located within a narrow 8 km-long and 1 km wide band. At depth, all events are located on a quasi-vertical structure. This, however, does not guarantee that the seismic activity occurred on a single fault. Such a cloud may as well be defined, for example, by events distributed along a dense network of numerous short faults with different orientations. We now aim at determining the fault zone structure associated with this swarm. We assume that micro-earthquakes are not randomly distributed within a volume but rather occur along planar faults/fractures. We then search for the preferential plane orientations, by a simple geometrical analysis of hypocenters spatial distribution.

We use the 3-point method (Fehler et al. 1987) to detect preferential planar alignments of hypocenters. This method relies on the distribution of plane orientations (strike, dip) obtained for each possible set of 3 events in the relocated catalogue (i.e. among 974 events). As the
orientation of planes defined by close events will have larger uncertainties because of locations errors, we restricted our analysis to events separated by at least 100 m. We also used a maximum separation distance of 10 km in order to remove events located far from the main swarm cluster. We remove the influence of the cluster elongated shape by normalizing the distribution of plane orientation with respect to 100 random location sets within a volume of comparable dimensions. We consider as significant every orientation occurring more than 3.62 standard deviations above the corresponding level obtained with the random datasets. This corresponds to a ratio of 1 chance in 10,000 that this preferential alignment be indicated by random variations around the mean number of similar orientations in the random dataset [Fehler et al., 1987]. The preferred plane then corresponds to the most frequent orientation above this threshold. This method also allows linking each seismic event with its preferred plane orientation, interpreted as the fracture plane on which this event most likely fell. For this purpose, we count how many times each event contributes to a set of 3 events aligned along a particular orientation. Events with the largest number of counts are those that occur along this particular plane.

Orientations of preferential planes are presented on Figure 4. Polar histograms display the number of relocated earthquakes associated with each strike (see Figure 4, left) and dip (see Figure 4, right) orientation. They show a clear prominence for planes striking N130°E ±5° and dipping 80°±5° to the west, according to the convention used in Aki and Richards (1980). This range of orientations is in good agreement with the general trend of relocated seismicity, and is also close to the N145°E direction obtained by Jenatton et al. (2007) from the set of original locations. Interestingly, we find no preferential orientation striking perpendicular to the cloud elongation direction, dismissing any possible interplay of conjugate faults during this episode.
We also notice that no temporal pattern is discernible in the evolution of the preferred orientation. Rather, the whole range of orientations represented on Figure 4 is associated with events from the initiation to the ending of the swarm episode. All these observations clearly argue in favor of a single seismogenic discontinuity at depth striking NW-SE and dipping 80°W.

3-2. Migration of the swarm activity

The most striking feature of the Ubaye crisis is certainly its temporal evolution. This is highlighted on Figure 2 by a color-scaling of hypocenters depending on their date of occurrence. Relocated events exhibit a quasi-unilateral migration of micro-earthquakes from the NW to the SE, within a band located between 3 and 8 km at depth.

We here discuss the diffusive character of the Ubaye swarm migration. For this purpose, we measure the progressive spreading of the main swarm cluster during the sequence. For each time \( t \), we compute the average distance \( R \) between all events that occurred at time \( t_i < t \) and the first earthquake of the sequence (Figure 5). Several previous studies have already documented the evolution of this distance \( R \) for earthquake sequences [Noir et al., 1997; Marsan et al., 1999; Marsan et al., 2000; Helmstetter et al., 2003b; Huc and Main, 2003]. For various global or regional earthquake catalogues, these authors found that \( R \) increases slowly with time, according to \( R(t) \propto t^H \) with \( H \) close to 0.1 or 0.2. Helmstetter et al. (2003b) also noticed that this \( H \) value may vary from one individual sequence to another, and depends on the methods used to measure \( R \). Such a relationship reveals that if a stress diffusion mechanism takes place within the Earth’s crust, it occurs slowly, and may be very weak [Marsan et al., 2000; Huc and Main, 2003].
Inspection of Figure 5 reveals that the seismic activity in Ubaye started to spread about 30 days after the swarm initiation. The average distance $R$ increases up to the end of 2004, mainly along the preferential plane orientation, see also Figure 2. Interestingly, the spreading of the Ubaye sequence exhibits a quasi-diffusive character, characterized by a diffusion exponent value $H=0.41\pm0.06$. Thus, not only did this swarm migrate very clearly, but also this migration took place according to a process closer to a normal diffusion (i.e. with $H=0.5$) than to the sub-diffusive process expected for typical earthquake sequences.

Normal diffusion processes characterize particle motions in physical systems close to equilibrium [e.g. Vlahos et al., 2008]. Within the Earth’s crust, such behavior may either be related to a viscous relaxation mechanism, or to a pore-pressure balancing mechanism induced by fluid flow in a relatively homogeneous medium. In Ubaye, as the depth of relocated hypocenters lies within the upper, elastic, brittle part of the crust, we rather support the latter mechanism, i.e. fluids. We argue that a deep increase in pore-pressure by fluid flow is the most likely mechanism, and could unclamp favorably oriented faults/fractures by decreasing the effective normal stress. In other words, we claim that seismicity in Ubaye is the result of a non-stationary forcing by fluids, a well-known likely mechanism for the generation of earthquakes [e.g. Nur and Booker, 1972].

For several years hydraulic fracturing studies have been focusing on the relationship between such temporal spreading of the micro-seismicity and physical properties of the fractured medium, e.g. permeability [see Shapiro et al. 1997, Shapiro et al., 2006b for instance]. Although their approach appears very attractive to characterize the fracturing process taking place during the swarm, these physical models require boundary conditions, or experimental settings, quite unlikely for natural seismic swarms. For instance, a constant fluid injection rate
may not be adequate for the Ubaye swarm, in reference with the size of the seismogenic volume and the long duration (2 years) of this episode. Nonetheless, the planar shape of the hypocenters cloud reveals that a fault zone with a higher permeability than the surrounding host rock was preexisting in the basement. When fluids invaded the medium during the swarm episode, this zone thus provided a natural channel for fluid circulation, and consequently, for earthquake occurrence. Recently, Shapiro and Dinske (2009) proposed a generalized model for microearthquakes migration that involves a nonlinear diffusion of fluids. According to their results, $H \neq 0.5$ may either follow from a pressure-dependent diffusivity parameter, or from a time varying fluid injection rate. These two mechanisms may have likely controlled the migration process observed in Ubaye.

4. Non-stationary forcing of seismicity by fluids

The driving of seismic swarms by fluids has been reported as a likely mechanism in numerous studies [e.g. Hill et al., 1977; Yamashita, 1999; Horálek and Fischer, 2008], although surface evidences of fluid flow are scarce [e.g. Tsuneishi and Nakamura, 1970]. Indeed in Ubaye no fluid outflow was observed during the sequence [Jenatton et al., 2007]. In the following, we hypothesize that a transient fluid circulation at depth led to a significant part of the swarm activity, the remaining part resulting from self-sustained cascades of aftershocks [Hainzl and Ogata, 2005]. We have developed a new methodology in order to retrieve the rate of microearthquakes induced by a non-stationary background forcing in discrete time-windows. We later associate this forcing with effective stress changes at depth. The procedure that we describe in the following aims at modeling the seismicity rate recorded at station JAUF as a stochastic process.
The earthquake rate detected at JAUF (Figure 3) cannot be consistent with a typical mainshock-aftershock sequence. In Ubaye, we could not model satisfactorily the sequence as a succession of aftershock sequences obeying the Omori law superimposed on a Poissonian background rate. Such a behavior would lead to a temporal seismic response similar to that modeled with an Epidemic-Type Aftershock Sequence model (ETAS) with a constant background seismicity term [Kagan and Knopoff, 1987; Ogata, 1988]. Conversely, suitable modeling of this sequence requires the involvement of a non-stationary background rate. Consequently, we model the earthquake timeseries in Ubaye by a time-dependent Poisson process. The probability to observe \( k \) seismic events during a time interval \( dt \) is given by

\[
P(k \mid \Lambda) = e^{-\Lambda} \frac{\Lambda^k}{k!}
\]

where

\[
\Lambda = \int_{t-dt} \hat{\Lambda}(s) \, ds
\]

The rate \( \hat{\lambda}(t) \) consists in the superposition of two distinct contributions: a non-stationary background term \( \hat{\lambda}_0(t) \) and an epidemic term \( \hat{\lambda}_e(t) \). This last term explicitly stands for the probability that each event of the sequence generates its own secondary aftershocks [Kagan and Knopoff, 1987; Ogata, 1988],

\[
\hat{\lambda}(t) = \hat{\lambda}_0(t) + \hat{\lambda}_e(t) \tag{2}
\]

with

\[
\hat{\lambda}_e(t) = \sum_{i_{i < t}} \left( \frac{A e^{\alpha(M_i - M_c)}}{(t - t_i + c)^p} \right)
\]

In this expression, \( t_i \) and \( M_i \) are, respectively the occurrence time and magnitude of an earthquake \( i \), whose magnitude is greater than, or equal to the magnitude of completeness \( M_c \). \( A, \alpha, c \) and \( p \) are epidemic parameters. This formulation has been used in previous studies to model seismicity rates and to retrieve the evolution of the non-stationary rate. Related studies
by Hainzl and Ogata (2005) applied such modeling to the Vogtland-West Bohemia swarm, and Matsu’ura and Karakama (2005) to the Matsushiro swarm, Japan. Both studies improved significantly the modeling of seismicity rates with respect to an ETAS model with a constant background term $\lambda_0(t)$. In addition, Hainzl and Kraft (2006) related this non-stationary forcing $\lambda_0(t)$ to changes in pore pressure $P$ according to the formula

$$\lambda_0(t) = \lambda_{00} + K \frac{\partial P}{\partial t}$$

(4)

where $\lambda_{00}$ is a constant background rate and $K$ is a proportionality constant. This link was recently confirmed by Llenos et al. (2009), who showed that, during swarm episodes, aseismic forcing (e.g. fluids or creep) influences preferentially the background activity rate rather than other epidemic parameters of the ETAS model.

Model estimation is here performed in two steps. Firstly, we determine an optimal set of discrete time windows and estimate their respective background rate $\lambda_0(t)$ for each time window, based on the distribution of earthquake inter-event times. Secondly, we obtain the 4 epidemic parameters ($A$, $\alpha$, $c$ and $p$) that best explain the observed seismicity rate, using a maximum likelihood procedure.

4-1 Discretization of $\lambda_0(t)$

Objective discretization of the function $\lambda_0(t)$ is an important concern. Indeed, there exists a tradeoff between a choice of long time windows - that preserve the epidemic character of the model but prevent to retrieve rapid changes of the forcing rate, - and a choice of short time windows that tend to annihilate the epidemic contribution $\lambda_e(t)$. In the first situation, the model converges towards the original ETAS formulation [Ogata, 1988] as the length of time windows tends towards the length of the sequence. In the last situation, the model converges towards
\( \lambda(t) = \lambda_0(t) \) as the length of time windows tends towards 0. In both cases, we may miss crucial information concerning the interplay between a time-dependent external forcing \( \lambda_0(t) \) and the self-triggering \( \lambda_e(t) \) of the seismic activity.

To overcome this difficulty, we here propose an objective procedure that optimizes the discretization of the time axis into separate intervals for the estimation of \( \lambda_0(t) \). We aim at finding successive non-overlapping time windows during which we consider the background external forcing \( \lambda_0(t) \) as constant. The estimation of \( \lambda_0(t) \) for each time window is based on the method of Hainzl et al. (2006) that builds upon the fact that the probability density function of inter-event times can be expressed as

\[
f(\delta t) = C e^{-a\delta t} (\delta t)^{-b}
\]

with

\[
C = \frac{a^{1-b}}{\Gamma(1-b)}
\]

where \( \delta t \) are the inter-event times, \( C \) is a normalization constant and \( \Gamma \) is the gamma function. Hainzl et al. (2006) showed that \( a \) and \( b \) can be estimated by

\[
a = \frac{\overline{\delta t}}{\sigma_{\delta t}^2}
\]

\[
b = 1 - (\overline{\delta t}a) = 1 - \frac{\overline{\delta t}^2}{\sigma_{\delta t}^2}
\]

We note that this approach relies on the hypothesis of independent inter-event times, and that taking into account their interdependence may affect our results. Following these authors, we
thus estimate the background rate as $\lambda_0(t)=a$. To evaluate the quality of the model $f(\tau)$, we divide the $\hat{\delta}$-axis into $N$ bins $[0, \hat{\delta}_1], \ldots \hat{\delta}_i, \ldots, \hat{\delta}_N$ such that $\{\hat{\delta}_1, \hat{\delta}_2, \ldots, \hat{\delta}_N\}$ are the observed inter-event times ranked in ascending order. For a given bin $[\hat{\delta}_{i-1}, \hat{\delta}_i]$ we observe exactly one occurrence ($\hat{\delta}_i$) of the inter-event times, while the model predicts

$$\mu_i = N \int_{\hat{\delta}_{i-1}}^{\hat{\delta}_i} d\hat{\delta} f(\hat{\delta})$$  \hspace{1cm} (9)$$

occurrences, on average. We thus define the likelihood $\ell = \prod_{i=1}^{N} e^{-\mu_i} \mu_i$ of the model, or equivalently

$$L = -\log(\ell) = \sum_{i=1}^{N} \mu_i - \ln(\mu_i)$$  \hspace{1cm} (10)$$

Following the gamma law of Hainzl et al. (2006), equations (9) and (10) can be written as

$$\mu_i = N \cdot P(1-b,a,\hat{\delta}_i) - N \cdot P(1-b,a,\hat{\delta}_{i-1})$$  \hspace{1cm} (11)$$

$$L = -\log(\ell) = N \cdot P(1-b,a,\hat{\delta}_N) - \sum_{i=1}^{N} \ln(\mu_i)$$  \hspace{1cm} (12)$$

where $P$ is the lower incomplete gamma function.

In order to optimize the selection of time windows during which $\lambda_0(t)$ is modeled as constant, we use an objective change-point analysis. The rationale of the method is the following: let consider a time period with $N$ inter-event times $\{\hat{\delta}_1, \hat{\delta}_2, \ldots, \hat{\delta}_N\}$. We want to know if this time period is better characterized by a change in $\lambda_0$ at a time $t$ such that there are $N_1$ inter-event times for the time series prior to $t$ and $N_2$ after $t$ ($N=N_1+N_2$). We thus compare the two hypotheses:
- \( \lambda_0(t) \) does not vary significantly between these two windows, hence a single model \( f(\delta t) \) can well describe the inter-event time distribution for the time period ;

- \( \lambda_0(t) \) varies significantly between these two windows, and we need to define two distinct densities \( f_1 \) and \( f_2 \), one for each window.

In the first case, the log-likelihood is \( L_1 \) as obtained from equation (12). In the second case, we compute \( L_2 \) from equations (9) and (12), but with

\[
f(\delta t) = \frac{N_1}{N_1 + N_2} f_1(\delta t) + \frac{N_2}{N_1 + N_2} f_2(\delta t)
\]

where \( f_1 \) and \( f_2 \) are parameterized independently for each window.

We search for the best time \( t \) (i.e. the change-point) by minimizing \( L_2 \). This change-point is then kept if \( L_2 \) is significantly lower than \( L_1 \). An objective procedure is to use the Bayesian Information Criterion [Davison, 2003]:

\[
BIC = 2L + n \ln(N)
\]

where \( n \) is the number of free parameters in the model (\( n_1 = 2 \) in the first hypothesis of only one density, \( n_2 = 5 \) in the second hypothesis of two densities and a change-point). We keep the change-point if \( \Delta BIC = 2(L_2 - L_1) + (n_2 - n_1) \ln(N) \) is negative, hence \( L_2 - L_1 < -3/2 \ln(N) \).

This procedure starts with the entire window and is iterated until no further change-point is required. For the Ubaye swarm, we obtain a set of 6 discrete time windows for \( \lambda_0(t) \) corresponding to the interval between two successive change-points. Figure 6 displays the fit of empirical inter-event times distributions by gamma distributions from equation 5. These diagrams show a good agreement between all inter-event times and the gamma law. By
estimating $\lambda_0(t)$ for each time interval associated with time windows defined according to this change-point method, we ultimately provide the stair-step estimate of $\lambda_0(t)$, see Figure 7 (dashed line) and Table 1.

**4-2 Epidemic parameters estimate**

We estimate the best set of epidemic parameters $\hat{\theta} = \{A, \alpha, c, p\}$ by a maximum likelihood procedure. We define it as the one that maximizes the following log-likelihood function:

$$L'(\theta) = \sum_k \ln \lambda(t_k; \lambda_0; \theta) - \int_0^T \lambda(t; \lambda_0; \theta) \, dt$$

(15)

where $T$ is the duration of the catalog, and $t_k$ are earthquake occurrence times. We suppose parameters $A$, $\alpha$, $c$ and $p$ to be constant, i.e. we make the hypothesis that the self-triggering process remains the same during the whole swarm sequence. Considering the seismicity rate model given in equations (2) and (3), we note that, for any $\theta$, the log-likelihood value will depend strongly on the shape of $\lambda_0(t)$. As our strategy for the estimation of $\hat{\theta}$ relies on an independent estimate of $\lambda_0(t)$, this procedure guarantees a robust estimation of $\hat{\theta}$.

Again, we use the BIC criterion (equation 14) with $n=4$ (number of epidemic parameters), $L=L'$ and $N=3546$ to check that the ETAS model with a non-stationary rate $\dot{\lambda}_0(t)$ significantly improves the modeling, with respect to the formulation involving only a stationary background seismicity rate. The non-stationary parameterization leads to a BIC value of -10304, which is smaller than the value of -9880 obtained for the stationary background model. This decrease of the BIC criterion thus ensures that the non-stationary model provides a better fit to the data, while preserving a reasonable level of model complexity.

Best epidemic parameters correspond to values of $A=0.0199 \pm 0.0006$, $\alpha=1.246 \pm 0.014$, $c=(1.35 \pm 0.67).10^{-4}$ and $p=1.065 \pm 0.001$. Confidence intervals here correspond to the range of
values enclosing a 63% decrease of the likelihood function. Interestingly, these estimates of parameters $A$, $\alpha$, $c$ and $p$ fall within the common range for seismicity observed in typical tectonic environments [Ogata, 1992]. This indicates that the self-triggering process in Ubaye is very similar to what is observed along major faults at plate boundaries [e.g. Helmstetter et al., 2003a; Marsan and Lengline, 2008]. We also interpret this close similarity as an indication that our modeling procedure properly succeeded at separating both contributions from, on one hand, the non-stationary forcing and on the other hand, the cascading process of secondary aftershocks.

The resulting model (black curve) of the swarm seismicity rate is in very good agreement with the rate observed at JAUF (gray curve), see Figure 7. This figure also displays the contribution of the non-stationary forcing rate $\lambda_0(t)$ (dashed curve) to the total seismicity rate of the Ubaye swarm. The forcing-induced activity rate increases progressively from the beginning of the swarm up to its apex between day 174 (2003/06/23) and day 350 (2003/12/16), when it led to about 5 events per day. Afterwards, this forcing slowly and progressively weakens towards the end of 2004. The general evolution of the forcing rate consequently presents an evolution that is quite similar to the overall trend of observed activity. This is an indication that low frequency variations of the earthquake rate may be related to a slow and progressive external forcing mechanism, while high frequency variations may be related to cascades of aftershocks sequences. We also note that our model fails at reproducing the amplitude of the four prominent peaks of seismic activity occurring respectively at days 174, 198, 243 and 276. This failure is a direct consequence of the definition of $\lambda_0(t)$ as a stair-step function. Indeed, by keeping a constant value for $\lambda_0(t)$ in each time window, we prevent the model to adapt rapid
fluctuations of the background-forcing rate, probably related with strong transients of the fluid
overpressure.

As explained in the previous section, our estimates of the background rate rely on Hainzl et al
(2006)’s method. In Table 1 we also provide estimates obtained from two other procedures.
The first alternative technique consists in inverting jointly the ETAS epidemic parameters and
background values for all windows (we use time windows as presented in Figure 7). The
second alternative technique attempted at reconstructing the background rate from the
difference between the observed rate of event and the rate of triggered events (estimated from
the ETAS triggering kernel using $A$, $\alpha$, $c$, and $p$ estimates presented in this section). This daily
background rate estimate was initially smoothed over a 100 days time window, and afterwards
averaged for each of the time windows defined above. Although the joint inversion technique
delivers background rate values quite close to estimates using Hainzl et al (2006)’s method, the
second alternative “background reconstruction” technique show higher discrepancies in respect
to this method. Such differences between background rate estimates for these two techniques
(see Table 1) may partly be due to the smoothing used for the background reconstruction
technique (alternative 2), and to the use of different sets of parameters $A$, $\alpha$, $c$, and $p$. However,
all of background rate estimation techniques explained here present overall a reasonable level
of coherency, and background rate estimates undergo very similar evolution patterns.

For the next part of the analysis, we use the background estimates obtained using the modified
change-point procedure described in section 4-1. This technique presents the advantages of
being the most objective, and the most appropriate method to decluster the Ubaye dataset.
Alternative modeling using time windows with constant duration, or constant number of events
have proved to lead to worse adjustments, in terms of BIC values. Best results have been obtained using the modified change-point technique.

5. Retrieval of effective stress changes

In this section, we estimate changes in effective stress (normal stress minus pore pressure) using the earthquake rate at JAUF declustered from its epidemic cascades of aftershocks. The link between the seismicity rate and stress changes arises from the constitutive laws based on rate-and-state friction and proposed by Dieterich (1994).

In the following, we hypothesize that the rate $\lambda_0(t)$ is directly related to a time-dependent change in effective stress within the swarm area. According to the Mohr-Coulomb criterion a decrease of the effective stress $\sigma = \sigma_n - \tilde{p}$ may favor the friction of rocks (i.e. earthquake occurrence) by unclamping faults at depth. Such a decrease of the effective stress can either be related to a decrease in normal stress $\sigma_n$, or to an increase in pore-pressure $\tilde{p}$. This also amounts to consider that cascades of secondary aftershocks ($\lambda(t) - \lambda_0(t)$) reflect the amount of seismicity triggered by shear stress changes on optimally oriented fault planes.

Dieterich et al. (2000) showed that local Coulomb stress changes could be estimated from the temporal changes of the seismicity rate in a given region. According to these authors, there is a non-linear relationship between stress changes and seismicity rates for a population of faults governed by rate-and-state friction laws [Dieterich, 1994]. The seismicity rate $R$ depends on a state variable $\gamma$ according to

$$R = \frac{r}{\gamma \tau_r}$$

(16)
where \( r \) is a reference seismicity rate under a reference shear stressing rate \( \dot{\tau} \). The evolution of the state variable \( \gamma \) is governed by the following differential equation:

\[
d\gamma = \frac{1}{A' \sigma} \left[ dt - \gamma d\tau + \gamma \left( \frac{\tau}{\sigma} - k \right) d\sigma \right]
\]

(17)

In this expression, \( A' \) and \( k \) are constitutive parameters, \( \sigma \) stands for effective stress and \( \tau \) for shear stress.

Here, we set \( R(t) = \lambda_0(t) \), and we calculate \( \gamma(t) \) by use of equation 16. We use a quasi-static formulation of equation 17 with time steps of length \( dt = 1 \) day. For each time step, \( \sigma(t+dt) \) corresponds to \( \sigma(t) + d\sigma \), where \( d\sigma \) is obtained by solving equation 17. In other words, we assume a constant stressing rate for shear stress \( (d\tau = \dot{\tau} \, dt) \) and a quasi-static evolution of effective stress \( d\sigma \) and \( \gamma \), with \( d\gamma = \gamma(t+dt) - \gamma(t) \). This approach tends to underestimate large amplitude, short-lived changes in \( |d\sigma| \) as the background rate is averaged over longer time intervals (see the discussion on time windows in section 4-1).

We select parameters values according to values reported in the literature. We consider a secular linear increase in shear stress with time of \( \dot{\tau} = 2.5 \, \text{kPa} \cdot \text{yr}^{-1} \), based on geodetic estimates in the area [Ferhat et al., 1998] and on a shear modulus equal to \( 0.25 \cdot 10^{11} \) Pa. This hypothesis for shear stress changes appeared as the most reasonable due to the likely influence of fluid pressure on the swarm activity. In addition, to the authors’ knowledge, no complementary geodetic dataset exists to better constrain the evolution of \( d\tau \) during this episode. The reference earthquake rate \( r \) for \( M_L \geq 0 \) is estimated from the rate \( r_1 \) of \( M_L \geq 1 \) event located in the area between 1989 and 2002, when no prominent seismic activity occurred. We obtain \( r_1 = 0.3 \) event/year with \( M_L \geq 1 \) from the relocated catalogue, which leads to \( r = r_1 \cdot 10^{b(1-0.2)} = 2.74 \) events/year with \( M_L \geq 0.2 \). We express changes in effective stress relatively to a reference
steady-state value $\sigma_0$ before the swarm initiation. We choose $\sigma_0$ to be equal to the overburden pressure (with bulk density $\rho=2700$ kg.m$^{-3}$) minus the hydrostatic pressure at 5 km depth. This leads to a steady-state effective stress of $\sigma_0=83$ MPa. According to equation 17 the amplitude of effective stress changes $d\sigma$ is directly related to $\sigma_0$. We have also observed that the relative height of stress steps increases when $\sigma_0$ increases. As a consequence, the selection of initial hydrostatic conditions thus represents a lower bound for changes in effective stress, that is, respectively, a higher bound for changes in pore-pressure. Initial shear stress was chosen to be equal to 0.6 times the steady-state effective stress, i.e. we suppose the crust to be close to a critical state for rupture. Laboratory measurements suggest that the $A'$ parameter usually ranges between 0.005 and 0.015 [Dieterich et al., 2000]. As we have no a priori knowledge on pressure and temperature conditions within the source volume, we choose an average value, i.e. $A' =0.01$. The resulting amplitude of effective stress is also related to the value of parameter $A'$, see equation 17, although stress changes remain of the same order. That is, we obtained maximum stress changes of -3 and of -9 MPa, respectively for $A'$ equal to 0.005 and 0.015. Parameter $k$ is set equal to 0.23 [Linker and Dieterich, 1992]. Figure 8 displays the effective stress history obtained using this procedure. The step-like shape is obviously unrealistic but is directly inherited from assumptions on $\lambda_0(t)$. This curve should consequently be understood as a first-order estimate of effective stress changes during the swarm. Negative changes in effective stress mean that the triggering of micro-earthquakes during the Ubaye swarm occurred either by a decrease in normal stress or by an increase in pore-fluid pressure. Finally, if one assumes constant normal stress conditions, this result suggests that a pore-pressure increase of about 8 MPa was sufficient to generate 41% (1448
background events) of the seismic activity in Ubaye between January 2003 and December 2004.

6. Discussion

In the previous sections, we have shown that the Ubaye swarm i) occurred on a simple planar structure striking N130E and dipping 80°W, ii) exhibited an unusual diffusive migration of hypocenters towards the SE, and iii) required the contribution of an external non-stationary forcing rate in addition to the self-triggering of seismicity (via cascades of secondary aftershocks). Assuming that fluid circulations at depth induced a significant part of this activity, we explain the migration of earthquake hypocenters as the result of a fluid diffusion process within the crystalline basement. Moreover, the distribution of seismicity along a preferential plane suggests that fluids may have propagated through a more permeable channel, possibly inherited from a preexisting fault structure. The diffusive migration of hypocenters during the swarm is also an indication that fluid overpressure at depth was not high enough to open new fractures in the medium.

The evocation of deep fluid circulation is of common use for explaining the spatial and temporal properties of seismic swarms [Horálek and Fischer, 2008]. In Ubaye, although no fluid outflow was observed during the sequence, we propose that a fluid overpressure at depth was responsible for the 2003-2004 swarm episode. First, this proposition relies on the similarity of the earthquake migration pattern with those observed during other swarm episodes that have been convincingly related with fluid circulations [Tsuneishi and Nakamura, 1970; Horálek and Fischer, 2008]. Second, it also relies on considerations about the present and past fluid circulations in the same bedrock, observed few kilometers further south. Recalling that the swarm activity was confined within a 3 to 8 km band at depth, the seismogenic structure of
the swarm is most probably confined within the crystalline bedrock, rather than within the overlying 1- to 2-km-thick Embrunais-Ubaye nappe [Jenatton et al., 2007]. The bedrock crops out few kilometers south of the Ubaye valley, forming the Argentera Massif. In this massif, numerous outcropping fault structures and rock weathering related with fluid circulations can be studied directly in the field. Fault structures show preferential orientations along a direction sub-parallel to the swarm alignment (see Baietto et al., 2009 and references therein). Furthermore, several places in the Argentera Massif are well known for their geothermal activity, like Bagni di Vinadio, Italia, or Terme di Valdieri, Italia, about 15 km southeast of the former (Figure 1). Baietto et al. (2008; 2009) studied the geological settings related with geothermal circulations in these areas. They reported an important fluid outflow at Terme di Valdieri, with a bulk discharge rate of 50 kg.s\(^{-1}\) and a fluid temperature reaching up to 70°C. According to these authors, fluids chemical properties are also consistent with a circulation path within the crystalline basement, that is, going down to 5-6 km depth below the surface. As a consequence, the involvement of fluid circulations within the basement in Ubaye appears a very reasonable hypothesis, and is quite consistent with circulation depth estimated in the Argentera area.

The analysis presented in section 5 shows that changes in effective stress can be estimated by use of the complete form of the differential equation for rate-and-state constitutive laws (see equation 17). Assuming constant normal stress during the sequence, a progressive increase in pore-pressure up to about 8 MPa could be sufficient to trigger the 16,147 events swarm. Figure 8 also shows that pore-pressure progressively increased to this maximum value in 350 days, and decreased afterwards by 7 MPa in about 350 days. This slow evolution of the pore-pressure may explain the particularly long duration of this swarm episode.
These estimates of pore-pressure change are in good agreement with numerical modeling of fluid circulations during swarm episodes, and with observations from fluid injection experiments. In a recent study of the 1965-1967 Matsushiro swarm in Japan, Cappa et al. (2009) argued that pore-pressure changes of 4 MPa were necessary to quantitatively reproduce the observed seismicity, deformation, and fluid outflow at the surface. Hainzl and Ogata (2005) also found that a pore-fluid diffusion mechanism with a maximum pore-pressure change of 2 to 5 MPa was compatible with the seismic properties of the Vogtland-West Bohemia swarm. In another example, Miller et al. (2004) showed that CO₂ pore-pressure changes of about 10-20 MPa can explain the spatial migration of the 1997 sequence of 6 M>5 earthquakes in central Italy. These authors also argued that such changes in pore-pressure are large enough to overwhelm static shear stress changes. In Ubaye, we find that for pore-pressure changes of about 8 MPa, shear stress transfers (leading to successive cascades of aftershocks) could still induce 59% of the seismic activity. Our estimates also agree with the results of Cornet et al. (1997) who reported seismicity in response to overpressure between 5 and 10 MPa during the 1993 fluid injection experiment at Soultz-sous-Forêts, France. The initiation of the swarm activity for very slight pore pressure changes (< 1 MPa) during the first days of 2003 is also very consistent with the conclusions of Zoback et al. (1997) and Shapiro et al. (2006a), and confirms the critical state of the fault before the swarm episode. Toda et al. (2002) proposed that earthquake swarms might be driven by change in shear stressing rate. They proposed that, according to this principle, aftershock duration would decrease with increasing shear stressing rate changes. However, we show here that the decrease in effective stress due to pore-pressure diffusion at depth constitutes another viable explanation for swarm generation. Our results also indicate that the seismicity in Ubaye area results from
the superposition of a time-varying external forcing over cascades of seismicity with constant
aftershock duration.

7- Conclusion

We have presented a new analysis of the Ubaye seismic swarm. This study relies on the
catalogue built by the French Sismalp seismological network, which we improved by
relocating 974 earthquakes. We also used the time series of 16,147 event detections at station
JAUF in 2003-2004. We have identified a clear spatial migration of earthquakes, along a sub-
vertical N130E fault structure. We interpreted this as the result of fluid circulation at depth.
Thus, the initiation and development of the Ubaye swarm could be related to the diffusive
propagation of fluid overpressure within the crystalline basement. An important result of this
study is the assessment of the associated fluid overpressure from the analysis of the earthquake
rate. This calculation is based on rate-and-state constitutive laws applied to the non-stationary
rate of fluid-driven (i.e. background) seismicity. We found that pore-fluid pressure varied with
time during the swarm sequence, with a maximum excess of pore-pressure of 8 MPa, with
respect to the level that preexisted before January 2003. This value is comparable with
estimates from numerical modeling of swarms in Italy and in Japan, or with direct pressure
measurements realized during fluid injection experiments.

Besides, some aspects of the fracture process still remain open questions, and could not be
addressed within the framework of the present study. For example, was the permeable channel
localized within the core or within the damage zone of the source fault? What was the
physico-chemical nature of fluids involved? How can we model their path to the seismogenic
zone? Did the presence of the overlying nappes in Ubaye played a role in the structure design
of the source?
Each of these aspects needs further investigation in the framework of a careful geological study of the area. Clarifying the process of fluid refill, its behavior at depth and its interplay with the basement geology are now essential steps to consider for a comprehensive explanation of episodic swarm occurrences in the Ubaye valley, and worldwide.

Acknowledgments

E.P. was supported by the CNRS-ANR ASEISMIC project. We also acknowledge the following institutions for their support to the Sismalp permanent network. The conseil général de l’Isère, the Délégation aux Risques Majeurs (French Ministry of the Environment), the Institut National des Sciences de l’Univers (CNRS), and the Conseil Régional Rhône-Alpes funded the Sismalp network. The Bureau Central Sismologique Français, the regional direction of the Environment (Dreal Rhône-Alpes), the Observatoire de Grenoble (OSUG), and the Conseils Généraux (Isère, Alpes-de-Haute-Provence, Hautes-Alpes, Haute-Savoie, Ain, and Savoie) support its running costs. The authors would like to thank the associate editor and two anonymous referees for their thorough reviews and helpful suggestions.
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<th>174</th>
<th>350.8</th>
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<td>Window ending time (days)</td>
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<td>174</td>
<td>350.8</td>
<td>458.8</td>
<td>614.9</td>
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<th>( Hainzl et al (2006) )'s method</th>
<th>Alternative 1: Joint inversion</th>
<th>Alternative 2: Background reconstruction method</th>
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Table 1: Limits of optimal time windows and amplitude of the background rate. We here present background rate estimates obtained from three different algorithms. Best adjustments are obtained using *Hainzl et al. (2006)*'s method. Two alternative techniques were tested. The first one inverts jointly ETAS epidemic parameters and background values. The second technique reconstructs the background rate from the difference between the observed rate of event and the rate of triggered events (obtained from the ETAS triggering kernel and \( A, \alpha, c, \) and \( p \) estimates). The differences between the background estimates for the alternative techniques 1 and 2 may partly be due to the smoothing used for the background reconstruction technique (alternative 2), and to the use of different sets of ETAS parameters \( A, \alpha, c, \) and \( p \). See section 4-2.
Figure 1: Map of the Southwestern Alps with main geological features. Crossed areas stand for the Pelvoux, Argentera and Dora Maira crystalline massifs. The lightly shaded area is the Embrunnais-Ubaye nappes. The dark gray area is the Peninnic domain. Fault traces after Sue (1998). Stars correspond to macro-seismic (M) and computed (C) epicenters of the 1959 M 5.5 St-Paul-sur-Ubaye damaging earthquake. Black triangles are permanents seismological stations from the Sismalp network, and black squares stand for temporary seismological stations deployed in the area from September 2003. White squares are hot springs. PP: Plan de Phasy; BV: Bagni di Vinadio; TV: Terme di Valdieri. The dash-dotted line is the French-Italian border. The study area is delimited by the box in the center of the map. Modified from Jenatton et al., 2007.
Figure 2: Map of the Ubaye 2003-2004 seismic swarm. The panels present a relocation of 974 seismic events a) in map view and b) in cross-section. Coordinates are projected on a planar orientation striking N130E, and dipping 80°W. Origins of coordinate axes correspond to the surface projection of the swarm centroid (with geographical coordinates 44°27.2N, 6°45E). Depth is expressed relatively to the sea level. Small dots stand for events with magnitude less than 2, and large dots represent earthquakes with magnitude larger than, or equal to 2. The color-scale highlights the date of each earthquake from January 2003 (magenta) to December 2004 (red).
**Figure 3:** (Top) Timeseries and magnitudes of the 16,147 events recorded at station JAUF between Jan 1st, 2003 (day 0) and Dec 31st, 2004 (day 730). (Bottom) Rate of $M_L \geq 0.2$ earthquakes detected at station JAUF (grey curve) and of $M_L \geq 1$ earthquakes relocated in this study (black curve, see also Figure 2).
Figure 4: Distributions of strike (left) and dip (right) angles for planes associated with seismic events of the relocated catalogue. Plane orientations were estimated for each possible set of 3 earthquakes using the method of Fehler et al. (1987). Sector length indicates the number of earthquakes associated with each plane orientation. On the left diagram, sector direction indicates the azimuth of planes, with 0° and 90° standing respectively for the North and the East directions. Bins are 10° wide. A clear preeminence exists for events occurring along planes striking N130°E and dipping 80°W.
Figure 5: Characteristic size $R$ of the main swarm cluster as a function of time. For a given time $t$, $R$ is measured as the average distance between all swarm events that occurred at time $t_i < t$ and the first earthquake of the sequence. After $\sim 30$ days of relative stability, this average distance increases as $R \sim t^{0.41}$ with $H = 0.41 \pm 0.06$. For the sake of comparison, we have represented in the lower right corner slopes that should be expected for a normal diffusive process ($H = 0.5$) and for a typical sub-diffusive process expected during aftershock sequences ($H = 0.1$). Information on the spreading of the data is given by the grey solid circles, which indicate the distance between every relocated earthquake and the first one of the sequence.
Figure 6: Adjustment of inter-event times distributions (dots) by a Gamma distribution (curve), according to a maximum likelihood method. Each subplot corresponds to the inter-event times distribution for a single time window with a constant background rate $\lambda_0(t)$. Time windows are defined by a change-point analysis, based on significant changes in successive inter-event time distributions (see section 4-1).
Figure 7: Comparison of the Ubaye seismic activity detected at station JAUF (gray curve) with the best non-stationary ETAS model (black curve), see equations (2) and (3). Best epidemic parameter estimates are $A=0.0199$, $\alpha=1.246$, $c=1.35\cdot10^{-4}$ day and $p=1.065$. The stair-step dashed line stands for the non-stationary background contribution $\lambda_0(t)$ to the seismicity rate. See also Table 1 for a report on the amplitude of $\lambda_0(t)$ for each time window. This stair-step shape arises from the determination of optimal time windows with a constant background rate $\lambda_0(t)$, as determined by the change-point method explained in section 4-1. This method is based on inter-event time adjustments presented on Figure 6.
**Figure 8:** Changes in effective stress integrated over the swarm area. These changes are estimated from the rate of background event $\lambda_0(t)$ represented on figure 7, and by use of rate- and-state constitutive laws for earthquake production [Dieterich, 1994; Dieterich et al., 2000], see section 5. We supposed that this seismicity rate was triggered by changes in effective stress under a constant shear stressing rate of $2.5 \times 10^{-3}$ MPa.yr$^{-1}$. Effective stress is expressed relatively to the steady-state value of 83.4 MPa before the swarm initiation. This value comes from the difference in overburden pressure (with bulk density $\rho=2700$ kg.m$^{-3}$) minus the hydrostatic pressure at $z=5$ km.