Analysis of Rock-Fall and Rock-Fall Avalanche Seismograms in the French Alps

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Abstract This study reviews seismograms from 10 rock-fall events recorded between 1992 and 2001 by the permanent seismological network Sismalp in the French Alps. A new seismic-magnitude scale was defined that allowed us to compare and classify ground-motion vibrations generated by these Alpine rock falls. Each rock fall has also been characterized by its ground-motion duration $t_{30}$ at an epicentral distance of 30 km. No relation was found between rock-fall parameters (fall height, runout distance, volume, potential energy) and rock-fall seismic magnitudes derived from seismogram amplitudes. On the other hand, the signal duration $t_{30}$ shows a rough correlation with the potential energy and the runout distance, highlighting the control of the propagation phase on the signal length. The signal analysis suggests the existence of at least two distinct seismic sources: one corresponding to the initial rupture associated with an elastic rebound during the detachment and the other one generated by the rock impact on the slope. Although the fall phenomenon includes other complex processes (fragmentation of the block, interaction with topography, plastic deformation during and after impact) 2D finite-element simulations of these two seismic sources are able to retrieve the main seismogram characteristics.

Introduction

Rock fall is the detachment of blocks from a steep slope along a surface on which little or no shear displacement takes place (Cruden and Varnes, 1996). The mass descends by falling, bouncing, and/or rolling, with a very rapid to extremely rapid movement. After a free fall with a vertical drop $H_f$ from the source rock slope (Fig. 1), the falling mass strikes the talus slope and breaks up and/or bounces with a rebound depending on material properties (Giani, 1992; Okura et al., 2000). Lower down, the talus angle diminishes and rock fragments tend to roll. Rock-fall volumes may range from a few m$^3$ to $10^9$ m$^3$ in terrestrial settings (Nicoletti and Sorriso-Valvo, 1991; Corominas, 1996). Small rock falls are characterized by a more or less independent movement of individual particles (fragmental rock fall; Evans and Hungr, 1993), as opposed to large rock falls that generate extremely rapid flows of dry debris and are usually called rock avalanches (Hsu, 1975; Evans and Hungr, 1993; Cruden and Varnes, 1996). There is no well-defined volume limit and various volume thresholds were proposed for defining rock falls, from $10^4$ m$^3$ (Hungre et al., 2001) to $10^5$ m$^3$ (Evans and Hungr, 1993). Rock-fall characterization is generally assessed by multiplying the deposit area ($A$) by an estimation of average thickness ($T$). Other sources of information for characterizing rock falls are the seismograms provided by permanent seismological networks, which are often the only measurements available during the event. Surprisingly, rock falls—and more generally, landslide records—have been little used so far for characterization purposes. We give here a quick (and nonexhaustive) review of the studies of seismic waves generated by landslides in general, with a focus on rock falls.

Berrocal et al. (1978) studied the seismic phases generated by the large $1.3 \times 10^9$ m$^3$ Mantaro landslide (25 April 1974), which was widely recorded by seismic observatories, at local and teleseismic distances. They showed that the seismic energy for this $M_s 4.0$ event is about 0.01% of the kinetic energy, which, in turn, is about 1% of the potential gravitational energy. To our knowledge, the first detailed study on landslide characterization from seismograms was made by Kanamori and Given (1982) and Kanamori et al. (1984) who analyzed seismic signals recorded during the eruption of Mount St. Helens (18 May 1980). They concluded that the long-period seismic source can be represented by a nearly horizontal single force with a characteristic time constant of 150 sec and that this single force is due to the massive $2.5 \times 10^9$ m$^3$ landslide affecting the north slope of Mount St. Helens. Other studies performed by Kanamori
and co-authors on massive landslides (Eissler and Kanamori, 1987; Hasegawa and Kanamori, 1987; Brodsky et al., 2003) confirmed that the long-period seismic radiation is better simulated using a nearly horizontal single force rather than a double couple. Later, Dahlen (1993) interpreted landslides as shallow horizontal reverse faults and showed that the seismic source can, in the long-wavelength limit, be represented by a moment tensor that reduces to a horizontal surface point force if the shear-wave velocity within the sliding block is significantly lower than the one of the slope. Weichert et al. (1994) examined the seismic signatures of the 1990 Brenda Mine collapse (\(V = 2 \times 10^6\) m\(^3\)) and of the 1965 Hope rockslides (\(V = 47 \times 10^6\) m\(^3\)), with a focus on the differentiation between seismic signals from landslides and real earthquakes. They suggested a long-period/short-period discriminant (\(M_s\) versus \(m_s\) seismic magnitudes) and they observed a correlation between the efficiency of potential to seismic energy conversion with the slope of the slide detachment. Very low efficiency (about \(10^{-6}\)) was obtained when using Richter’s (1958) energy equation. For the Hope events, they observed two phases on the long-period records that they interpreted as the initial downhill thrust, followed one-half minute later by the impact on the opposite valley side. La Rocca et al. (2004) analyzed the seismic signals produced by two landslides that occurred with a delay of 8 min at the Stromboli volcano on 30 December 2002, with volumes of about \(13 \times 10^6\) and \(7 \times 10^6\) m\(^3\). Both landslides generated complex seismic signals with an irregular envelope, a frequency range between 0.1 and 5 Hz, and duration of a few minutes. Comparing the observed low-frequency seismograms with synthetic signals, La Rocca et al. (2004) estimated the magnitude of the force exerted by the sliding mass, from which they inferred the landslide volumes. Compared to the works on massive rockslides, studies of rock-fall seismic signals have been very few. Norris (1994) reviewed seismograms from 14 rock falls and avalanches of moderate to large volumes (\(10^4\)–\(10^7\) m\(^3\)) at Mount St. Helens, Mount Adams, and Mount Rainier in the Cascade Range. At Mount St. Helens, the analysis of five rock falls (\(10^5\)–\(10^6\) m\(^3\)) suggested a consistent increase in seismogram amplitude with the volume of rock falls having the same source area and descent paths. On the contrary, rock-fall sequences or smaller rock falls, such as those studied earlier at Mount St. Helens (Mills, 1991) and Makaopuhi Crater (Tilling et al., 1975), show a poor correlation between signal amplitude/duration and volume. In the conclusions, the authors stressed the importance of seismic networks for detecting large mass movements. In Yosemite Valley, the records of the 10 July 1996 Happy Isles rock fall were studied by Uhrhammer (1996) and Wieczorek et al. (2000). They found that the prominent seismic phases (\(P\), \(S\), and Rayleigh waves) are consistent with two rock impacts 13.6 sec apart and they calculated a seismic magnitude of 1.55 and 2.15 for these two events. In order to test the feasibility of monitoring rock falls with seismic methods in Yosemite Valley, Myers et al. (2000) deployed a network of five stations in the late summer and fall of 1999. They concluded that monitoring using seismic records was theoretically feasible and that an event with equivalent earthquake magnitude of 2.6 would be located. However, the detection of rock-fall-related events was not verified. In a recent paper reviewing rock falls and rock avalanches that occurred in 1991 and 1996 in Mount Cook National Park (New Zealand), McSaveney (2002) displayed several seismograms recorded during these events at distances between 31 and 190 km. He used these signals for providing an estimate of rock-fall duration but no attempt was made to link the seismic parameters to the rock-fall geometric properties or to give a quantitative distribution of mass collapse over time.

This introduction illustrates the attempts and the difficulty of extracting relevant information on landslide characteristics from seismic signals. Compared to previous works, our study is focused on rock falls and rock-fall avalanches, and particularly on those that occurred in the Alps between 1992 and 2001 and were recorded by the French permanent seismological network Sismalp (Thouvenot et al., 1990; Thouvenot and Fréchet, 2006).

The aims of this article are fourfold: (i) to evaluate the ability of this network to detect rock falls in the western Alps, (ii) to identify the seismic parameter(s) that could characterize rock falls and help in classifying them, (iii) to establish the relation (if any) between the seismic parameters and the geometric characteristics of rock falls, and (iv) to identify the seismic sources appearing in the signals and to study the potential link between them and the different phases of a rock fall (detachment, impact, rolling, and/or sliding). In the first step of the study, we try to obtain simple relations between seismic and rock-fall parameters, in order to determine the potentiality of seismic parameters for rock-fall characterization. In the second part of the study, we use signal-processing techniques and 2D numerical modeling for interpreting the different seismic phases appearing within the seismograms.
Rock-Fall Location and Characteristics

Rock falls with a volume larger than $10^3$ m$^3$, which occurred in the western Alps during the 1992–2001 period, were extracted from different inventories (Bureau de Recherches Géologiques et Minières database, www.brdmvt.net; Fraysseins and Hantz, 2006) and cross-checked with data from the Alpine permanent seismological network (Sismalp). The Sismalp project, launched in 1987, aimed at deploying a network of several tens of automatic seismic stations in southeastern France, from Lake Geneva to Corsica (Thouvenot et al., 1990). In its present state, the network consists of 44 stations that monitor the seismic activity over an area covering around 70,000 km$^2$ with distances between stations of about 30 km (Thouvenot and Fréchet, 2006). All of the stations of the network are equipped with 1-Hz Mark-Product L4C velocimeters, 10 of which are three-component instruments. At each station, a microprocessor scans the digital signal, and, whenever a detection criterion is met, the corresponding signal is stored in memory. The equipment used at the turn of the 1980s allowed the storage of six 40-sec signals only. Upgraded at the end of the 1990s, it can now store hundreds of triggered signals, each up to 4-min long. Stations are connected to the switched telephone network and are dialed every night from a central station at the Grenoble Observatory. Any earthquake with an $M_L$ larger than about 1.3 can be detected and located (two events per day on average); the location precision on the hypocenter is high, with horizontal uncertainties smaller than 1 km for $M_L > 2$ events.

Only events recorded by at least three seismic stations were considered in this study. Figure 2 shows the location of the 10 selected rock falls and rock-fall avalanches ($R_1$–$R_{10}$) and of the 39 Sismalp seismological stations (out of a total of 44) installed north of the 44° N parallel. Two events ($R_1$, La Palette, and $R_{10}$, La Dent du Loup) are located 15 km northwest of Grenoble, six ($R_2$, Versaire, and $R_5$–$R_9$), Saint-Antoine valley) are clustered 30–40 km east of Grenoble, and the remaining two occurred near the Swiss and Italian borders ($R_6$, Les Drus) or in Switzerland ($R_3$, Sandalp). Eight rock falls ($R_1$, $R_3$, and $R_5$–$R_{10}$) occurred in limestone, one in amphibolite ($R_2$), and one in granite ($R_4$). All sites exhibit near-vertical slopes (over 70°) in or under the source zone, which implies a free-fall phase during the movement (Cruden and Varnes, 1996).

The main characteristics of the 10 rock-fall events are listed in Table 1. They were obtained from international publications ($R_1$, $R_3$, and $R_{10}$) and unpublished geotechnical reports ($R_2$, $R_4$, and $R_5$–$R_9$). Fall volumes vary over a wide range from $2 \times 10^4$ m$^3$ to $1.75 \times 10^6$ m$^3$ for total drop heights between 270 and 820 m and runout distances between 190 and 1300 m.

The La Palette rock fall (event $R_1$) occurred in the upper part of a 250 m high, 70° dipping cliff composed of thick limestone beds dipping 10°–30° transversely to the slope (Frayssine and Hantz, 2006). The initial failure mechanism is a slide along a 45° dipping joint; the sliding mass ($2 \times 10^4$ m$^3$) fell 170 m down to the underlying 50°–30° dipping marly slope, where it propagated up to 450 m from the failure scarp. The Versaire rock fall ($R_2$) occurred in the upper part of a 150 m high, 70° dipping cliff made of massive amphibolite. The initial failure mechanism is a slide; the sliding mass ($5 \times 10^4$ m$^3$) fell 100 m down to the underlying 50° dipping amphibolite slope, where it propagated up to 250 m from the failure scarp. The Sandalp rock fall ($R_3$) took place in the middle part of a 700 m high rock wall, which consists in thick near-horizontal limestone beds (Keusen, 1998). The rock mass ($1.75 \times 10^6$ m$^3$) initially slid on 45° dipping schistosity planes, jumped over a 100 m high, 80° dipping cliff, moved on a 35° dipping limestone slope, and stopped in the valley with a runout distance of 1300 m. Because of the intense schistosity of the rock mass, an important part of the avalanche deposit consists in fine particles. The Drus rock fall ($R_4$; Ravanel and Deline, 2006) took place in the middle part a 700 m high, 75° dipping granite wall, in the Mont Blanc Massif. The failure mechanism might have been topple or slide and the drop height reached 450 m. Between January 1998 and June 1999, five rock falls ($R_5$–$R_9$) affected a 500 m high cliff made of thin folded limestone beds, in the Saint-Antoine valley. Volumes ranged from $3 \times 10^4$ to $1 \times 10^5$ m$^3$. They occurred at different heights in the middle part of the cliff that dips 70°. The first two rock falls ($R_5$ and $R_6$) involved tall columns with beds dipping opposite to the slope. The failure mechanisms might have been topple or slide, with a fall height of 90–100 m. The three following ones ($R_7$–$R_9$) were located higher in the cliff (fall height of 190 m) and were slides along bedding planes, steeply dipping towards the slope. The fallen masses then propagated on a slope made of marl and limestone thin layers, whose slope angle decreases from 65°–25°. Finally, the Dent du Loup rock fall ($R_{10}$) occurred in a 200 m high, 70° dipping cliff, made of thick limestone beds dipping 10°–30° opposite to the slope (Frayssines and Hantz, 2006). The initial failure mechanism is a stepped slide on 75° dipping joints. The sliding mass ($2 \times 10^3$ m$^3$) then fell down to the underlying 35° dipping scree slope, where it propagated up to 300 m from the failure scarp.

All of these rock failures took place in a steep cliff (with a slope of at least 70°) and were followed by a free-fall phase. Considering the volume threshold ($10^4$ m$^3$) proposed by Hungr et al. (2001), all of these events should be classified as rock avalanches, except the Dent du Loup rock fall ($R_{10}$) whose size ($2 \times 10^3$ m$^3$) is too small. However, eight of the events have a volume between $10^4$ and $10^5$ m$^3$, which is the other threshold proposed by Evans and Hungr (1993). Thus, the limits between a rock fall and a rock avalanche cannot be defined precisely, as the interactions between the blocks progressively increase with the number of blocks and the volume. Only the Sandalp event ($R_3$) can be unambiguously classified as rock avalanche. For simplicity’s sake, we will use the general term rock fall in the following, except when specifically discussing the mechanisms (fragmental rock fall or rock-fall avalanche).
These rock falls were recorded by a number of stations varying between 3 and 21, with distances ranging from 10 to a maximum of 250 km. Distances between the events and the closest station are usually between 10 and 25 km.

Figure 3 shows seismograms recorded during event $R_9$ for five distances from 25–83 km. One can observe the quick degradation of the signal-to-noise ratio with the epicentral distance, resulting from the strong attenuation in shallow crustal layers. In Figure 4 are plotted the vertical seismograms and the displacement Fourier spectra of the 10 events for the nearest records. The seismograms exhibit various and complex waveform shapes from one event to the other, with emergent beginnings and several late energetic phases that we will attempt to interpret further in this article. The corner
frequency of the spectra, marked by an arrow in Figure 4, is always close to 1 Hz whatever the event, showing that 1-Hz velocimeters only record the high-frequency part of ground motion. These results support the deployment of broadband seismometers for analyzing the frequency content of rock-fall signals.

Table 1 lists location and characteristics for the 10 events. The free-fall drop height ($H_f$) varies from 90 to 450 m and the potential energy values ($E_p$) values are between 6.5 and 6560 GJ for volumes ranging from $2 \times 10^3$ to $1.75 \times 10^6$ m$^3$. Table 1 also includes local seismic-magnitude values ($M_L$) provided by the Sismalp network, using the Richter empirical model (1958). These values are between 0.9 and 2.8. Except for event R3 ($M_L$ 2.8), other rock falls have low magnitudes (0.9–1.7), actually very close to—and sometimes beyond—the lowest magnitude detectable by the network, estimated to $M_L$ 1.3 and twice lower than the one assessed for the network deployed in the Yosemite valley (Myers et al., 2000). Moreover, locating rock falls with emergent P onsets and unclear S onsets is a challenge difficult to face by a seismic network, although other types of seismic arrays such as antennae might have better capabilities in this respect. The limited number of observed events (10) and of the corresponding records (103 in total) partly results from the relative sparseness of the stations and from the wave attenuation in the upper crust. However, as pointed out by Weichert et al. (1994) and suggested by the low-$M_L$ values in Table 1, the poor efficiency of potential to seismic energy conversion is probably a significant limiting factor, the effect of which will be addressed further in this article.

Seismic Record Analysis and Rock-Fall Seismic-Magnitude Scale

Our aim is to characterize rock falls from the analysis of the recorded seismograms. In this part, the event is treated as an entity (we do not separate the detachment, impact, and propagation phases) in order to have a global characteristic. The first option is to compare rock falls in terms of seismic magnitude in a way similar to what was done for earthquakes. The $M_L$ scale was defined from the maximum recorded displacement (Richter, 1935, 1958) for segregating large, moderate, and small shocks. The relation between the maximum seismographic amplitudes for a given shock and the given shock to that of a standard shock at the same epicentral distance. The standard shock (seismic magnitude 8) was assumed that the ratio of the maximum amplitudes recorded displacement (Richter, 1935). Kradolfer and Mayer-Rosa (1988) showed that this relationship is

\[ \frac{A_{\text{max}}}{A_{\text{max}}^0} = 10^{M_L - M_L^0} \]

where $A_{\text{max}}$ is the maximum amplitude, $A_{\text{max}}^0$ is the maximum amplitude of a standard shock, $M_L$ is the local seismic magnitude, and $M_L^0$ is the new rock-fall seismic magnitude, and $E_s$ is the seismic energy derived from equation (4).

<table>
<thead>
<tr>
<th>Date (dd/mm/yyyy) (UTC)</th>
<th>Longitude (E)</th>
<th>Latitude (N)</th>
<th>$N_p$</th>
<th>Event</th>
<th>$V$ (m$^3$)</th>
<th>$D_r$ (m)</th>
<th>$H_f$ (m)</th>
<th>$E_p$ (GJ)</th>
<th>$M_L$</th>
<th>$M_L^0$</th>
<th>$E_s$ (MJ)</th>
<th>$E_s/E_p$</th>
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<td>5°58</td>
<td>45°24</td>
<td>4</td>
<td>R1</td>
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<td>450</td>
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<td>1.5</td>
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<td>45°12</td>
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<td>270</td>
<td>125</td>
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<td>1.8</td>
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<td>46°46</td>
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<td>150</td>
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<td>800</td>
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$N_p$ is the number of stations having recorded signals, $V$ is the volume, $H_f$ is the vertical free-fall height of the center of gravity, $D_r$ is the runout distance, $H_t$ is the total drop height, $E_p$ is the initial potential energy ($\rho V g H_f$), $M_L$ is the local seismic magnitude, $M_L^0$ is the new rock-fall seismic magnitude, and $E_s$ is the seismic energy derived from equation (4).
For defining a seismic-magnitude scale for rock falls, it is first necessary to determine the relation between the maximum seismographic amplitudes of a given rock fall at various distances. Because of the small number of available events and records (67 vertical-component records), the following simple attenuation relationship was used (Ambraseys et al., 1996; Gasperini, 2002; Berge-Thierry et al., 2003): 

$$\log_{10}(PGD) = b + b_m M_L + b_r \log_{10}(r) \pm \sigma, \quad (1)$$

where PGD is the peak ground displacement, $M_L$ the local seismic magnitude, $r$ the epicentral distance (in kilometers), and $\sigma$ the standard deviation. Parameters $b$, $b_m$, and $b_r$ are empirical coefficients determined from the linear regression on the values of peak displacements and epicentral distances. In this relation, we propose that the $M_L$ is replaced with $M_{rf}$, which will be called the rock-fall seismic magnitude. In order to determine both the attenuation model coefficients of equation (1) and the seismic magnitude, an iterative scheme was applied. In a first step, rock-fall seismic magnitudes $M_L$ are approximated by $M_{rf}$ and the coefficients $b$ ($b_m$, $M_{rf}$) and $b_r$ are determined by fitting equation (1) to the data. Using Richter’s original definition of an $M_L$ 0 shock, $M_{rf}$ values have been computed from the ($b_m$, $M_{rf}$) terms. Equation (1) is then updated with these new $M_{rf}$ values. The iterative process is stopped when the root-mean-square difference between two iterations is stable. The attenuation relation obtained for rock falls is given by

$$\log_{10}(PGD) = -1.58[\pm0.39] + 1.00[\pm0.27] \times M_{rf} - 0.94[\pm0.18] \times \log_{10}(r) \pm 0.21, \quad (2)$$

where the seismic magnitude $M_{rf}$ is defined as the logarithm of the ratio of the amplitude for the given rock fall to that of the standard rock fall at the same epicentral distance. The 95% prediction interval bands for each parameter are indicated between brackets. The PGDs as a function of distance are shown in Figure 5a for the 10 rock falls. In the same graphs are plotted the Richter attenuation laws derived for the $M_L$ values. In Figure 5b, the new attenuation relation is compared to corrected displacement data and to the corresponding Richter attenuation law. The amplitude decay for some rock falls ($R5$, $R6$, $R8$, $R9$, and $R10$) significantly differs from the Richter attenuation curve used for earthquake characterization. This highlights the expected predominance of surface waves generated by rock falls. $M_{rf}$ and $M_L$ values are given for the 10 rock falls in Table 1. $M_{rf}$ values exhibit a narrower range (1.2–2.1) compared to $M_L$ values (0.9–2.8) due to the smaller slope of the attenuation model.

As the corner frequency of the displacement spectra has been shown to be an unreliable source parameter (Fig. 4) due to the frequency cutoff of the short-period seismometers, we investigate the possibility of using the signal duration for characterizing and discriminating the rock falls. The ground-motion duration was computed for all rock-fall seismograms, following the definition (Trifunac and Brady, 1975) that is the time interval between the points at which 5% and 95% of the total energy has been recorded. Figure 6 shows the duration-distance graphs for the 10 events in a bilogarithmic diagram for distances shorter than 100 km. The 40-sec record length on most Sismalp stations was too small to measure the signal duration for the high-volume event ($R3$). For events $R10$, only three stations exhibit a good
signal-to-noise ratio. Data for the remaining eight events show a regular increase of the duration with the epicentral distance, resulting from the propagation of waves at different velocities and from diffusion in the crust. A theoretical relation (equation 3) was fitted to each dataset and the regression parameters \( a_1 \) and \( a_2 \) are given in Table 2, with their 95% prediction interval bands:

\[
\log_{10}[t(r)] = a_1 + a_2 \log_{10}(r).
\]  (3)

The slope parameter \( a_2 \) varies between 0.1 and 0.85. The \( a_2 \) values with reasonable prediction interval bands are between 0.35 and 0.42. A value of 0.33 was found considering all events. As most signals were recorded in the 20–40-km distance range, each rock fall was characterized by the ground-motion duration \( t_{30} \) computed at an epicentral distance of 30 km using equation (3). This value, which is calculated with the global total energy recorded on seismogram, includes all of the phases of rock falls: detachment, impact, and propagation of the mass. Values of \( t_{30} \) given in Table 2 will be discussed in the next section.

Comparison between Seismic and Rock-Fall Characteristics

Despite the few recorded rock falls, we attempt to link the measured ground-motion characteristics (rock-fall seismic magnitude, seismic energy, and duration) to the rock-fall parameters (fall height \( H_f \), runout \( D_p \), volume \( V \), and potential energy \( E_p \)).

Seismic energy for landslides is hard to assess from seismic records, as it depends on the radiation pattern that is generally unknown. This difficulty and the scarcity of records explain why previous works on energy calculation used the formulas established for earthquakes. Wiechert et al. (1994) considered Richter’s formulas for deriving the seismic energy released by several landslides from \( M_s \) and \( M_L \). In this study, we applied Kanamori’s (1977) equation,

\[
\log_{10} E_s = 1.5 M_s + 4.8,
\]  (4)

where \( E_s \) is in joules and \( M_s \) is the surface-wave magnitude. \( M_s \) was replaced by \( M_{rf} \) for computing \( E_s \) values for the 10 rock falls given in Table 1. This relation is very close to the one proposed by Richter (1958) from surface waves.

Figure 7 compares in a systematic way the three ground-motion and the four rock-fall characteristics. As \( E_s \) and \( M_{rf} \) are linked, they are plotted in the same graphs with different ordinate values. The comparison of the seismic energy \( E_s \) with the potential energy \( E_p \) (Fig. 7a) shows that only a very small amount of the fall energy is transmitted as seismic waves. The \( E_s/E_p \) ratio varies between \( 10^{-6} \) and \( 10^{-3} \) (see Table 1). These results agree with the energy conversion values (also between \( 10^{-6} \) and \( 10^{-3} \)) found by Weichert et al. (1994) from \( M_s \) values for rockslides. They highlight the strong influence of nonlinear effects during the impact. In particular, the highly variable geotechnical site conditions of the impact zone (from soil to rock) probably explain the large variation of \( E_s/E_p \) ratios and the poor correlation between \( M_{rf} \) (or \( E_s \)) and the rock-fall characteristics \( H_f, V, \) and \( D_p \) (correlation coefficient \( R \) lower than 0.5, Fig. 7b,c,d).

All of the events where the rocks fell on a marly slope (\( R_1, R_5–R_9 \)) exhibit \( M_{rf} \) values below the regression line, resulting from the low coefficient of restitution of the slope sur-
face. Two data points ($R_3$ and $R_5$) are systematically far from the best regression line. $R_5$ is the first rock fall in a sequence of five events that occurred in the same place, and it shows an unexpected low-magnitude value, compared to the other events. It occurred in winter and the mass failed on a snow layer that could have absorbed a part of the energy, particularly on such a steep slope (65°). Event $R_3$ exhibits a relatively high magnitude for the values of fall height and runout (Fig. 7b,c). In Figure 7b, the vertical distance to the line could result from the initial sliding phase that contributed to the seismic energy and was not considered in the height-fall estimation. No explanation was found for the magnitude-runout graph that shows a very poor correlation. On the contrary, the signal duration $t_{30}$ exhibits a better correlation with the potential energy ($R = 0.69$, Fig. 7e) with the runout ($R = 0.61$, Fig. 7h) and to a lesser extent with the volume ($R = 0.47$, Fig. 7g). No correlation was found between the fall height $H_f$ and the ground-motion duration $t_{30}$ (Fig. 7f). Although limited in number, these results show that, contrary to earthquakes, the seismic energy derived from records cannot characterize rock falls. Alternatively, the signal duration $t_{30}$ is more promising. The good correlation between $t_{30}$ and $D_p$ indicates that the signal duration, which conveys information on the different phases of the failure process, is controlled by the propagation phase of the rock fall. As the runout distance increases with the rock-fall volume $V$ (Le-gros, 2002), correlations are also found between $t_{30}$ and the rock-fall characteristics $E_p$ and $V$. However, the limited number of events considered in this study does not allow us to propose quantitative relationships between these parameters, and these preliminary results should be validated in the future for a larger number of events. Because of the limited success of global seismic parameters for characterizing rock falls, we attempt to understand the different phases within the seismograms, using signal processing and 2D numerical modeling.

Spectrogram and Polarization Analysis

Rock-fall seismograms (Fig. 4) exhibit complex shapes with an irregular envelope and several energy pulses, probably resulting from the existence of multiple sources and
from the propagation of different waves. During an event
(Fig. 1), seismic waves are likely to be generated during
the initial slide and/or detachment of the block (elastic re-
bound), the impact on the ground, and the mass propagation.
As these seismic sources are all superficial, the energy is ra-
diated as both body and surface waves. In the following, we
attempt to identify distinct seismic phases in the seismo-
grams. Figure 8 shows the signals and the corresponding
spectrograms for three events (R1, R5, and R9) recorded
at two close stations. The spectrograms are calculated with
a sliding window of 2 sec and an overlap of 80%.

For the smallest event R1 (V = 2 × 10^4 m^3), the seis-
mogram recorded at station OG13 (Fig. 8a), along with the
spectrogram (Fig. 8b), clearly shows four distinct seismic
phases: the first P wave at 3 sec, a lower-frequency wave
(around 2 Hz) arriving about 3 sec later, a high-frequency
waves radiated during the detachment. On the other hand, the
impact associated with the initial rupture associated with an elastic rebound during the
departure of the mass.

However, the seismograms are globally more complex. On
the one hand, some features can be obscured by the super-
position of two seismic phases, depending on the relation
between the fall duration and the difference between the
propagation times of P and surface waves. This is observed
for the second record (station OG17, Fig. 8c) of event R1,
where P waves generated by the impact interfere with surface
waves radiated during the detachment. On the other hand,
the source mechanism for the two other greater rock falls R5 and
R9 is clearly more complex than the one proposed for R1, as
shown by the presence of energy pulses later in the signal
(Fig. 8e,g,i,k). In particular, the seismograms and spectro-
grams for rock fall R5 (V = 1 × 10^4 m^3) suggest a multifall
sequence and/or the generation of waves during the mass
propagation. However, the time shift between the source de-

energetic wave (2 Hz) 3 sec later, just before the signal
slowly begins to decrease. The time difference (6 sec) be-
tween the first onset and the second high-frequency wave
is compared to the theoretical fall duration D_f given by
the equation

\[ D_f = t_i - t_d = \sqrt{\frac{2 \times H_f}{g}}. \]  

where \( t_i \) is the impact time, \( t_d \) is the time of the mass detach-
ment, \( H_f \) is the fall height (170 m for R1), and \( g \) is the gravity
constant (9.81 m/sec^2). The computed fall duration (6.2 sec
for R1, see Table 3 and the solid line in Fig. 8) is consistent
with the observed time difference, supporting the existence
of at least two seismic sources: one corresponding to the ini-
tial rupture associated with an elastic rebound during the
detachment and the other generated at the rock impact on the
slope. In Figure 8a two solid vertical lines are drawn showing
the first onset time \( t_d \) and the impact time \( t_i \). The signal
associated with the impact has higher amplitude and higher fre-
cuency, compared to the one observed during the elastic
rebound phase (Fig. 8b). In the same figure vertical dashed
lines are also shown with the theoretical times \( t_d S \) and \( t_i S \)
of the surface waves generated during the mass detachment and
impact, estimated from the seismic model used for earth-
quake location (Paul et al., 2001).

Computed times are given in Table 3, along with fall-
height values and epicentral distances. The fit between these
theoretical times and the two observed low-frequency wave
arrivals is excellent, supporting the interpretation that the
four main seismic phases observed in the seismogram are
due to the generation of P and surface waves during the det-
achment and the impact of the mass.

A similar analysis was made on the other five couples of
seismograms and spectrograms, and the four theoretical
times are indicated in the same way in Figures 8c–8l. These
times are usually associated with energy pulses exhibiting
frequency variations consistent with the impact (high fre-
cuency) or with the arrival of surface waves (low frequency).
However, the seismograms are globally more complex. On
the one hand, some features can be obscured by the super-
position of two seismic phases, depending on the relation
between the fall duration and the difference between the
propagation times of P and surface waves. This is observed
for the second record (station OG17, Fig. 8c) of event R1,
where P waves generated by the impact interfere with surface
waves radiated during the detachment. On the other hand,
the source mechanism for the two other greater rock falls R5 and
R9 is clearly more complex than the one proposed for R1, as
shown by the presence of energy pulses later in the signal
(Fig. 8e,g,i,k). In particular, the seismograms and spectro-
grams for rock fall R5 (V = 1 × 10^4 m^3) suggest a multifall
sequence and/or the generation of waves during the mass
propagation. However, the time shift between the source de-

\begin{table}
\centering
\begin{tabular}{|c|c|c|c|c|}
\hline
Event & \( \alpha_1 \) & 95% PI & \( \alpha_2 \) & 95% PI \& \( t_d \) (s) \\
\hline
R1 & -0.09 & \pm 3.1 & 0.85 & \pm 1.01 & 16.6 \\
R2 & 1.60 & \pm 0.68 & 0.37 & \pm 0.18 & 17.7 \\
R4 & 2.09 & \pm 1.71 & 0.29 & \pm 0.5 & 21.3 \\
R5 & 2.07 & \pm 3.13 & 0.35 & \pm 1.08 & 26.2 \\
R6 & 1.55 & \pm 3.13 & 0.42 & \pm 0.12 & 19.6 \\
R7 & 2.74 & \pm 0.46 & 0.1 & \pm 0.32 & 22.1 \\
R8 & 1.7 & \pm 1.12 & 0.35 & \pm 0.34 & 18.0 \\
R9 & 1.41 & \pm 1.00 & 0.41 & \pm 0.26 & 16.7 \\
All events & 1.82 & \pm 0.35 & 0.33 & \pm 0.09 & 19.4 \\
\hline
\end{tabular}
\caption{Regression Parameters \( \alpha_1 \) and \( \alpha_2 \) of Equation (3)}
\end{table}

Regression parameters with their corresponding 95% prediction interval (PI) computed for the eight valuable rock falls (see text for details) and corresponding \( t_d \) values.
ing-amplitude part of the signal is controlled by the propagation phase, as shown by the relation between the signal duration and the runout distance.

In order to validate the interpretation of $P$ waves and surface waves, wave polarization analyses were carried out on the available three-component stations. Figures 9 and 10 show the seismograms recorded at station OG14 and the particle motions for the rock falls $R_5$ and $R_9$, respectively. The polarization analysis was performed on short time windows (0.5–1.5 sec, according to the wave period) at the arrival

Figure 7. Comparison between ground-motion characteristics (rock-fall seismic magnitude $M_{rf}$, seismic energy $E_s$, and duration $t_{30}$) and rock-fall parameters (potential energy $E_p$, fall height $H_f$, volume $V$, runout $D_p$). $R$ is the correlation coefficient of the linear regression analysis (solid black lines) (see text for details).

Figure 8. Vertical-component signals (top) and corresponding spectrograms (bottom) for the $R_1$ (a)–(d), $R_5$ (e)–(h), and $R_9$ (i)–(l) events recorded at two different stations. The first solid line shows the $P$ wave generated during the initial rupture ($t_d$) while the second indicates the theoretical impact time after the fall ($t_i$) computed with equation (5). Dashed lines show the surface-wave arrival times for the two sources ($t_{ds}$ and $t_{is}$ for the first and second source, respectively).
times \( (t_d, t_i, t_{dS}, \text{and} \ t_{iS}) \) of the four identified waves. At \( t_d \) and \( t_i \) times (Figs. 9b,d and 10b,d), the particle motions have the characteristics of a \( P \) wave, mainly vibrating along a particular direction in the radial vertical plane, with an incidence angle between \( 45^\circ \) and \( 60^\circ \). At \( t_{dS} \) and \( t_{iS} \) times (Figs. 9c,e and 10c,e), the particle motions clearly exhibit an elliptical polarization typical of surface waves with, however, a difference in the polarization direction. For both rock falls, surface waves generated during the detachment (Figs. 9c and 10c) are Rayleigh-type waves polarized in the propagation plane, consistently with the approximation of the elastic rebound by a vertical force. On the contrary, the surface waves radiated at the time of the impact also include Love-type waves with a significant tangential component (Figs. 9e and 10e), particularly for event \( R9 \). Both rock falls moved in a direction perpendicular to the line linking the events to the station OG14 (Fig. 2). As the slope at the impact area is greater than \( 50^\circ \) for the two events, a near-vertical impact then induces a strong

![Figure 9.](image-url)
parallel-to-the-surface shear force, which generates Love-type surface waves at station OG14. Additional Love-type waves are also observed in the later part of the signals (not shown) and could result from the shearing due to the sliding mass if the movement evolves to a rock avalanche. Unfortunately, no three-component station was located in the propagation plane to show the generation of Rayleigh waves in this plane during the impact.

In conclusion, polarization analysis on three-component stations confirms the types of waves detected in the seismogram and spectrogram study, showing the existence of at least two seismic sources in the rock-fall records. The first, which is probably due to the rupture and detachment phases, generates nonimpulsive P waves, while the second, which is interpreted as resulting from the impact, generates higher frequency and more energetic waves. The seismic characteristics of these two phenomena are studied using 2D numerical simulations.

### Numerical Modeling

We simulate the fall of a rectangular block detaching from a cliff along a vertical plane (Fig. 11a). The size of the block is $40 \times 80$ m and the fall height is 170 m. The explicit 2D dynamic finite-element code Plast2 (Baillet et al., 2005; Baillet and Sassi, 2006) is used to simulate detachment, frictional contact, fall, and impact. The motion equation is both spatially and temporally discretized by using the finite-element method and the $\beta_2$ explicit time integration scheme (Carpenter et al., 1991), respectively. In order to ensure stability, the explicit scheme satisfies the usual Courant-Friedrichs-Levy condition ($\Delta t \leq \xi (h/c)_{\text{min}}$), where $\Delta t$ is the timestep, $h$ is the element size, $c$ is the wave speed, and $\xi$ is a positive constant ($\xi < 1$, $\xi \approx 0.5$ in most practical purposes). Correct wave propagation is obtained by using 10 finite elements per wavelength (Mullen and Belytschko, 1982) with the absorbing boundary conditions proposed by Stacey (1988). Computations were made with 89,000 quadrilateral finite elements with an element size of 5 m.

The code Plast2 considers large strains, large displacements, and large rotations, as well as nonlinear material behavior. Contact nonlinearity (block/cliff interface) is taken into account by using the forward increment Lagrange multiplier method (Carpenter et al., 1991) that enables the evaluation of the normal and tangential contact stresses, as well as the determination of whether the contact surfaces locally stick, slip, or separate. The contact algorithm uses slave nodes on the block and target surfaces on the cliff. An elementary target surface defined by two nodes is broken down into a Ferguson patch with continuously differentiable adja-
cent boundaries (Faux and Pratt, 1979). A model coupling unilateral contact condition, Coulomb friction (constant coefficient), and adhesion (Raous et al., 1999) is used for computing the contact stresses and displacements at each iteration. The intensity of adhesion is characterized by an internal variable \( \beta \) with \( \beta = 1 \) for total adhesive interface and \( \beta = 0 \) for contact without adhesion.

First, the seismic signals generated during the block detachment are computed at two points A and B located at about 375 m from the cliff (Fig. 11a) on the lower and upper surfaces. The block and the cliff are supposed to be elastic (\( P \)-wave velocity \( V_p = 5820 \) m/sec, \( S \)-wave velocity \( V_s = 3112 \) m/sec, and density \( \rho = 2700 \) kg/m\(^3\)). Thus, the impact of the detached stiff elastic block is simulated for three rheological conditions of the ground, which are given in Table 4. In the first case, the ground is elastic with the same characteristics as the block. In the second case, the ground is still elastic but softer (\( V_p = 1700 \) m/sec, \( V_s = 909 \) m/sec, and \( \rho = 1500 \) kg/m\(^3\)) in order to simulate the impact conditions of a limestone block on a marl layer or on scree deposits. In the third case, we use an elastoplastic law for simulating the nonlinear behavior of the ground. For the marl characteristics, the values given by Eberhardt et al. (2005) have been taken (\( c = 65 \) KPa and \( \Phi = 35^\circ \)). Here,
we chose to use Von Mises criterion, with a corresponding elastic limit in compression of 288 KPa.

The seismic signals generated during the detachment at the two points A and B in the 0–20 Hz frequency range are shown in Figure 11b,c, respectively. They both exhibit a sharp signal, with a greater amplitude at point B (upper surface) than at point A (lower surface). This difference, which results from the difference of distance due to the cliff height and from the scattering on the edges, should attenuate at large distance when the cliff height becomes negligible. In the following, we will consider the signal on the lower surface (point A) for comparing it to the seismograms due to the impact. The signals generated by the detachment of two blocks with different sizes (20 × 40 and 40 × 80 m) are shown in Figures 11d,e, respectively, as well as the corresponding spectrograms (Fig. 11i,j). For the 40 × 80-m block, the signal and the spectrogram show a maximum energy at very low frequency (below 2 Hz) with a permanent displacement due to the elastic rebound of the cliff after the block detachment (t > 0.2 sec). For the 20 × 40-m block, this effect is less visible and the maximum energy is shifted to a higher frequency in relation with the size of the block. The signals generated by the impact at point A for the three rheological conditions of the ground (Table 4) are plotted in Figure 11f,g,h, along with the corresponding spectrograms (Fig. 11k,l,m). The difference of time between the detachment and the impact events corresponds to the fall duration (about 5.8 sec).

In the two elastic cases (Fig. 11f,g), the waves generated during the impact are 200–350 times greater than those radiated during the detachment (these figures have to be divided by two if we consider point B for the detachment). P wave is better distinguished from Rayleigh wave for the soft elastic medium (case 2) due to the lower propagation velocities. In the spectrograms, the signal on the elastic stiff ground (Fig. 11f) exhibits Dirac-like characteristics with energy spread over the whole frequency range (Fig. 11k), while in the soft elastic case, the energy is more concentrated between 1 and 10 Hz (Fig. 11l). Although the synthetic signals are simulated at a small distance from the source, these results agree with the observations made on the real seismograms, that the signal associated to the impact has higher amplitude and a higher frequency, compared to the one observed during the detachment phase. However, the real amplitude difference is not as high as the one simulated, and a ground plastic behavior is tested in order to evaluate the nonlinear effect on the wave characteristics (Fig. 11h,m).

The introduction of plasticity in the ground with soft elastic characteristics dramatically decreases the impact amplitude by a factor of 100 and strongly affects the spectral energy that concentrates below 5 Hz. The signal generated during the impact still exhibits greater amplitude (2–3.5) than the one due to the detachment, with a lower ratio range. This ratio is comparable to the one observed on measured seismograms (compare Figs. 8 and 11). Even with a simple plastic law, these numerical results explain some of the main characteristics of observed seismograms and highlight the strong influence of ground nonlinear behavior on the waves generated during the impact. The consequence is that frequency content and amplitude of the impact-related part of the signal cannot be used for extracting information on the fallen block or on the rupture mechanism. That analysis has to be focused on the early part of the seismograms, linked to the detachment phase, which shows spectral variations with the block size at low frequency.

Conclusions

We analyzed seismograms recorded during rock falls in the western Alps by the French permanent seismological network Sismalp with the aim of getting new information on the rock-fall mechanism. We used records of 10 known events that occurred between 1992 and 2001. The study of the peak ground motions showed that the regional attenuation relation used for earthquakes is inappropriate for rock falls. A new empirical attenuation relation for rock-fall-induced motions was derived from the dataset, allowing a rock-fall seismic magnitude to be attributed to each event. In agreement with previous works, the comparison between the seismic energy

### Table 4

Dynamic Characteristics of the Block and the Ground in the Three Simulation Cases

<table>
<thead>
<tr>
<th>Case Number</th>
<th>Elastic Block and Cliff Characteristics</th>
<th>Elastic Ground Properties</th>
<th>Plastic Ground Properties</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>V_p = 5820 m/sec V_s = 3112 m/sec</td>
<td>V_p = 5820 m/sec V_s = 3112 m/sec</td>
<td>—</td>
</tr>
<tr>
<td></td>
<td>ρ = 2.7</td>
<td>ρ = 2.7</td>
<td>—</td>
</tr>
<tr>
<td>2</td>
<td>V_p = 5820 m/sec V_s = 3112 m/sec</td>
<td>V_p = 1700 m/sec V_s = 909 m/sec</td>
<td>—</td>
</tr>
<tr>
<td></td>
<td>ρ = 2.7</td>
<td>ρ = 1.5</td>
<td>—</td>
</tr>
<tr>
<td>3</td>
<td>V_p = 5820 m/sec V_s = 3112 m/sec</td>
<td>V_p = 1700 m/sec V_s = 909 m/sec</td>
<td>σ_y = 348(2.10^{-3} + ε^p)^0.03</td>
</tr>
<tr>
<td></td>
<td>ρ = 2.7</td>
<td>ρ = 1.5</td>
<td>σ_y(ε^p=0) = 289 Kpa</td>
</tr>
</tbody>
</table>

V_p and V_s are the P-wave and S-wave velocities, ρ is the density, σ_y is the yield strength (Von Mises criterion), and ε^p is the equivalent plastic strain.
and the potential energy released during rock falls showed that only a very small amount (between 10⁻⁶ and 10⁻³) of the fall energy is transmitted as seismic waves. It highlights the effect of nonlinear processes (friction, cracking, plastic deformation) that probably explains the very poor correlation found between the seismic magnitude $M_{\text{et}}$ (or $E_i$) and the rock-fall characteristics $H_f$, $V$, and $D_p$. These results imply that, contrary to earthquakes, the peak ground amplitude, dominated by the impact source, is not a good parameter for characterizing rock falls. On the other hand, we showed that the signal duration was correlated to the runout distance, thus confirming the role played by the propagation phase on this characteristic of the seismogram. As the Sismalp network is equipped with short-period seismometers, it can only be concluded that the corner frequency $f_0$ is close to or below 1 Hz for the investigated rock falls. Another step forward for a more detailed study of the rock-fall dynamic mechanism would be to remove the propagation effects from the seismic records, using blind deconvolution methods (Liao and Huang, 2005; Sèbe et al., 2005).

Signal and particle-motion analyses pointed out the complexity of the seismograms, with the arrival of at least two $P$-wave trains and two surface-wave trains. We linked these seismic phases to two distinct sources: the rupture process, which generates an elastic rebound on the one hand, and the waves radiated during the impact following the fall on the other hand. The fall phenomenon might include other complex processes (fragmentation of the falling mass and interaction with the topography during the fall). However, preliminary 2D elastic and plastic numerical results retrieved the major spectral and amplitude characteristics of the rock-fall records. In particular, they highlighted the major effect of the plastic deformation on waves generated during the impact. Our numerical results also showed an influence of the block volume on the low-frequency content of the waves, suggesting that the first $P$-wave train could be used for characterizing rock falls if high-quality broadband seismometer records were available.

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References


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