

# Seismic Anisotropy

## Monitoring of Seismogenic and Volcanic zones

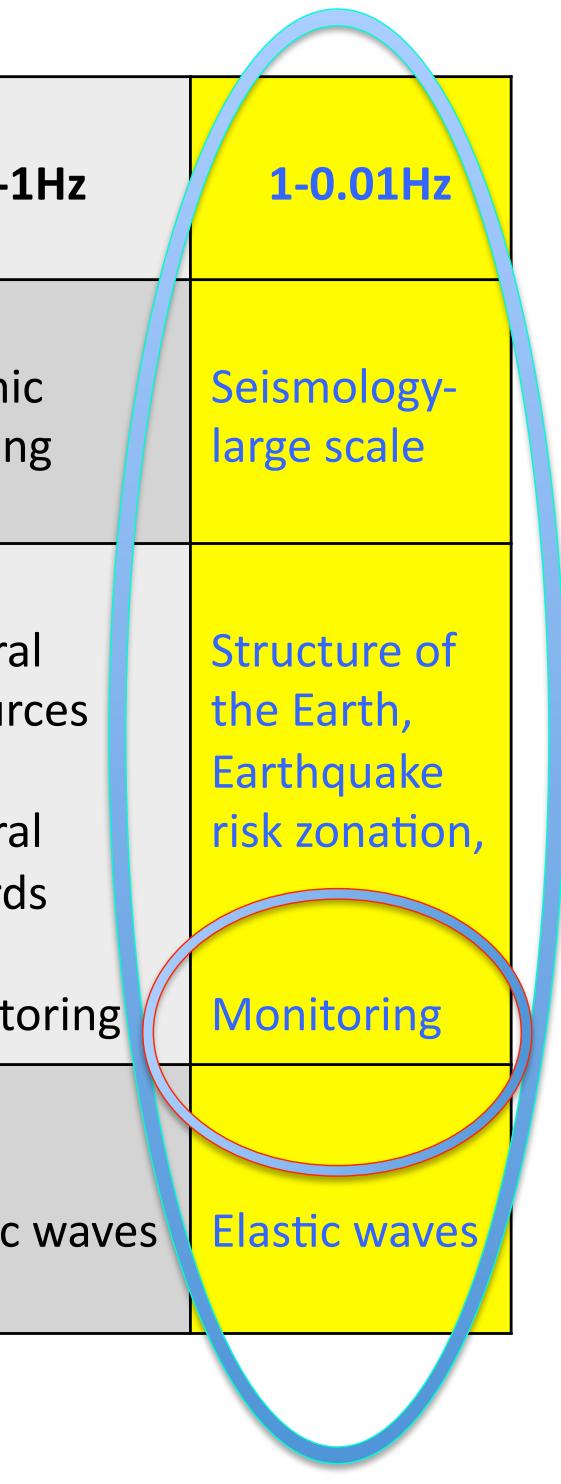
Jean-Paul Montagner

**Maria Saade**, Philippe Roux, Florent Brenguier,  
Edouard Kaminski, Stéphanie Durand, Yanick Ricard,  
Kohtaro Araragi, Yosuke Aoki, Paul Cupillard

...

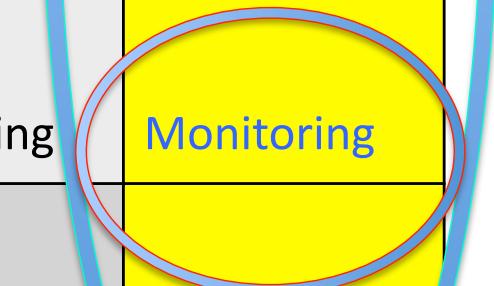
IPG-Paris, ISTerre-Grenoble, U. Nancy, ENS-Lyon, ERI-Tokyo

Frequency	Mhz-kHz	10000-100Hz	100-10Hz	10Hz-1Hz	1-0.01Hz
Domain	Laboratory acoustics	Underwater acoustics	Shallow seismic imaging	Seismic imaging	Seismology-large scale
Applications	NDT	Tomography Source detection	Structure of shallow layers Geotechnical applications, land slides	Natural resources Natural hazards	Structure of the Earth, Earthquake risk zonation,
	Monitoring		Monitoring	Monitoring	Monitoring
Wave type	Acoustic/ elastic waves	Acoustic waves	Elastic waves	Elastic waves	Elastic waves



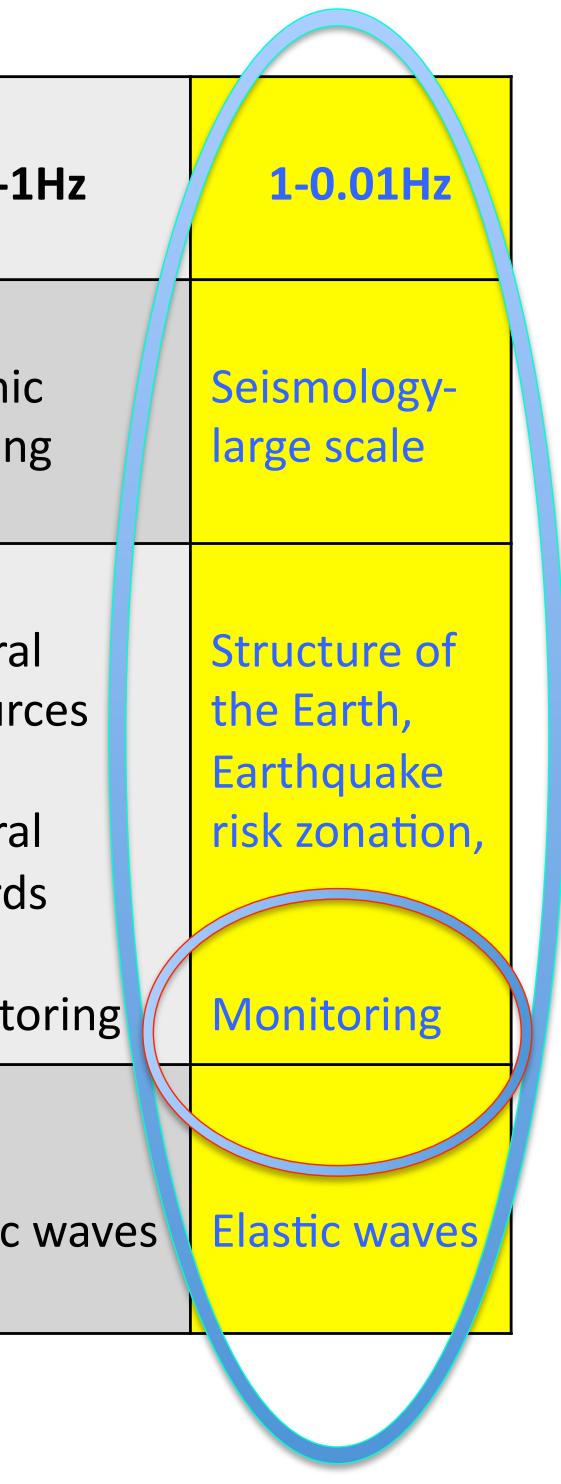
1-0.01Hz

Seismology-large scale

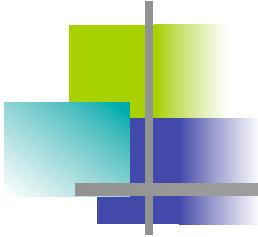


Structure of the Earth, Earthquake risk zonation,

Monitoring



Elastic waves



# OUTLINE

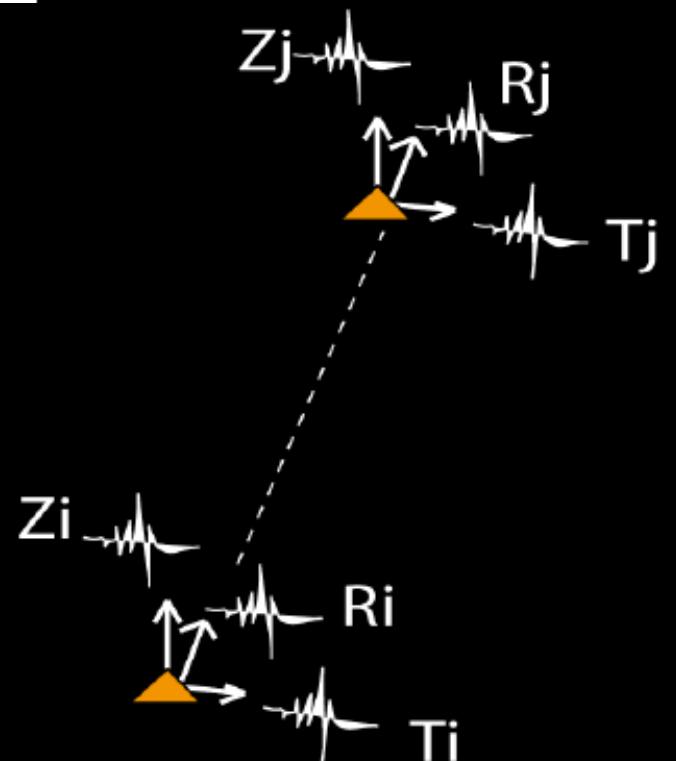
- **Data driven field: Seismic Data**
- **Cross-correlation tensor: Seismic Anisotropy?**
- **Seismic Anisotropy: many processes**
  
- **Scientific Issues:**
  - 3D- Anisotropic Structure of the Earth  
Upper mantle – LAB
  - Seismic monitoring:
    - Temporal changes of anisotropy in
      - seismogenic zones (Northern Honshu – Japan)
      - volcanic zones (Mt Fuji)

Cross-correlation tensor  $C_{ij}$   
 for 2 stations i, j and 3 components k, l  
 Seismic signals  $S_{ik}(t), S_{jl}(t)$

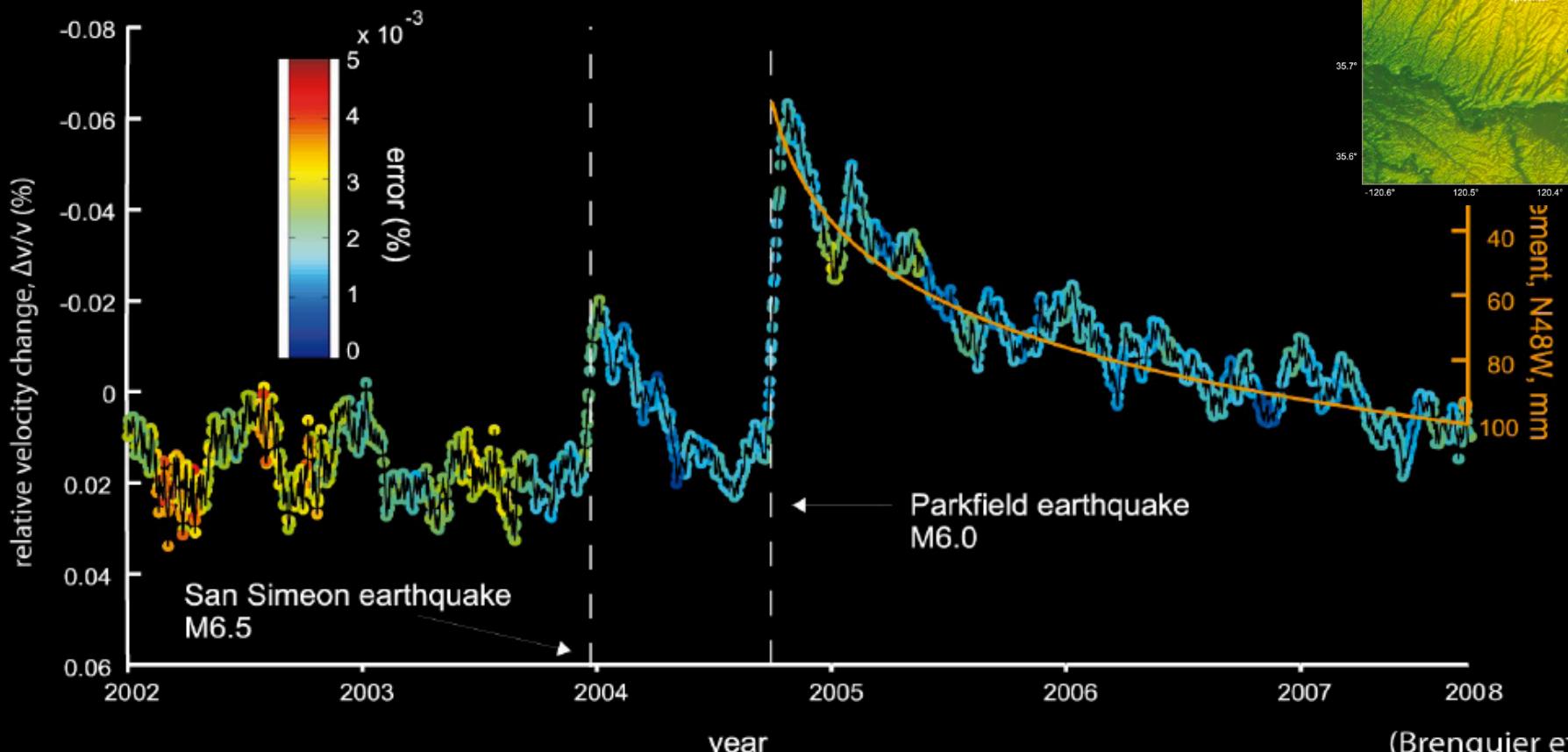
$$[C_{ij}(t)]_{kl} = \frac{\int_0^T S_{ik}(\tau) S_{jl}(t + \tau) d\tau}{\sqrt{\int_0^T S_{ik}^2(\tau) d\tau \int_0^T S_{jl}^2(\tau) d\tau}},$$

<b>ZZ</b>	<b>ZR</b>	<b>ZT</b>
<b>RZ</b>	<b>RR</b>	<b>RT</b>
<b>TZ</b>	<b>TR</b>	<b>TT</b>

Brenguier et al., 2008

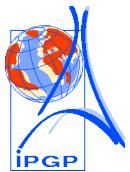


# Parkfield High Resolution Seismic Network (HRSN)

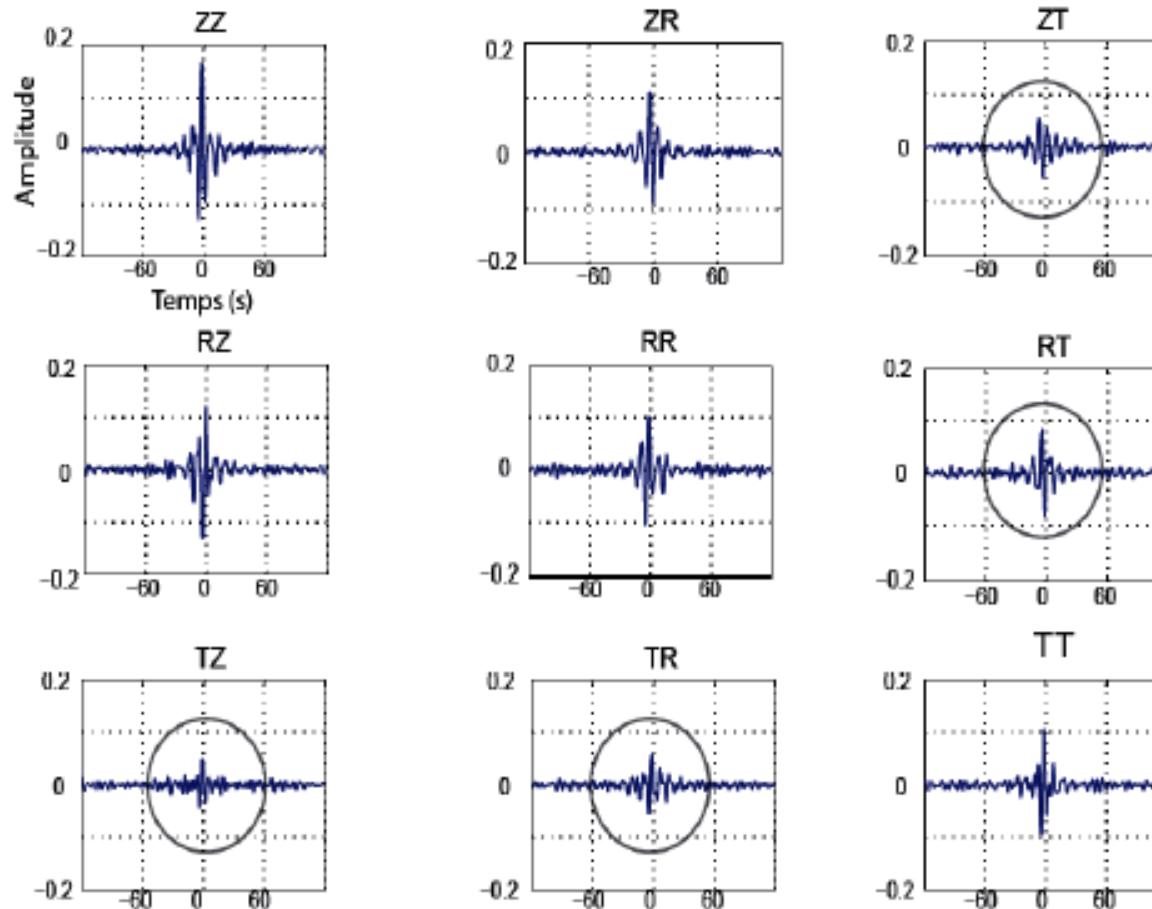


ZZ: Co-seismic and post-seismic relative velocity change  
(Brenquier et al., 2008)

# Example of cross-correlation tensor



## Parkfield HRSN – Stack (30days)

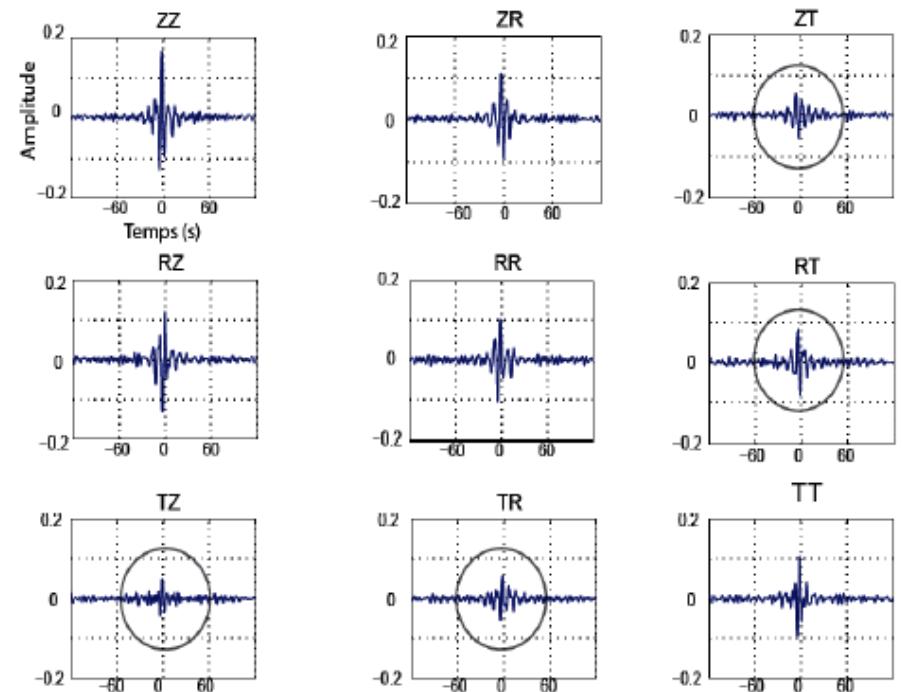


$TZ, TR, ZT, RT \neq 0$

# How can we explain the off-diagonal terms of the cross-correlation tensor?

$TZ, TR, ZT, RT \neq 0$

- Non uniform distribution of seismic noise sources?
- Lateral heterogeneities of Velocities?
- Seismic anisotropy?**

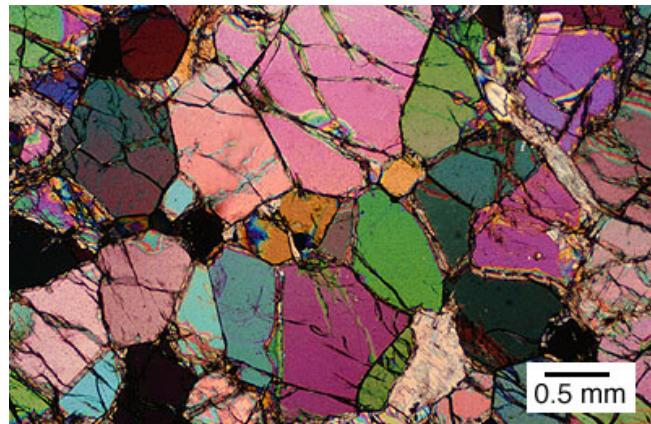


# To explain seismic data: heterogeneities isotropic / anisotropic, anelasticity

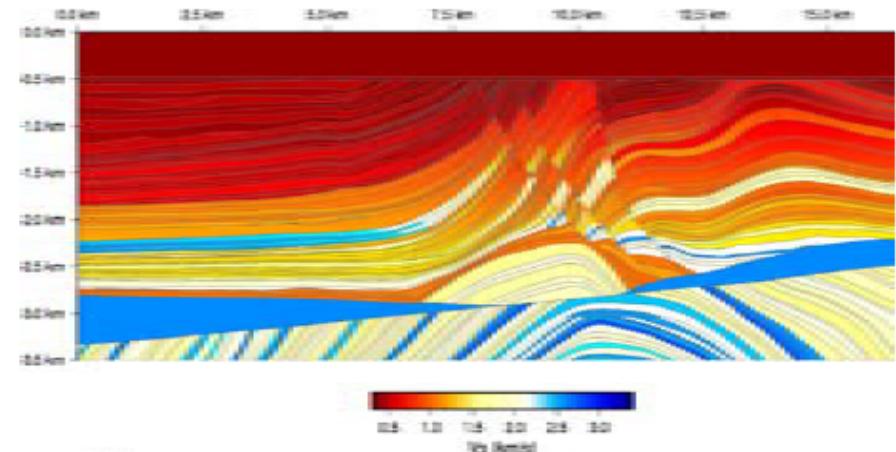
Confusion:      Heterogeneity  $\neq$  Anisotropy

-Homogeneous, anisotropic  
(Olivine aggregates)

-Heterogeneous, isotropic

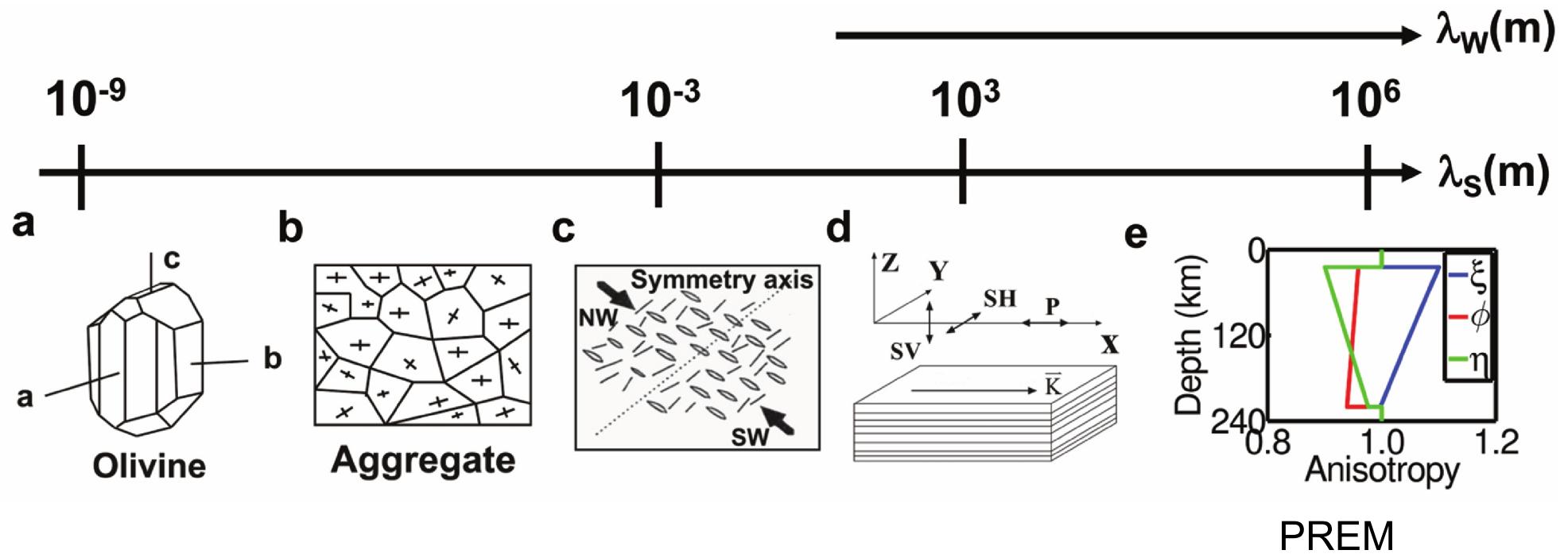


Marmousi



Solid Earth: heterogeneous + anisotropic + anelastic

# Seismic Anisotropy at all scales



PREM

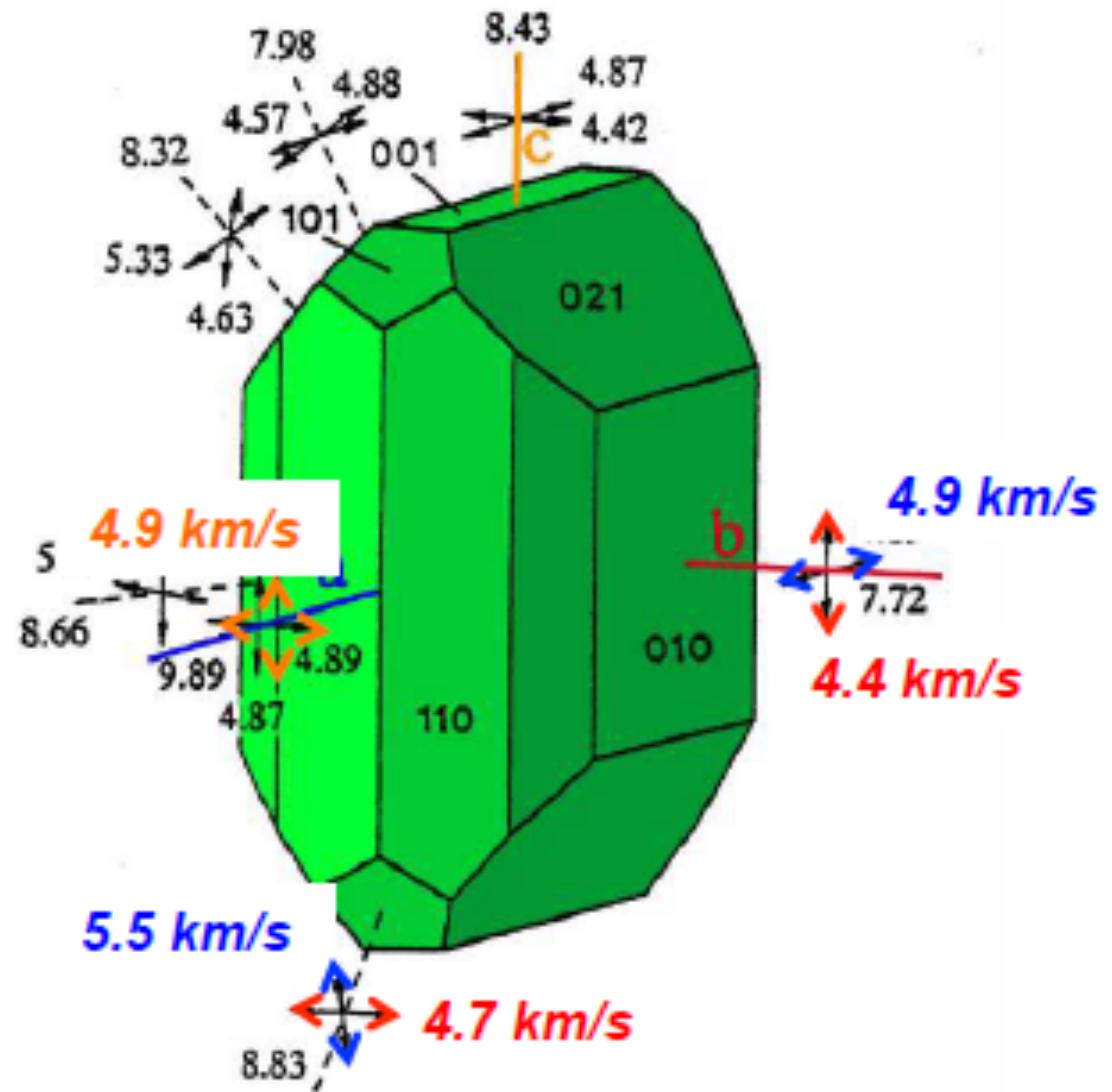
PREM: radial anisotropy: up to 10%

$\lambda_W$  seismic wavelength

$\lambda_S$  spatial scale

(Wang et al., 2013)

# Olivine : 20% anisotropy

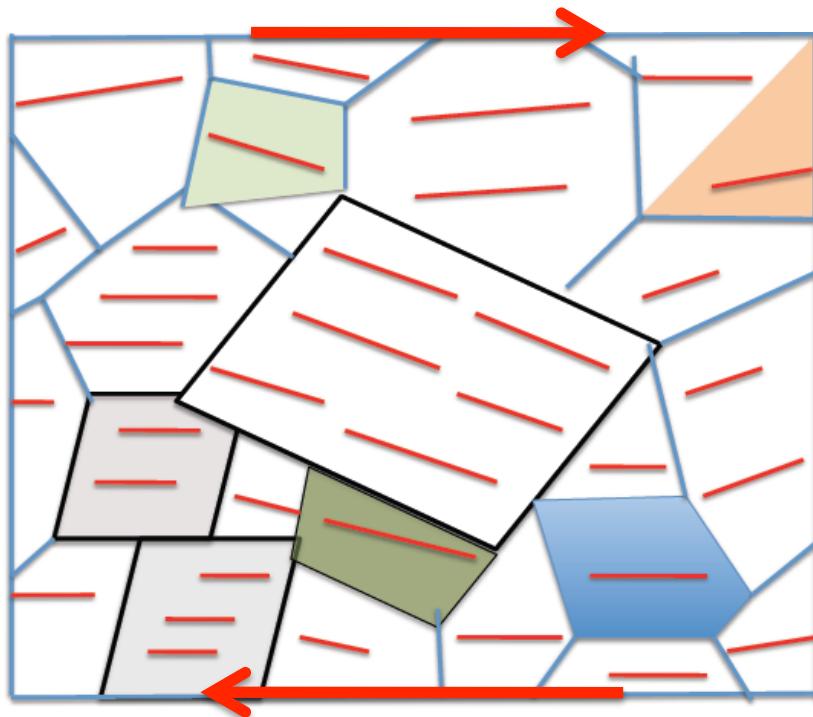


Coherent Strain field (convective process)  
(L.P.O.: lattice preferred orientation)

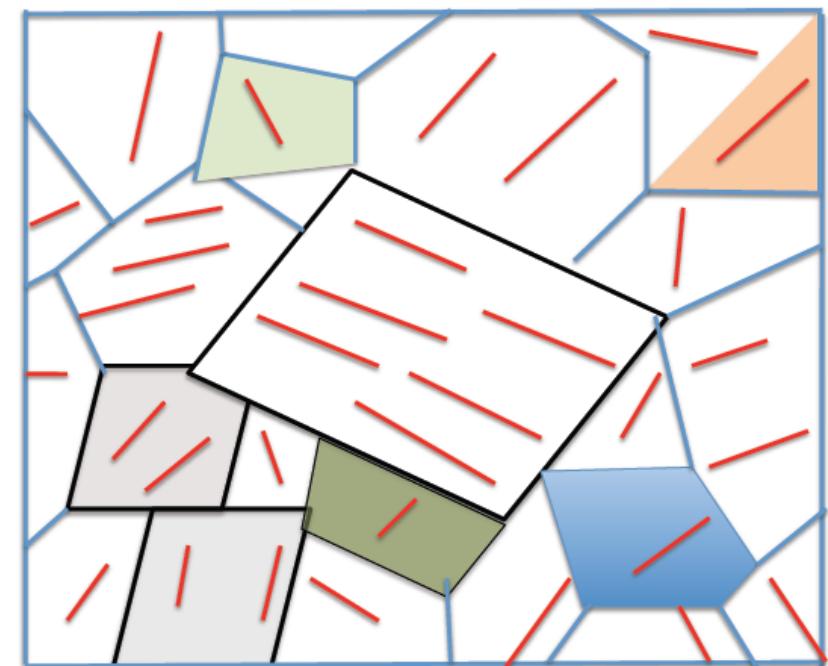
Incoherent Strain field  
(random orientation)

Large-scale Seismic anisotropy  $\neq 0$

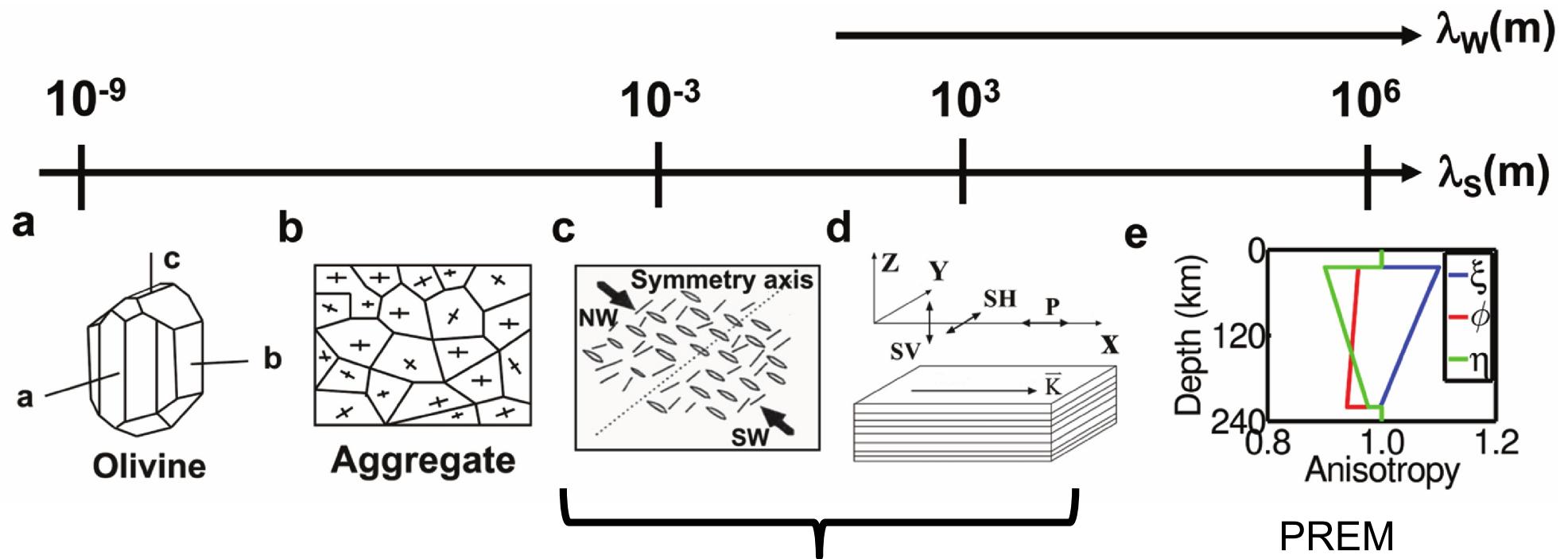
Large-scale Seismic anisotropy  $\approx 0$



Inner Organization



# Seismic Anisotropy at all scales



PREM: radial anisotropy: up to 10%

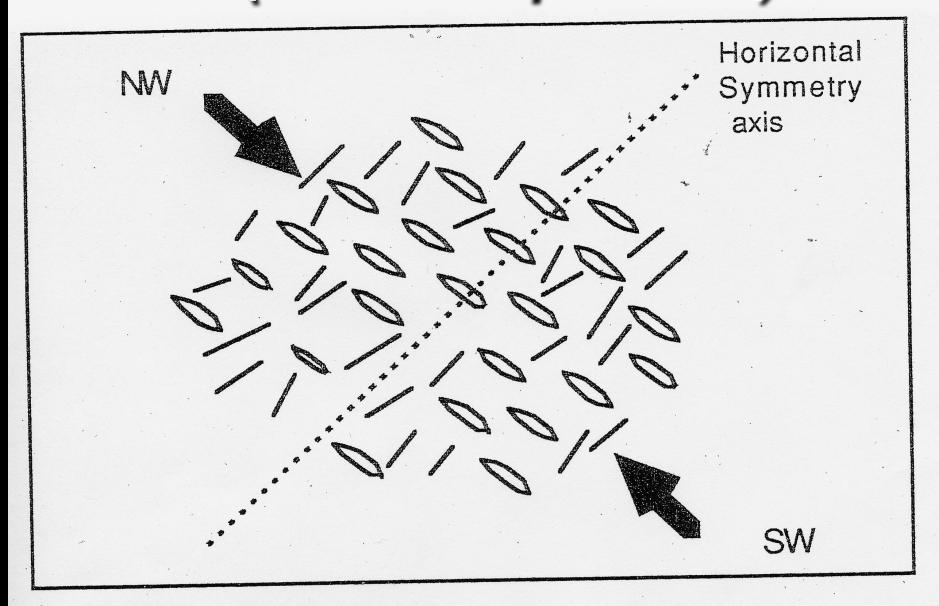
$\lambda_W$  seismic wavelength

$\lambda_S$  spatial scale

(Wang et al., 2013)

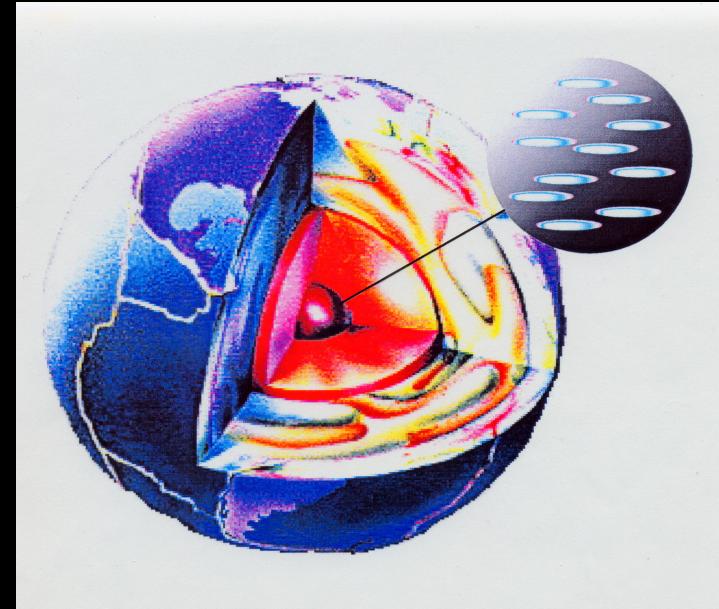
# S.P.O.: Shape Preferred Orientation Cracks, fluid inclusions, ... (Stress field)

*Crust (+lithosphere)*



(Babuska and Cara, 1991)

*Inner core*



(Singh et al., 2001)

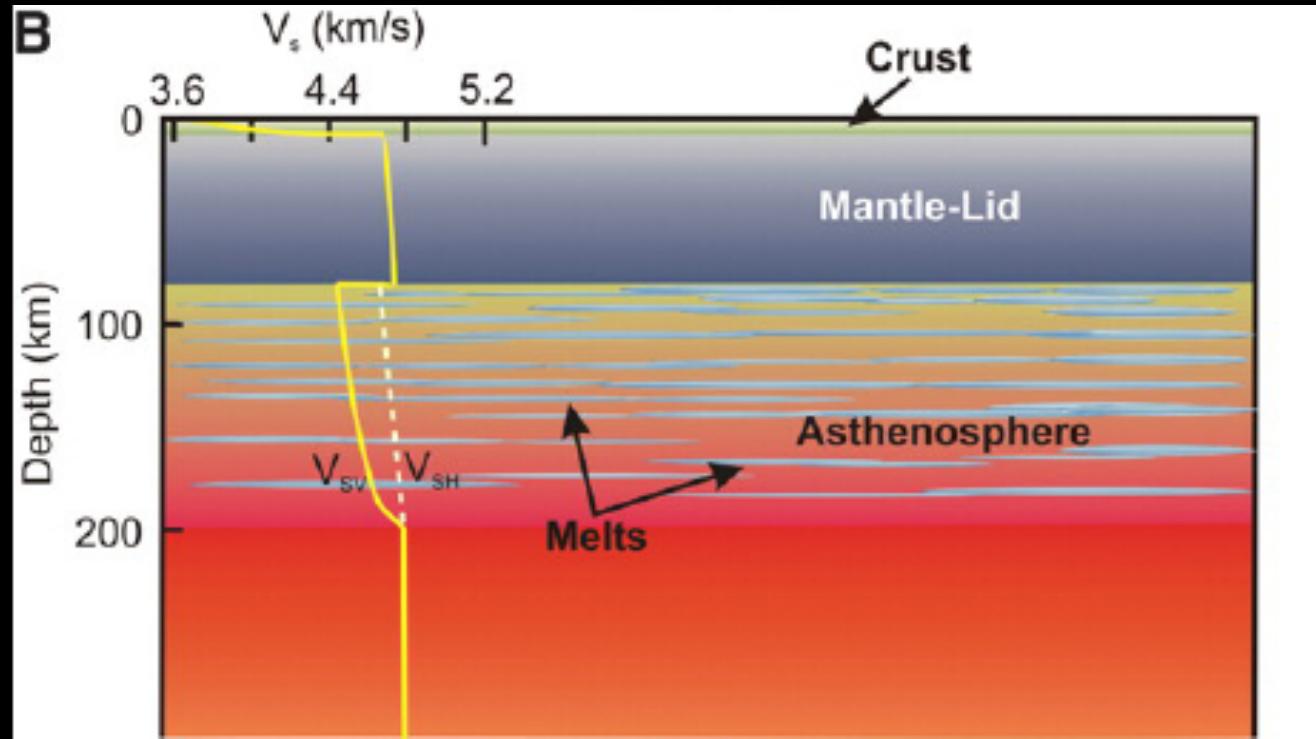
→ **STRESSMETER**

*Temporal variations of anisotropy?*

**Monitoring of cracked, fractured zones**

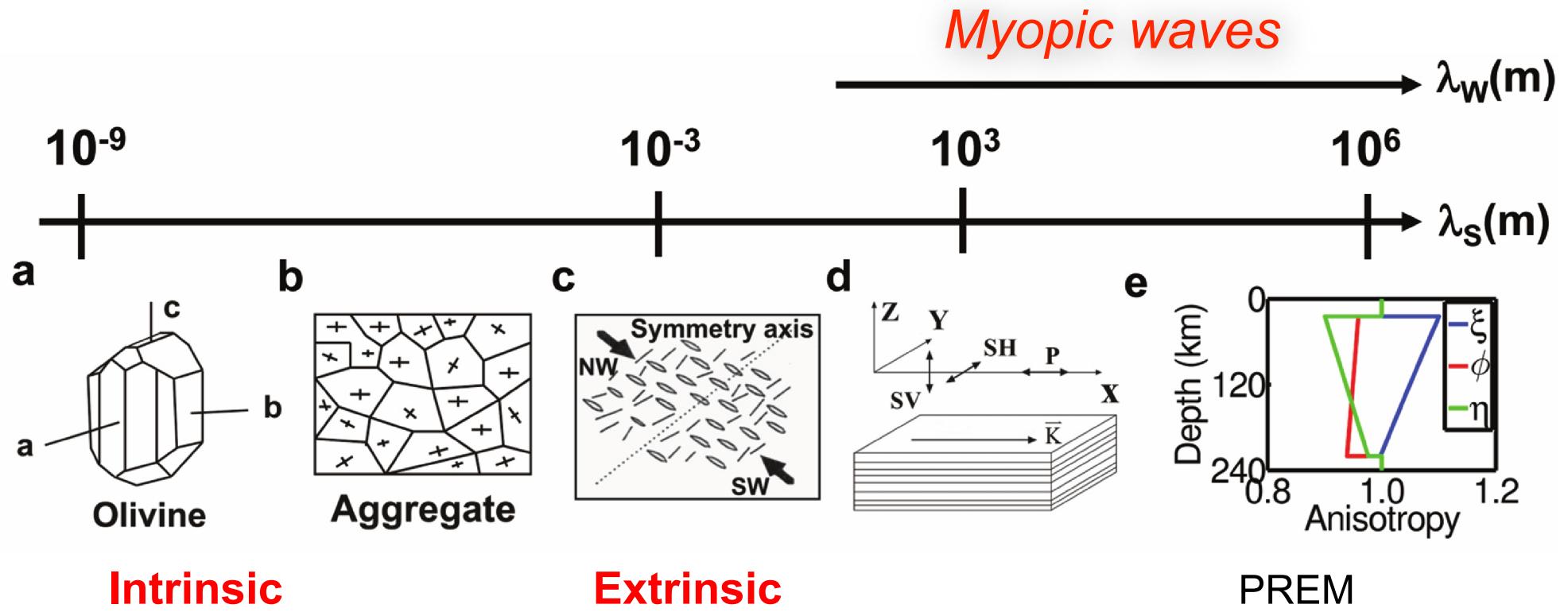
*(seismogenic zones: Durand et al. 2011; Saade et al., 2014, 2017)*

# FINE LAYERING: Stratification Anisotropy Mille-feuilles model (partial melting)



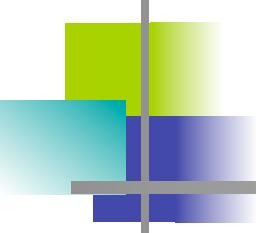
→ *Effective medium*  
*Radial anisotropy (Kawakatsu et al. 2009)*  
*V.T.I. Vertical Transversely Isotropic medium:*  
*5 parameters*  
 $(A=\rho V_{PH}^2, C=\rho V_{PV}^2, F, L=V_{SV}^2, N=V_{SH}^2)$

# Seismic Anisotropy at all scales



Observed (apparent) anisotropy  
 Intrinsic versus Extrinsic anisotropy  
 $\alpha = p\alpha^{\text{int}} + (1-p)\alpha^{\text{ext}}$

NOT A SECOND ORDER EFFECT, different interpretations



# Wave propagation in anisotropic medium

- Isotropic medium

$$\rho \frac{\partial^2 u_i}{\partial t^2} = \lambda \frac{\partial \Theta}{\partial x_i} + \mu \frac{\partial}{\partial x_j} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$$

Where  $\mathbf{u}$  is seismic displacement,  
 $\lambda$  and  $\mu$  Lamé parameters  
 $\Theta = \nabla \cdot \mathbf{u}$

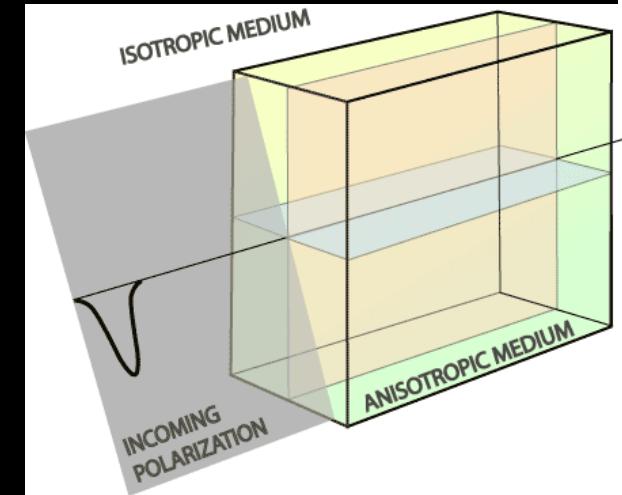
- Anisotropic medium

$$\rho \frac{\partial^2 u_i}{\partial t^2} = \frac{1}{2} \gamma_{ijkl} (u_{k,lj} + u_{l,kj})$$

$\gamma_{ijkl}$  4th-order elastic tensor

# Different kinds of anisotropy effects on seismic waves

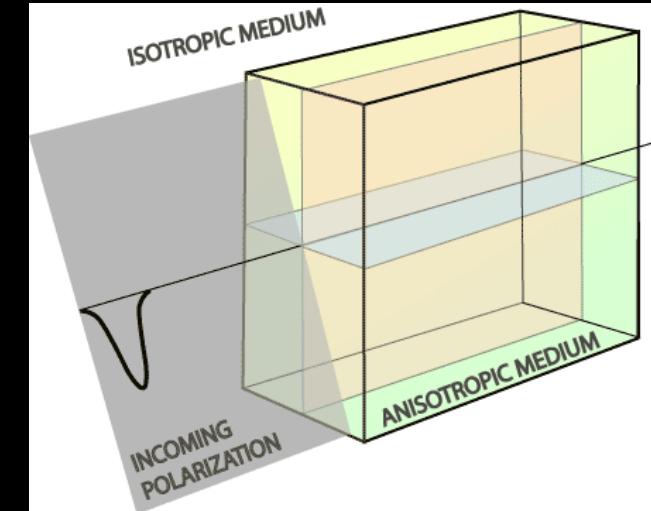
- Body waves: Shear wave splitting (birefringence)



Courtesy of Ed. Garnero

# Different kinds of anisotropy effects on seismic waves

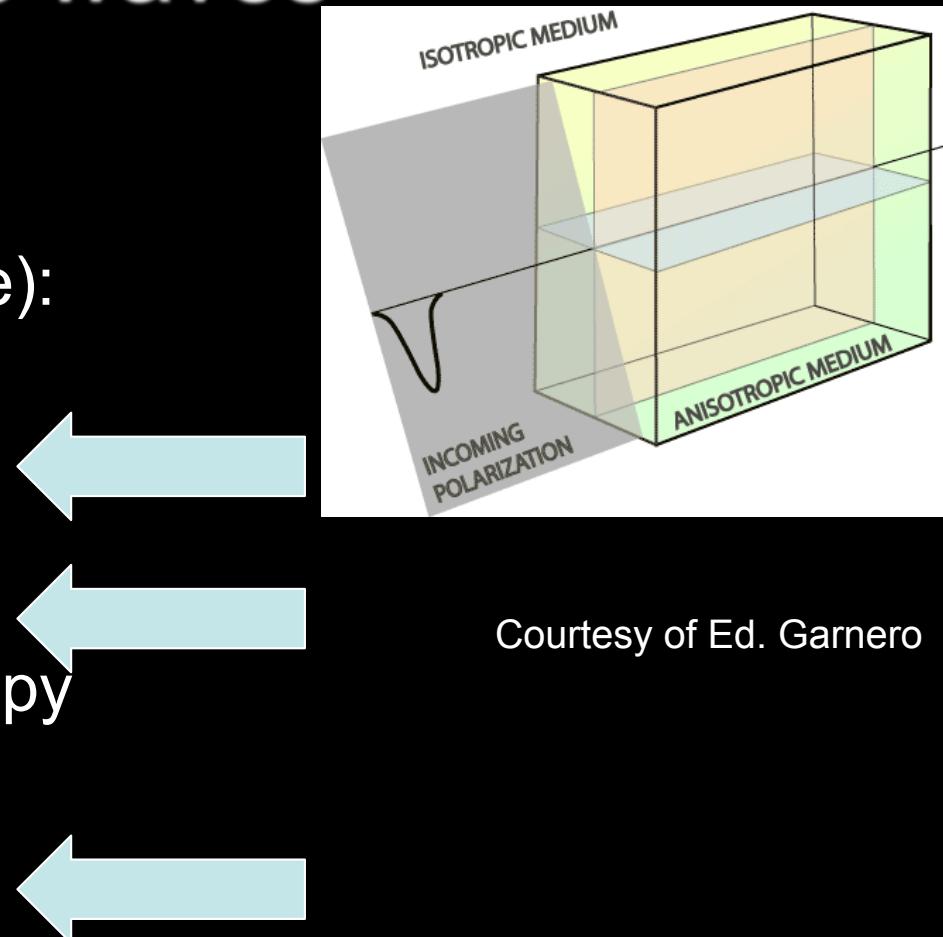
- Body waves: Shear wave splitting (birefringence)
- Surface waves (Rayleigh and Love):
  - Rayleigh-Love discrepancy
  - Azimuthal variations of phase (or group) velocities, radial anisotropy
  - Quasi-Rayleigh, Quasi-Love polarization anomalies



Courtesy of Ed. Garnero

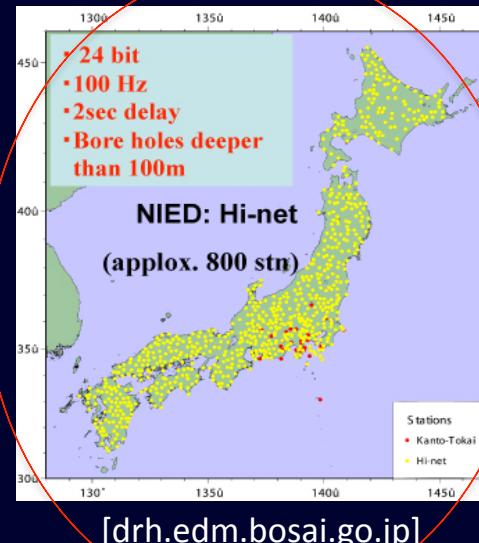
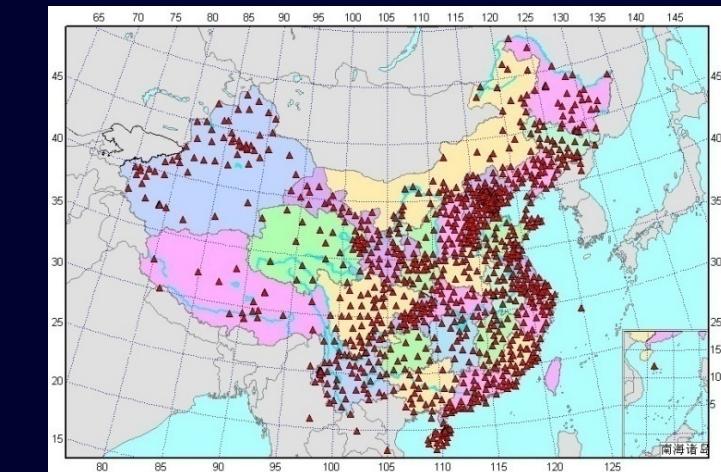
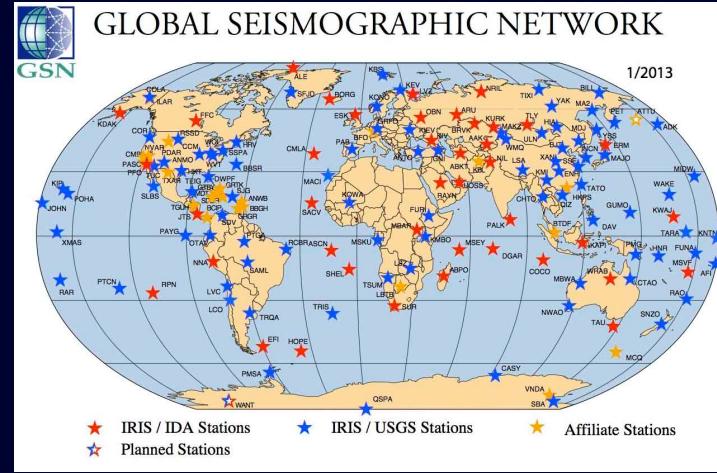
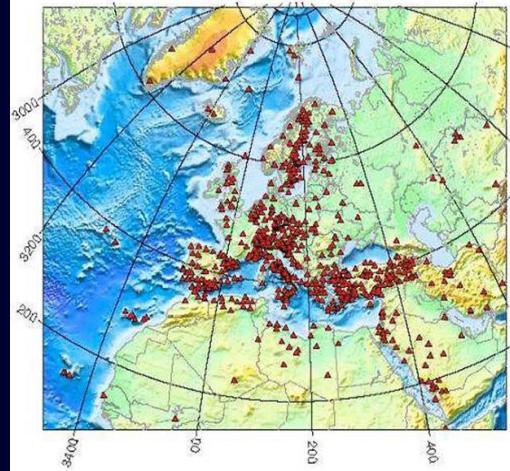
# Different kinds of anisotropy effects on seismic waves

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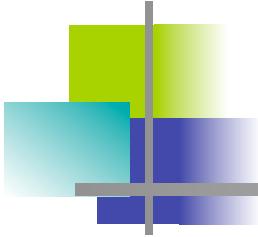


Courtesy of Ed. Garnero

# Data in Global & Regional Seismology



Barruol et al., 2013



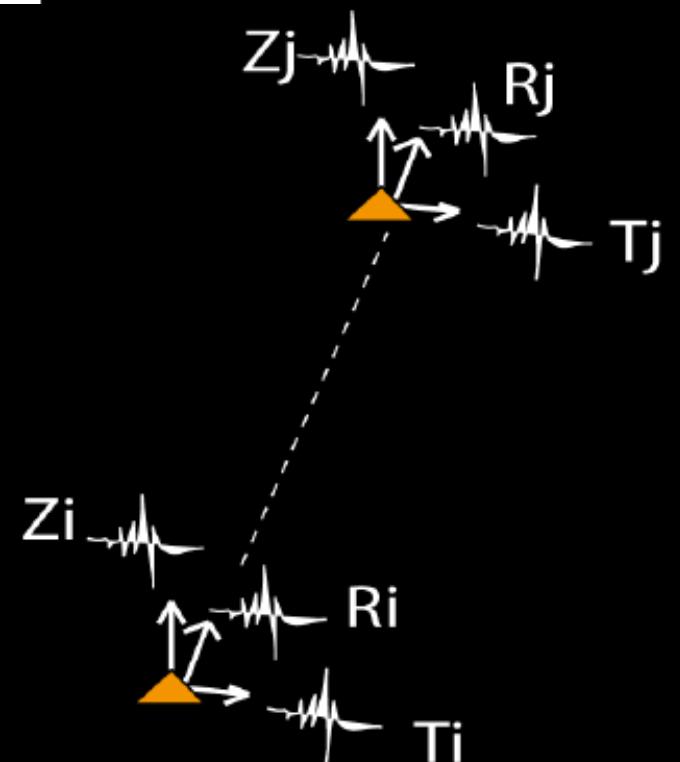
# OUTLINE

- Data driven field: Seismic Data
- Cross-correlation tensor: Seismic Anisotropy?
- Seismic Anisotropy: many processes
- **Scientific Issues:**  
**Seismic monitoring:**  
**Temporal changes of polarization anisotropy in:**
  - **seismogenic** (Parkfield, Cal., USA; Iwate-Miyagi, Japan)
  - Volcanic zones (Mount Fuji, Japan)

Cross-correlation tensor  $C_{ij}$   
 for 2 stations i, j and 3 components k, l  
 Seismic signals  $S_{ik}(t), S_{jl}(t)$

$$[C_{ij}(t)]_{kl} = \frac{\int_0^T S_{ik}(\tau) S_{jl}(t + \tau) d\tau}{\sqrt{\int_0^T S_{ik}^2(\tau) d\tau \int_0^T S_{jl}^2(\tau) d\tau}},$$

<b>ZZ</b>	<b>ZR</b>	<b>ZT</b>
<b>RZ</b>	<b>RR</b>	<b>RT</b>
<b>TZ</b>	<b>TR</b>	<b>TT</b>



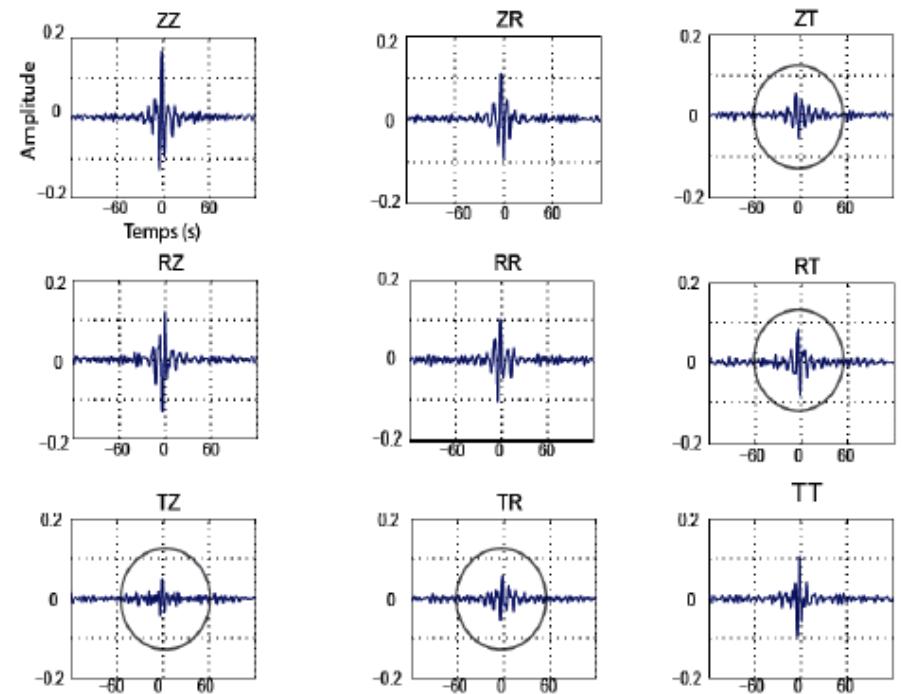
# How can we explain the off-diagonal terms of the cross-correlation tensor?

$TZ, TR, ZT, RT \neq 0$

-Non uniform distribution of seismic noise sources?

-Lateral heterogeneities of Velocities?

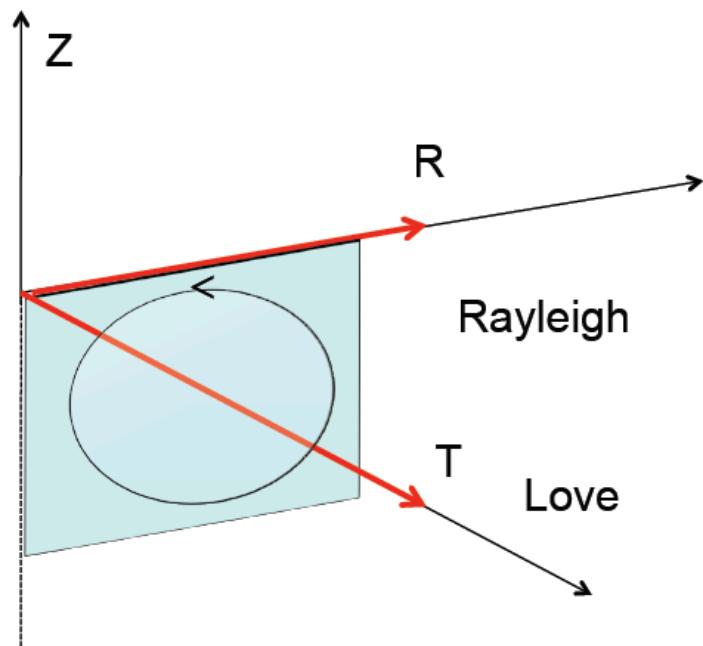
-Seismic anisotropy?



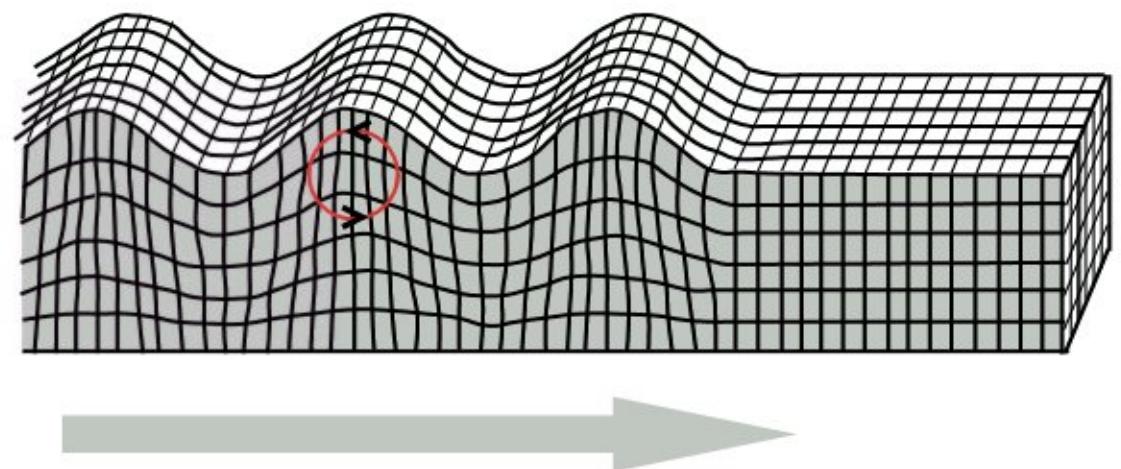
# Effect of anisotropy on amplitude

## Polarization of surface waves

ISOTROPIC MEDIUM

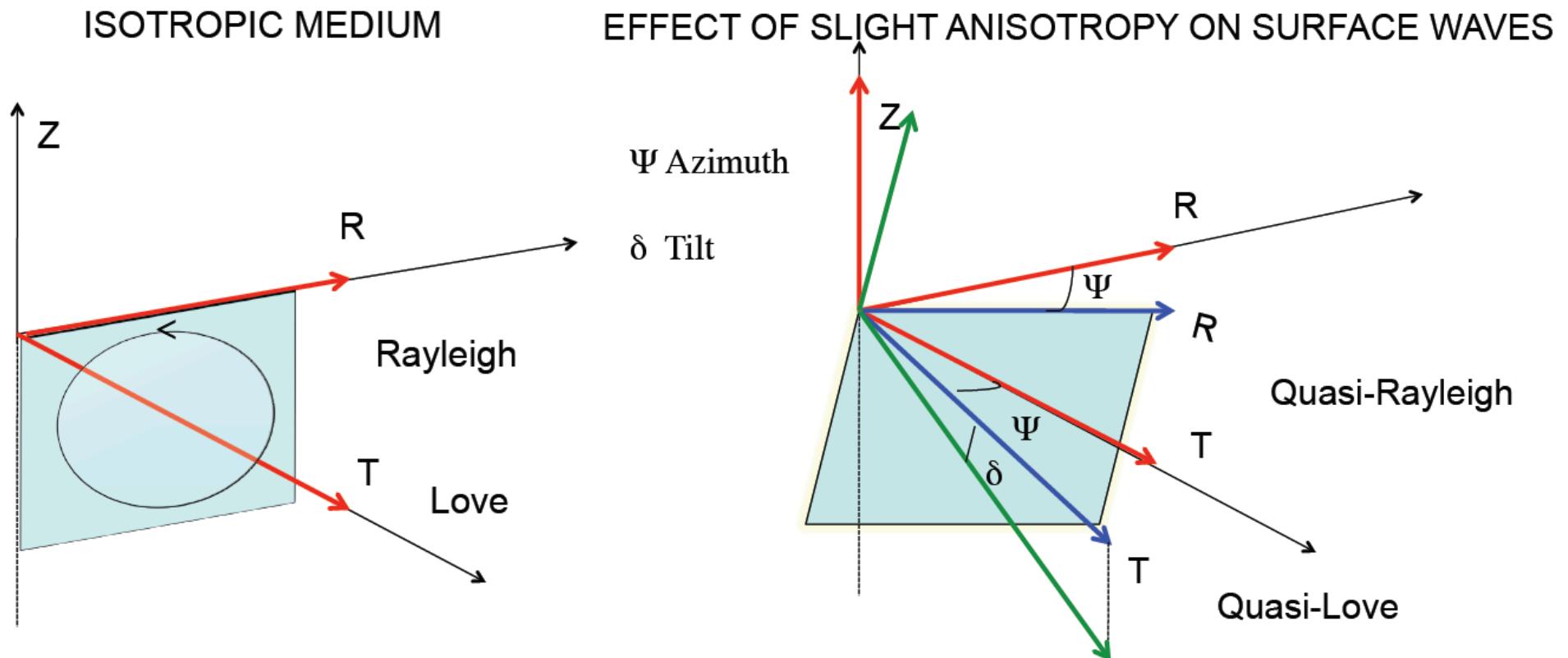


Rayleigh Wave



# Effect of anisotropy on amplitude

## Polarization of surface waves



New Observables  $\Psi, \delta$

# THEORY

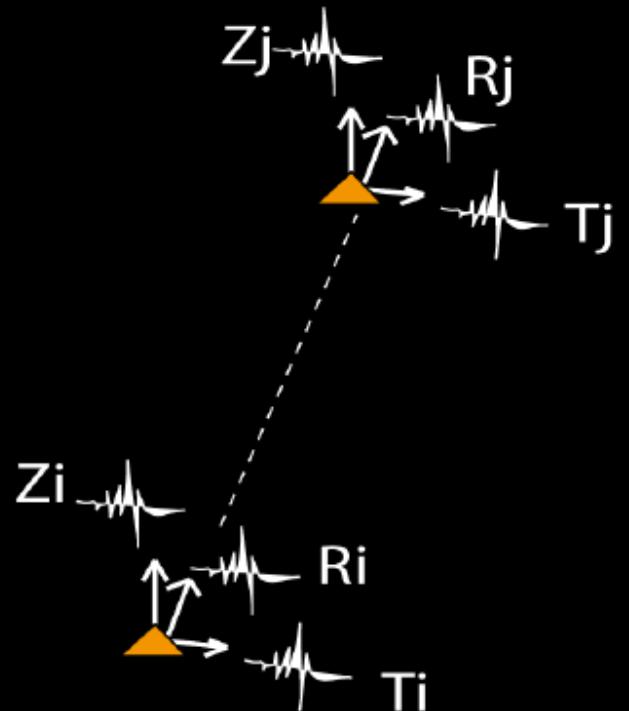
Cross-correlation for 2 stations i, j and 3 components k, l

$$[C_{ij}(t)]_{kl} = \frac{\int_0^T S_{ik}(\tau) S_{jl}(t + \tau) d\tau}{\sqrt{\int_0^T S_{ik}^2(\tau) d\tau \int_0^T S_{jl}^2(\tau) d\tau}}$$

## Cross-Correlation Tensor

ZZ	ZR	ZT
RZ	RR	RT
TZ	TR	TT

Random sources:  
Related to Green's  
tensor i,j (Medium  
response)



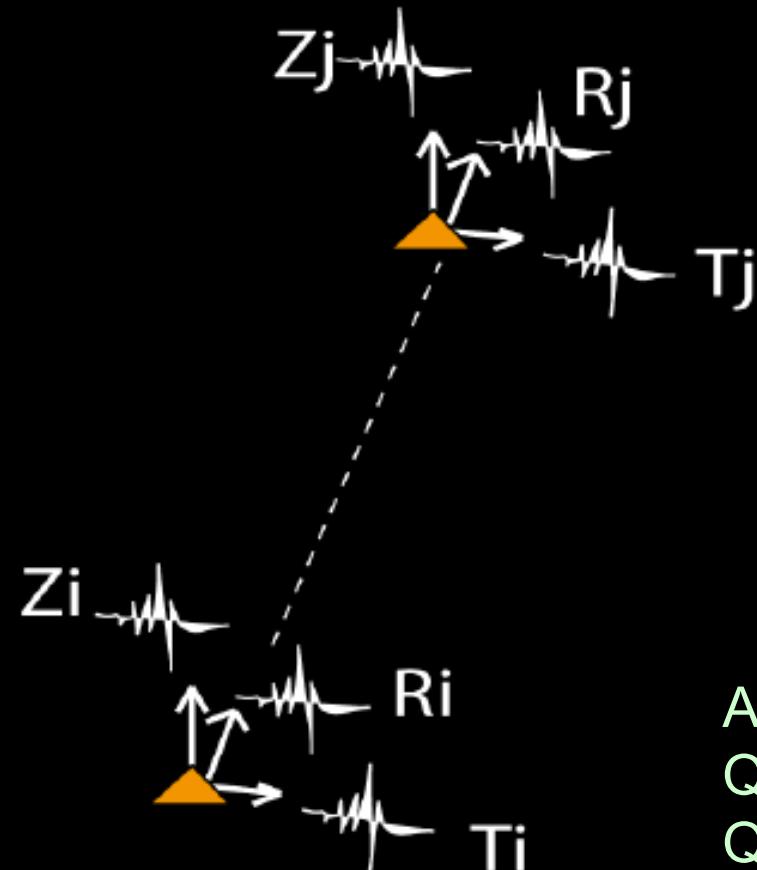
# THEORY

Cross-correlation  
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<b>ZZ</b>	<b>ZR</b>	<b>~0</b>
<b>RZ</b>	<b>RR</b>	<b>~0</b>
<b>~0</b>	<b>~0</b>	<b>TT</b>

ISOTROPIC MEDIUM  
Rayleigh wave  
Love wave



<b>ZZ</b>	<b>ZR</b>	<b>ZT</b>
<b>RZ</b>	<b>RR</b>	<b>RT</b>
<b>TZ</b>	<b>TR</b>	<b>TT</b>

ANISOTROPIC MEDIUM  
Quasi-Rayleigh wave  
Quasi-Love wave

# THEORY

Cross-correlation  
for 2 stations i, j  
and 3 components k, l

$$[C_{ij}(t)]_{kl} = \frac{\int_0^T S_{ik}(\tau) S_{jl}(t + \tau) d\tau}{\sqrt{\int_0^T S_{ik}^2(\tau) d\tau \int_0^T S_{jl}^2(\tau) d\tau}},$$

Azimuthal  
Anisotropy  
of Rayleigh  
waves

Effect of anisotropy on  $C_{ij}$

ZZ	ZR	ZT
RZ	RR	RT
TZ	TR	TT

Joint Inversion  
of Rayleigh  
and Love waves:  
Radial anisotropy

# THEORY

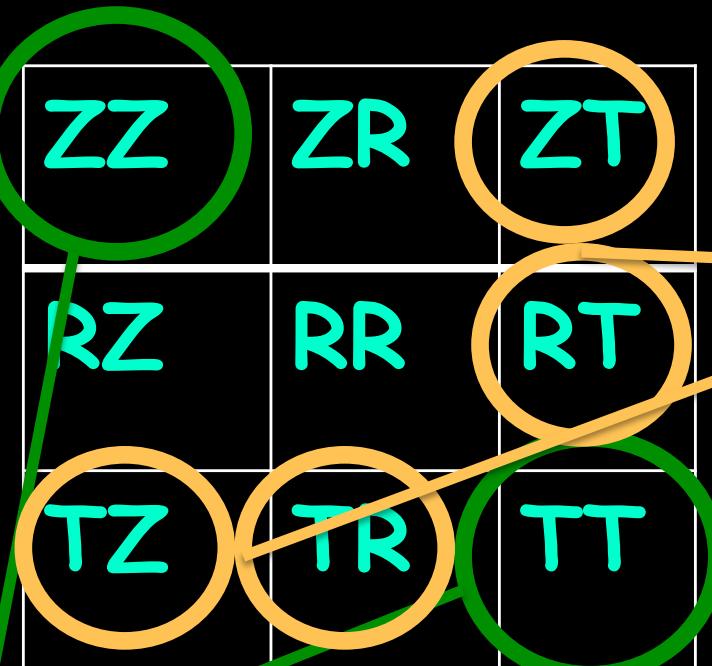
Cross-correlation  
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Azimuthal  
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Effect of anisotropy on  $C_{ij}$

Joint Inversion  
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Radial anisotropy

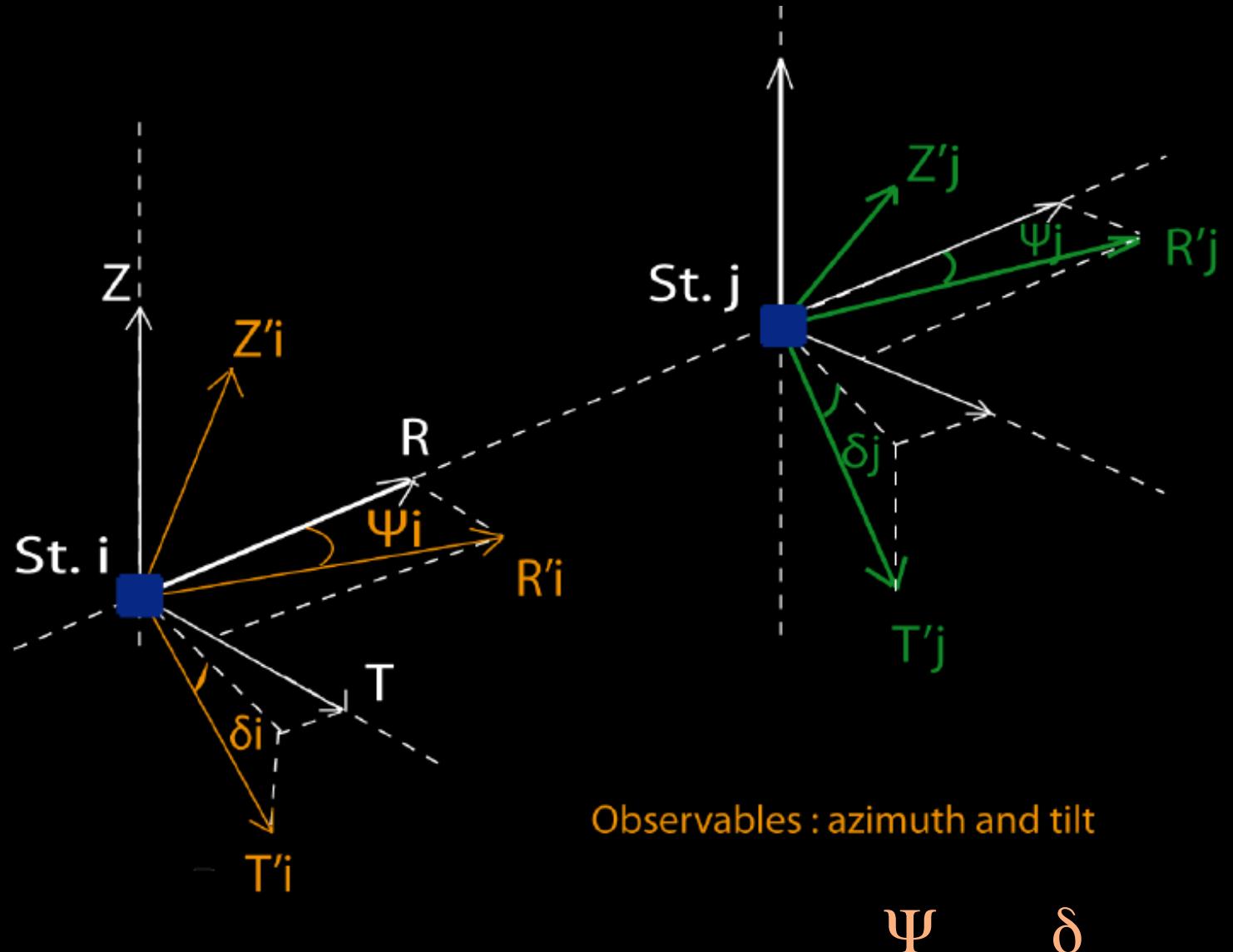


Quasi-Rayleigh  
Quasi-Love  
waves:  
polarization  
anomalies

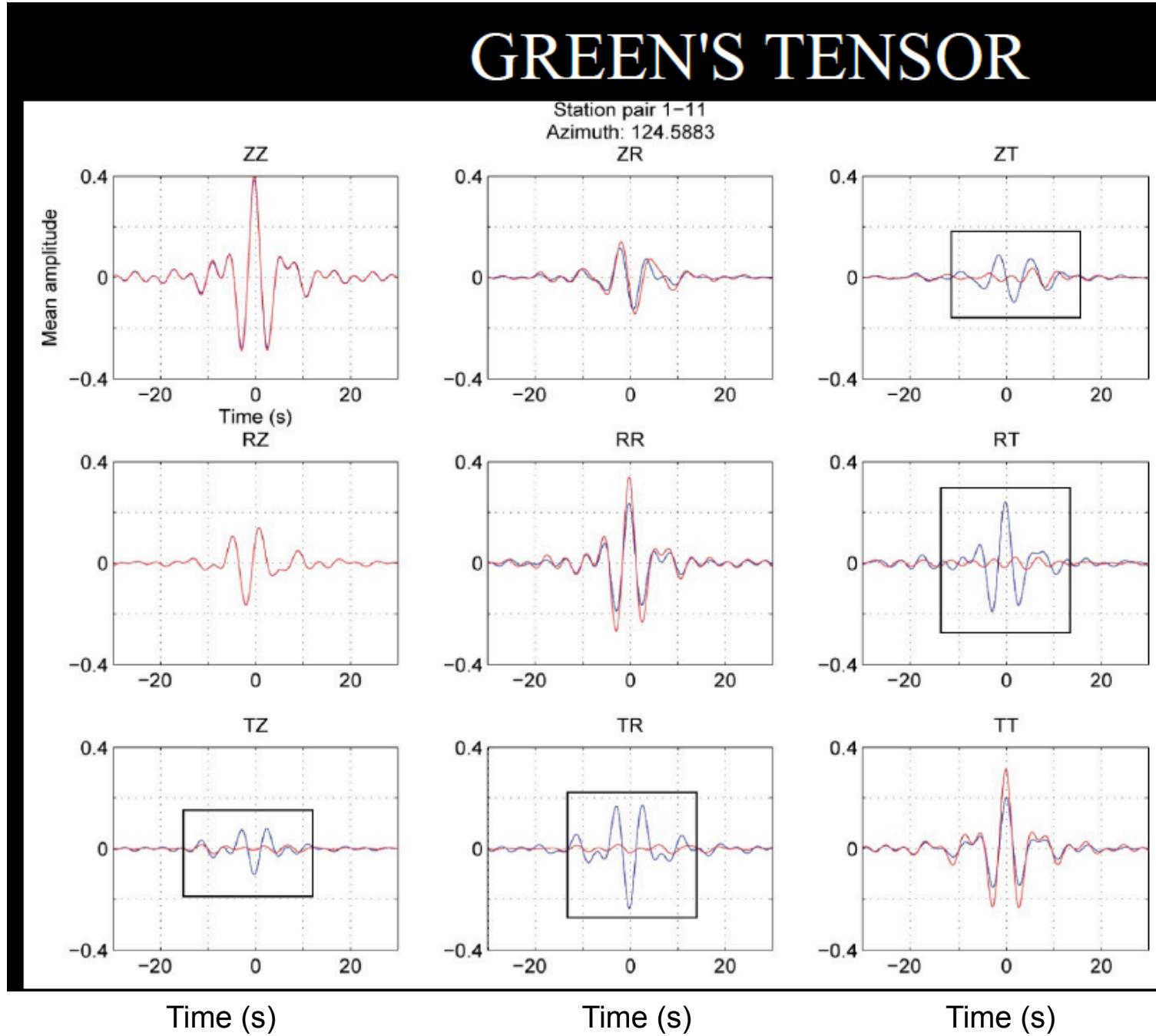
# ORA: Optimal Rotation Algorithm (Roux, GJI, 2010)

Minimization of  
the RT, TR, ZT and TZ  
components

ZZ	ZR	<del>ZT</del>
RZ	RR	<del>RT</del>
<del>ZT</del>	<del>TR</del>	TT



# Efficiency of Optimal Rotation Algorithm (ORA)



## ***Temporal changes of Cross-correlations (polarization angle $\Psi$ )***

2 effects:

- Non-random distribution of seismic sources

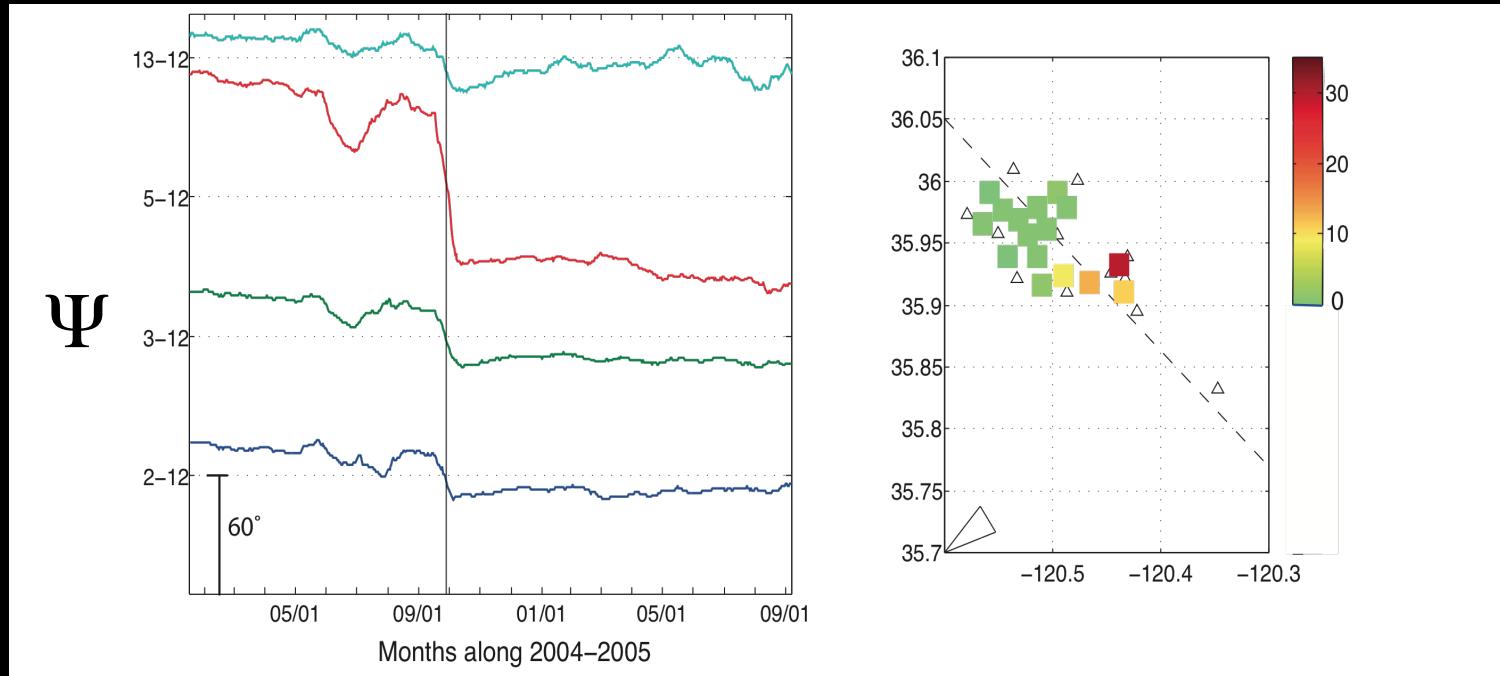
seasonal variations

(beamforming analysis)

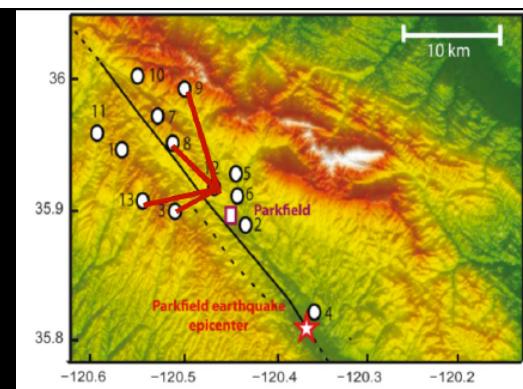
→ - ANISOTROPY changes

→ Stress field temporal variations

# Time variations of $\Psi$ angle after noise removal



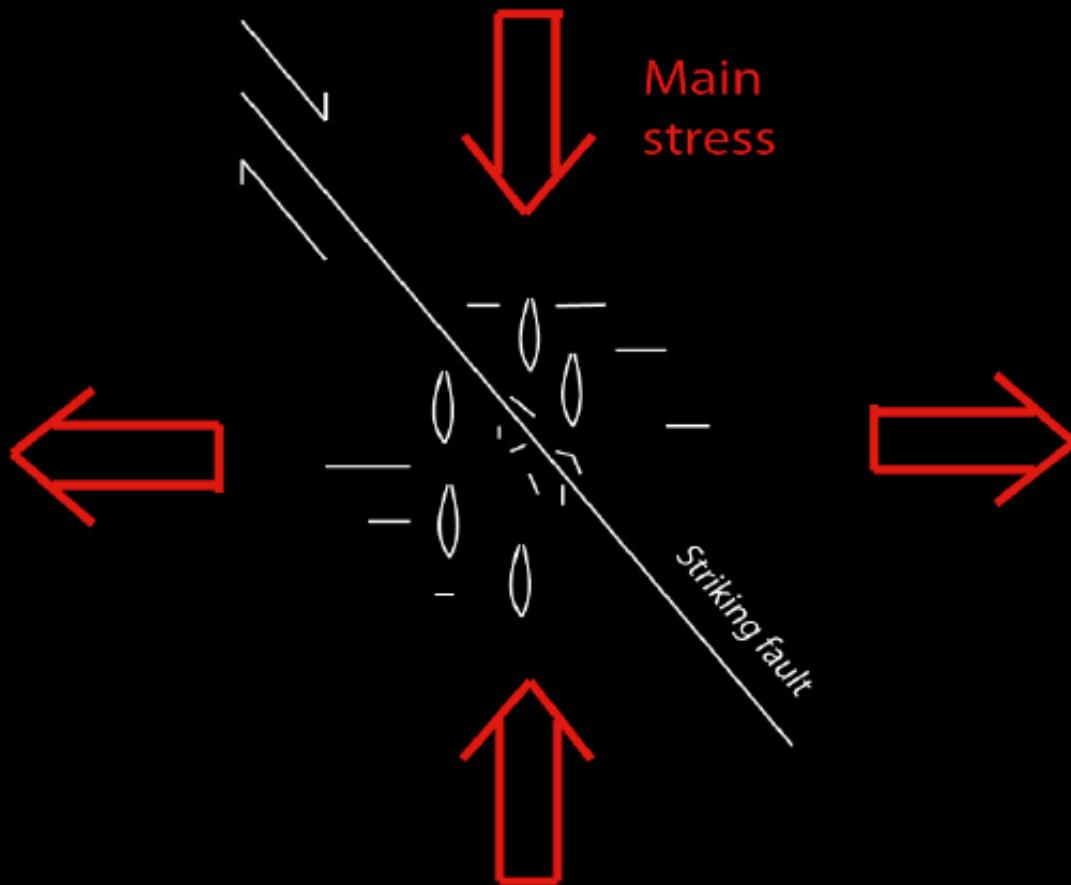
Significant co-seismic  
jumps for station pairs  
containing station 12



Tentative (reasonable) interpretation:  
stress rotation => apparent rotation of the crack distribution

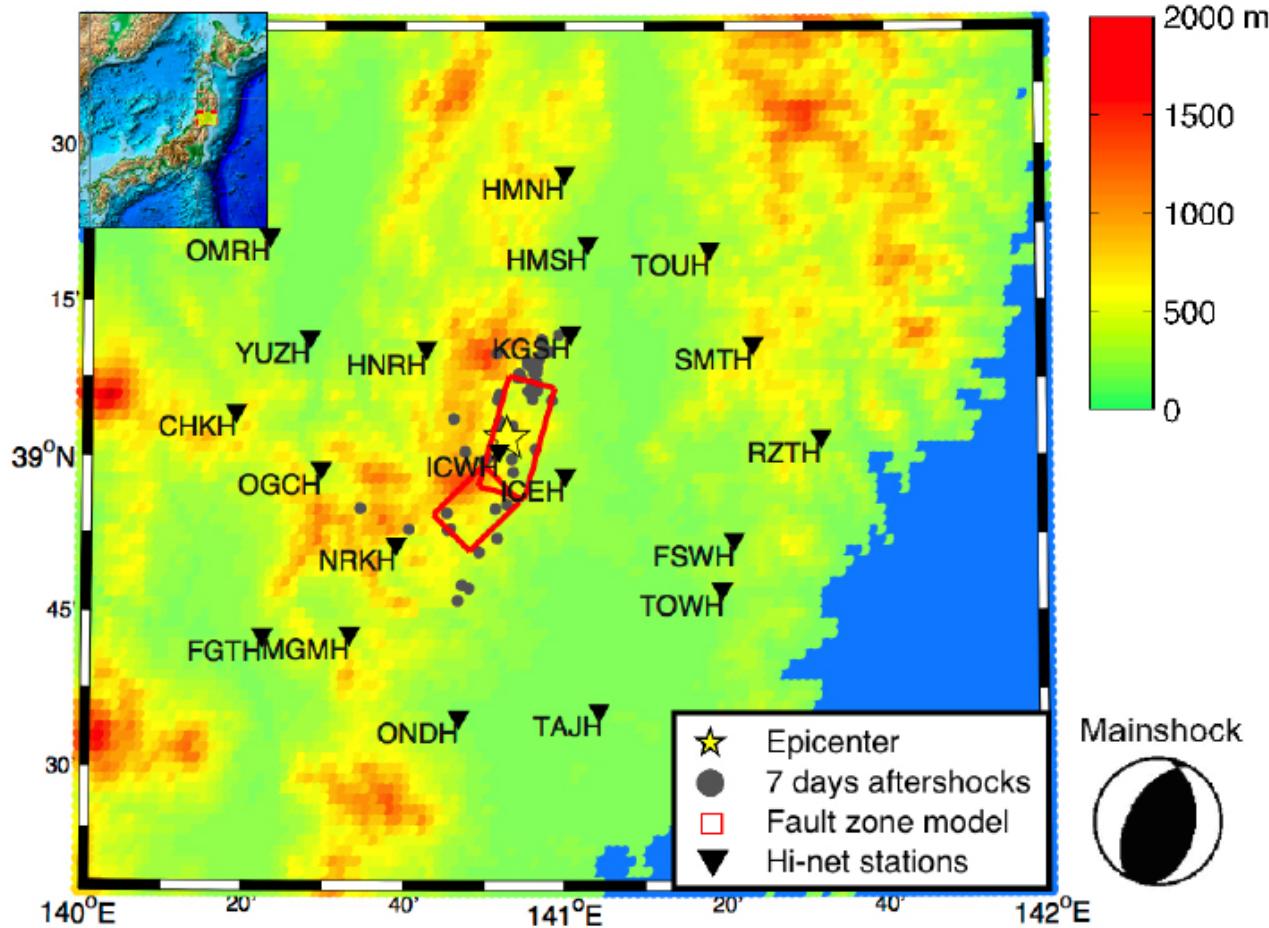
# Seismic Anisotropy: Cracks, fluid inclusions

stress field rotations in the crust  
⇒ temporal variations of velocity  
and anisotropy during seismic cycle?



# Other Tectonic context

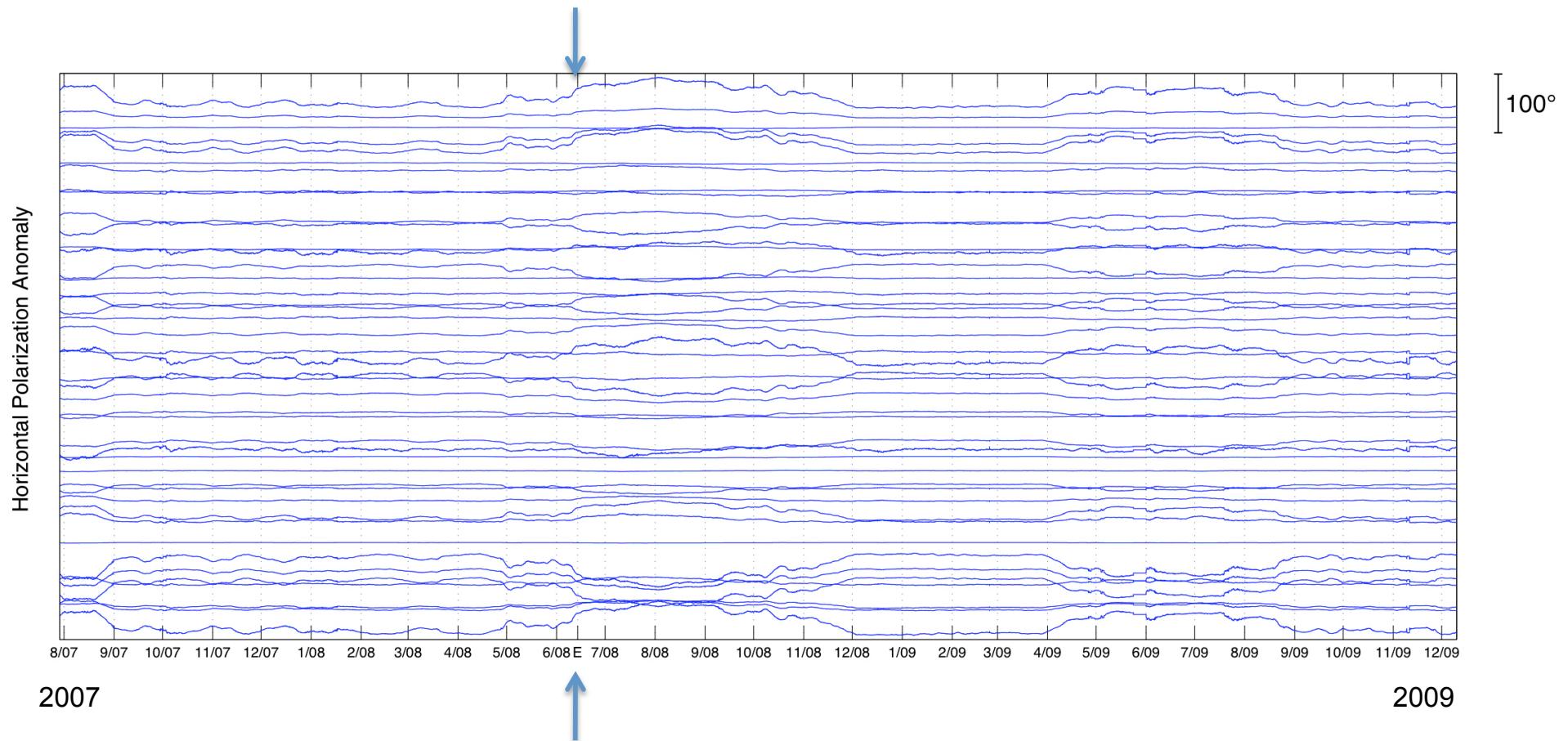
## Iwate – Miyagi earthquake (14/06/08)



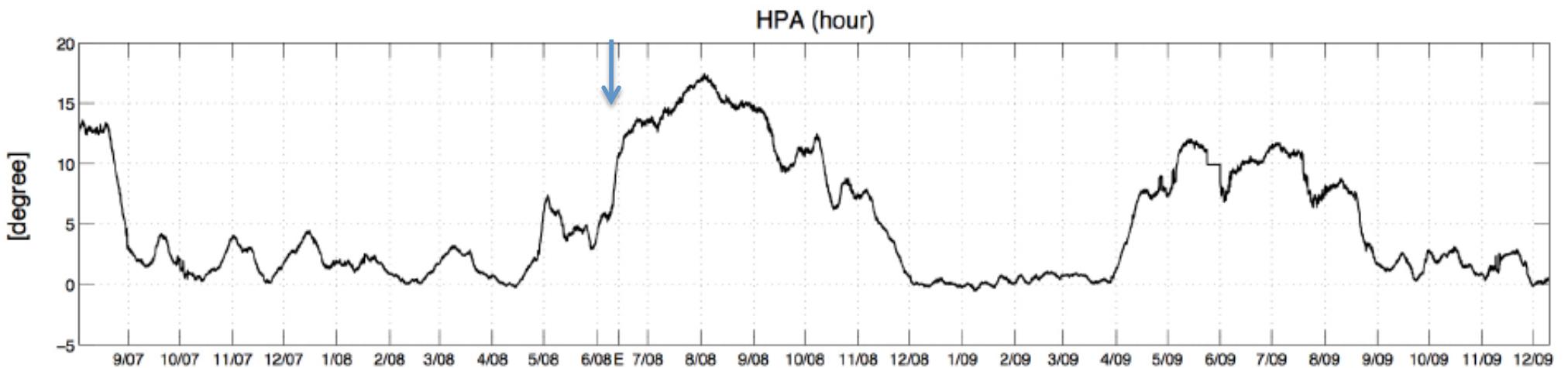
Data: Jul. 2007- Dec. 2009

NIED

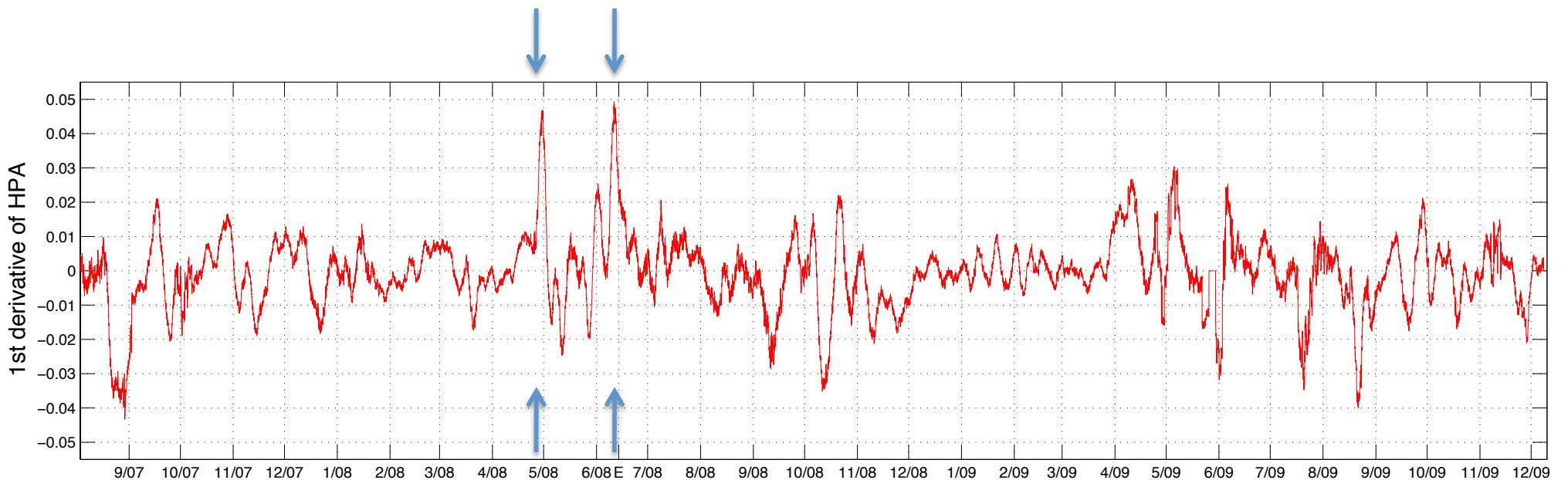
# Horizontal Polarization Anomaly $\Psi$



# Average of the Horizontal Polarization Anomaly $\Psi$ (HPA)

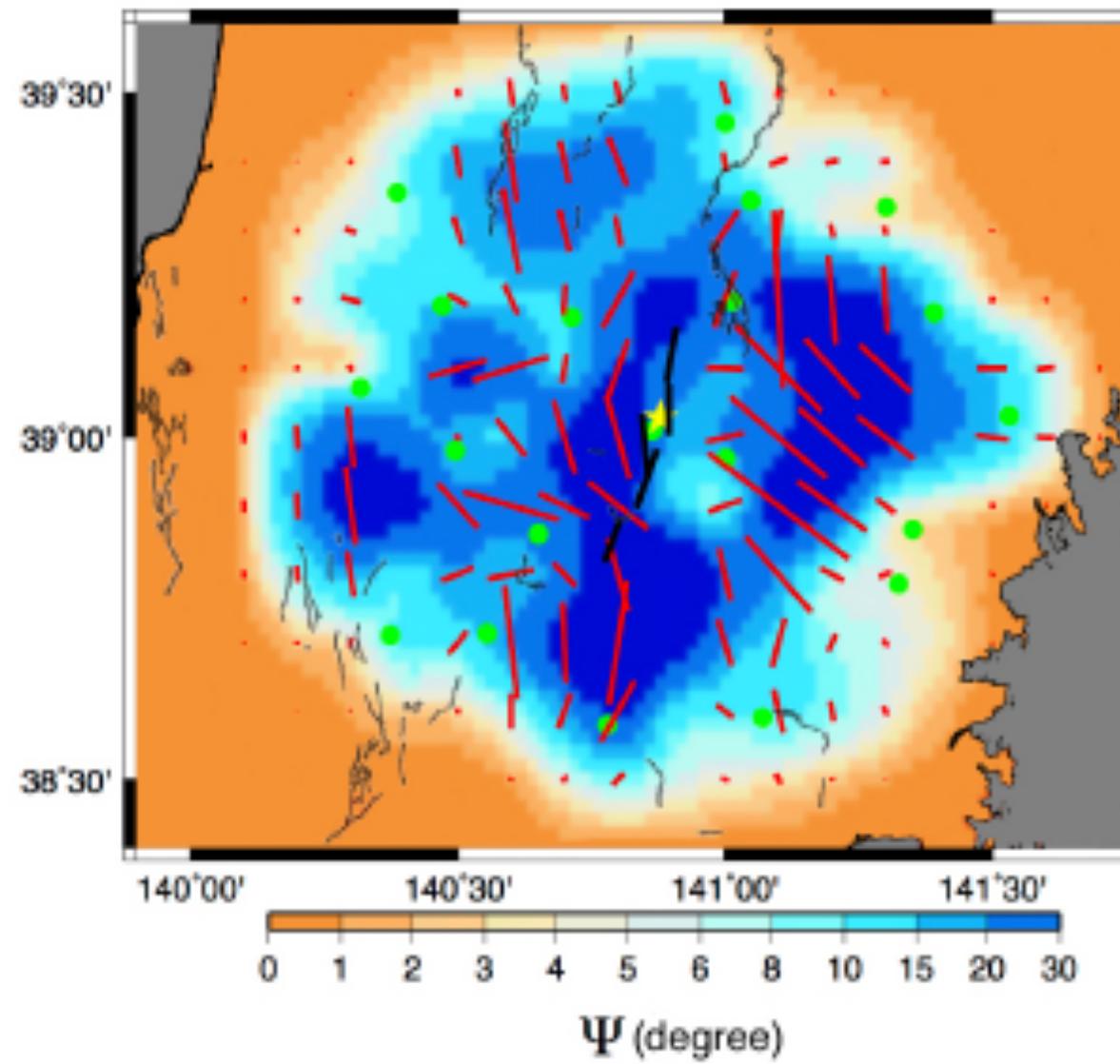


## Time derivative of HPA

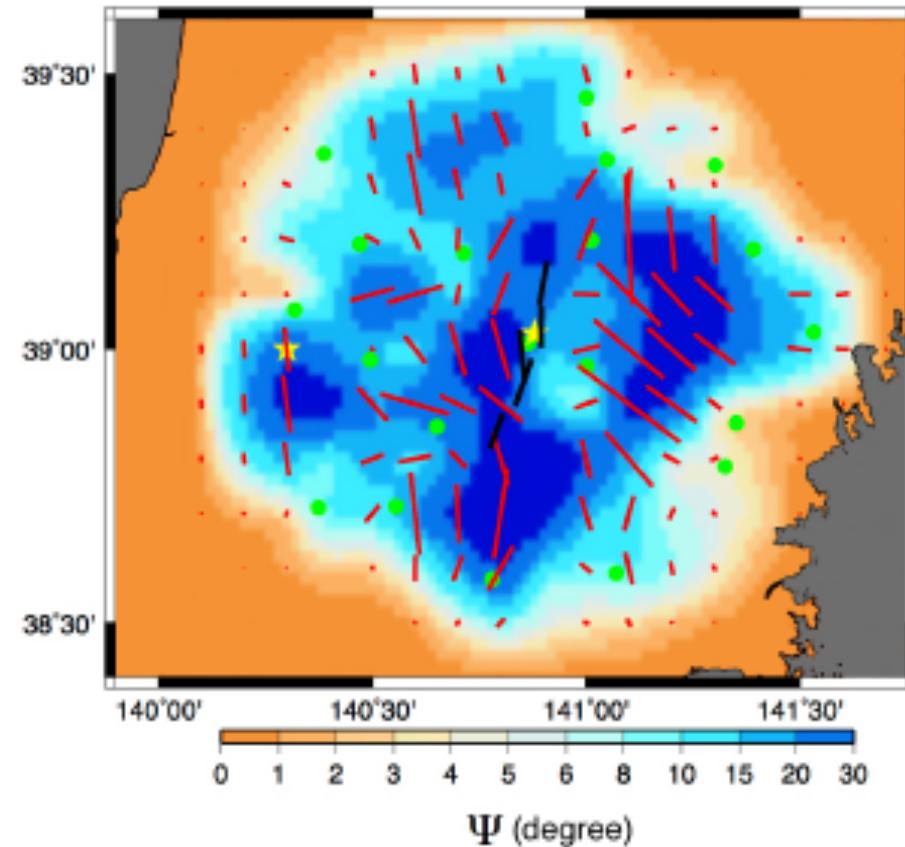
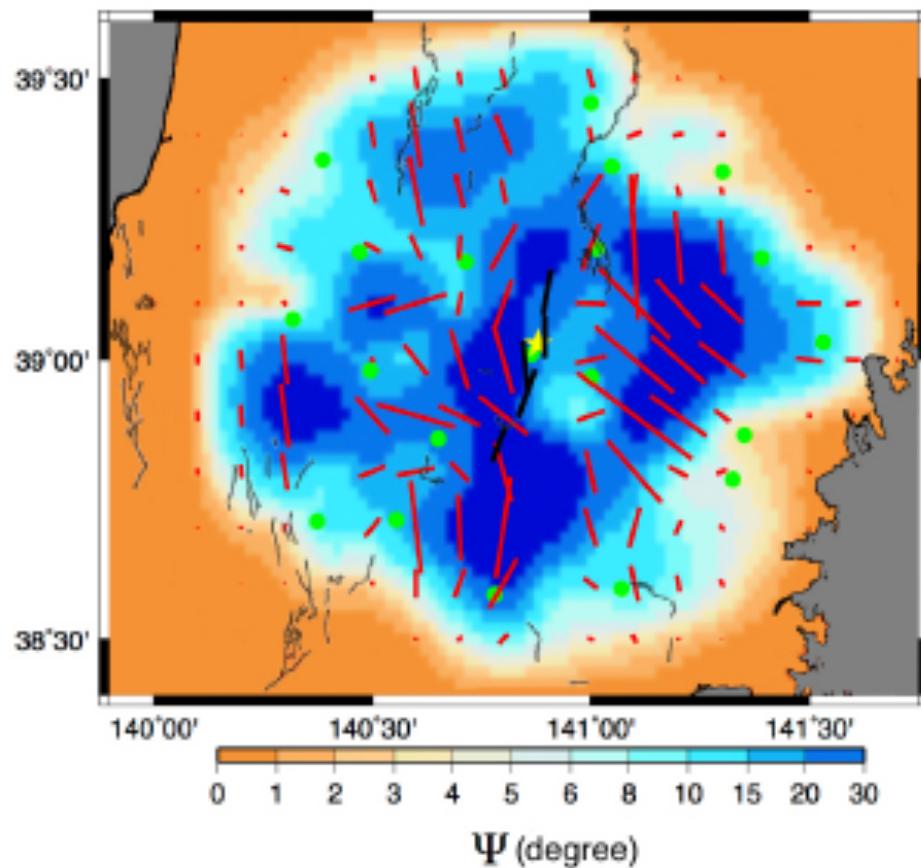


# Horizontal Polarization change $\Psi$ at the time of the EQ

## June 13, 2008



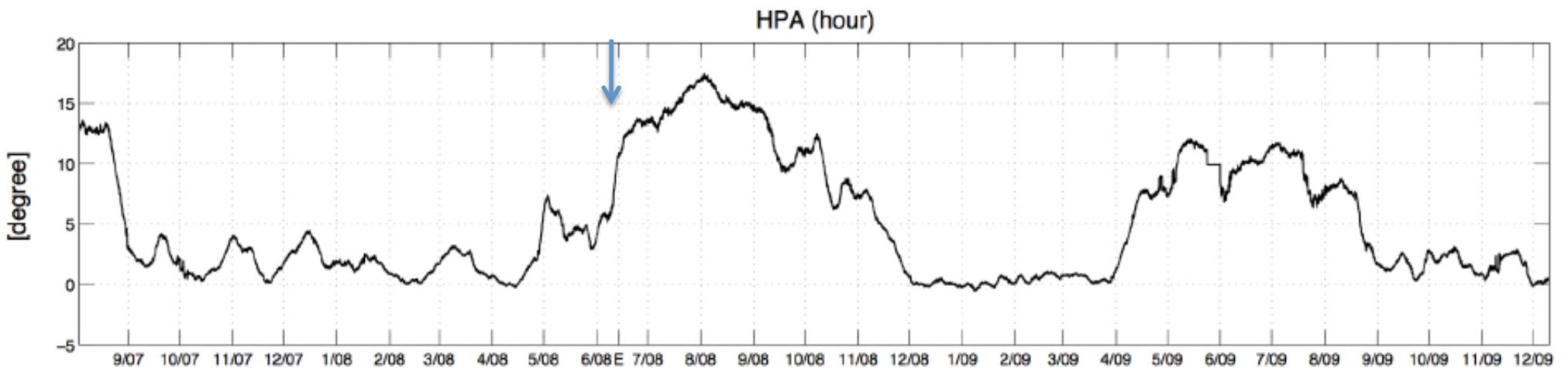
# Horizontal Polarization change $\Psi$ at the time of the EQ      and      at the end of April



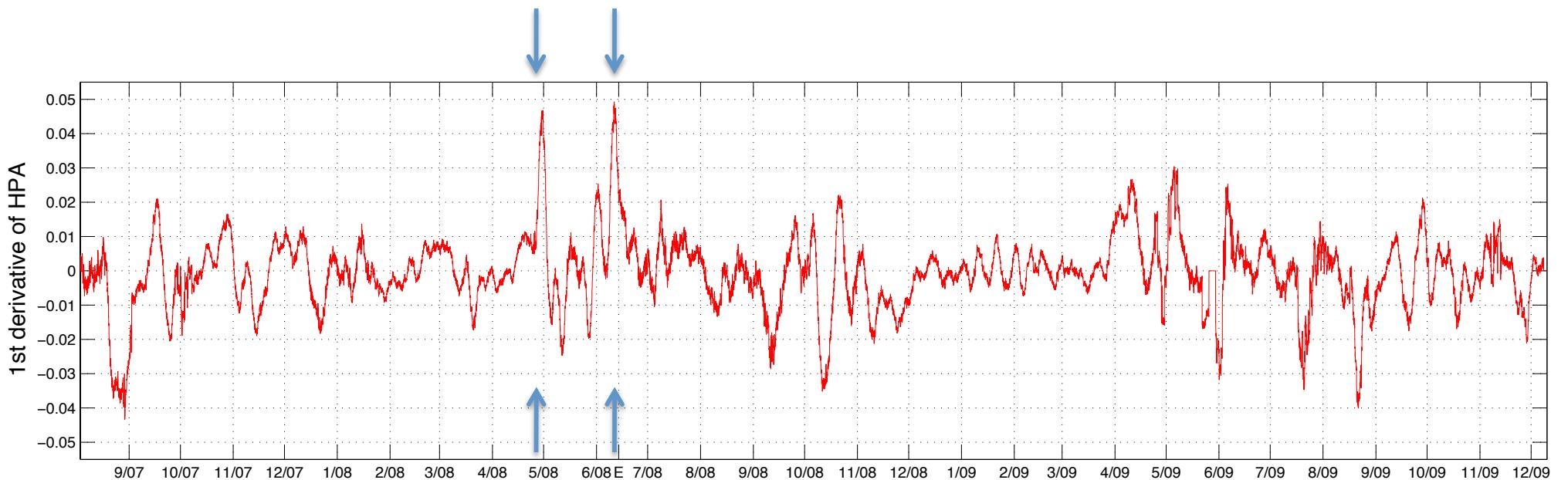
Many similarities for variations of the polarization anomaly for both events  
(deep earthquake on April 17, 2008; Mw= 5.7)

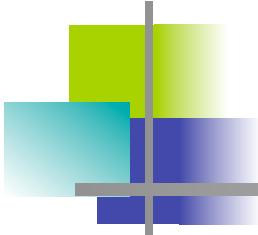
Z! correlation does not mean causality

# Average of the Horizontal Polarization Anomaly $\Psi$ (HPA)



## Time derivative of HPA

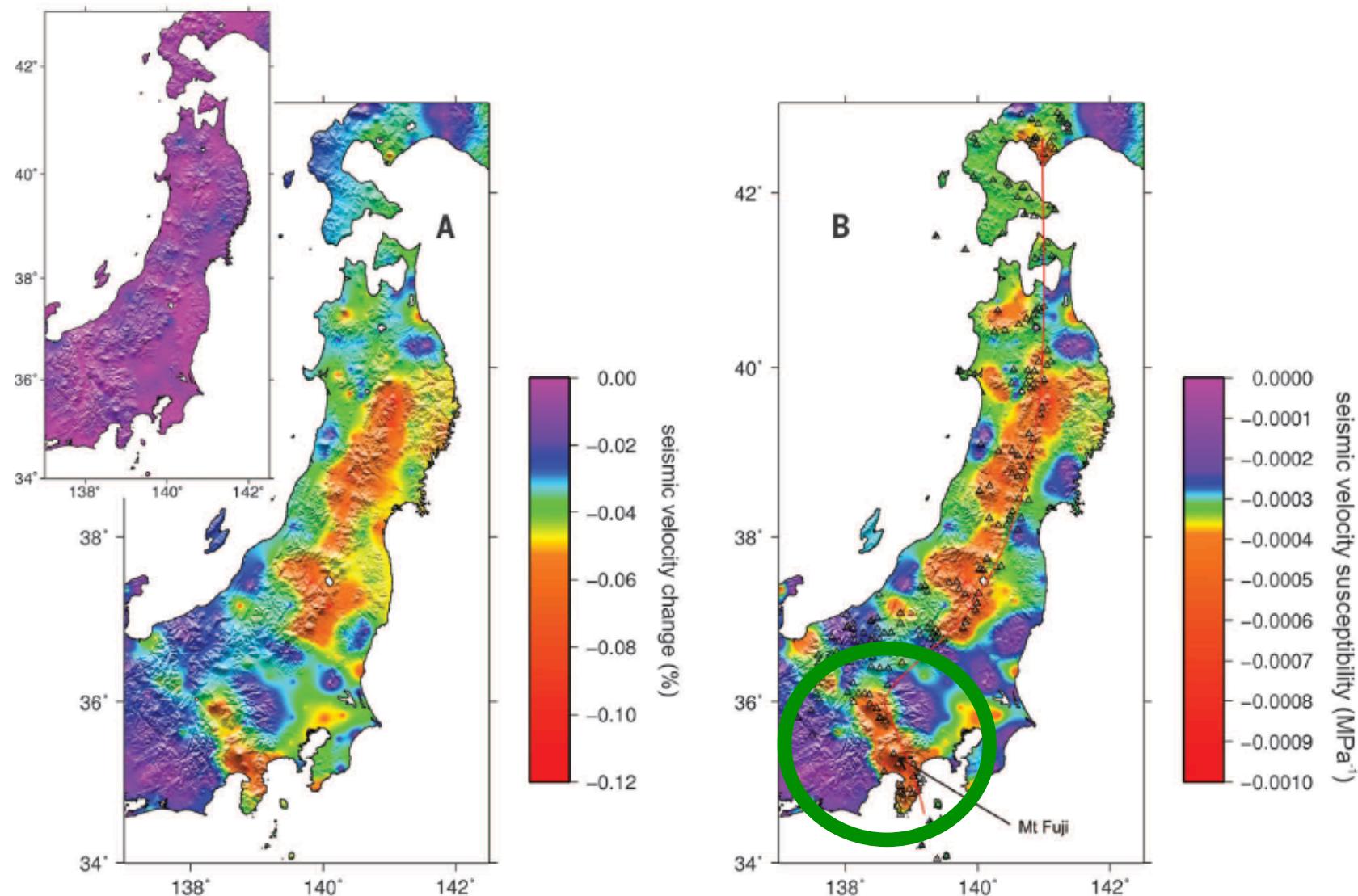




# OUTLINE

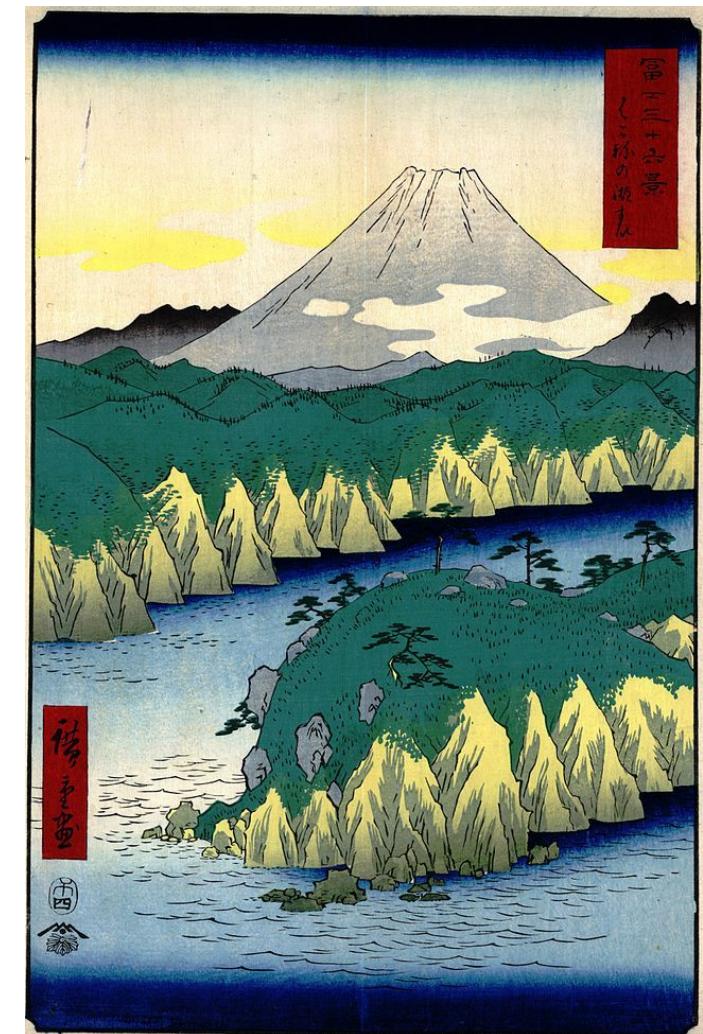
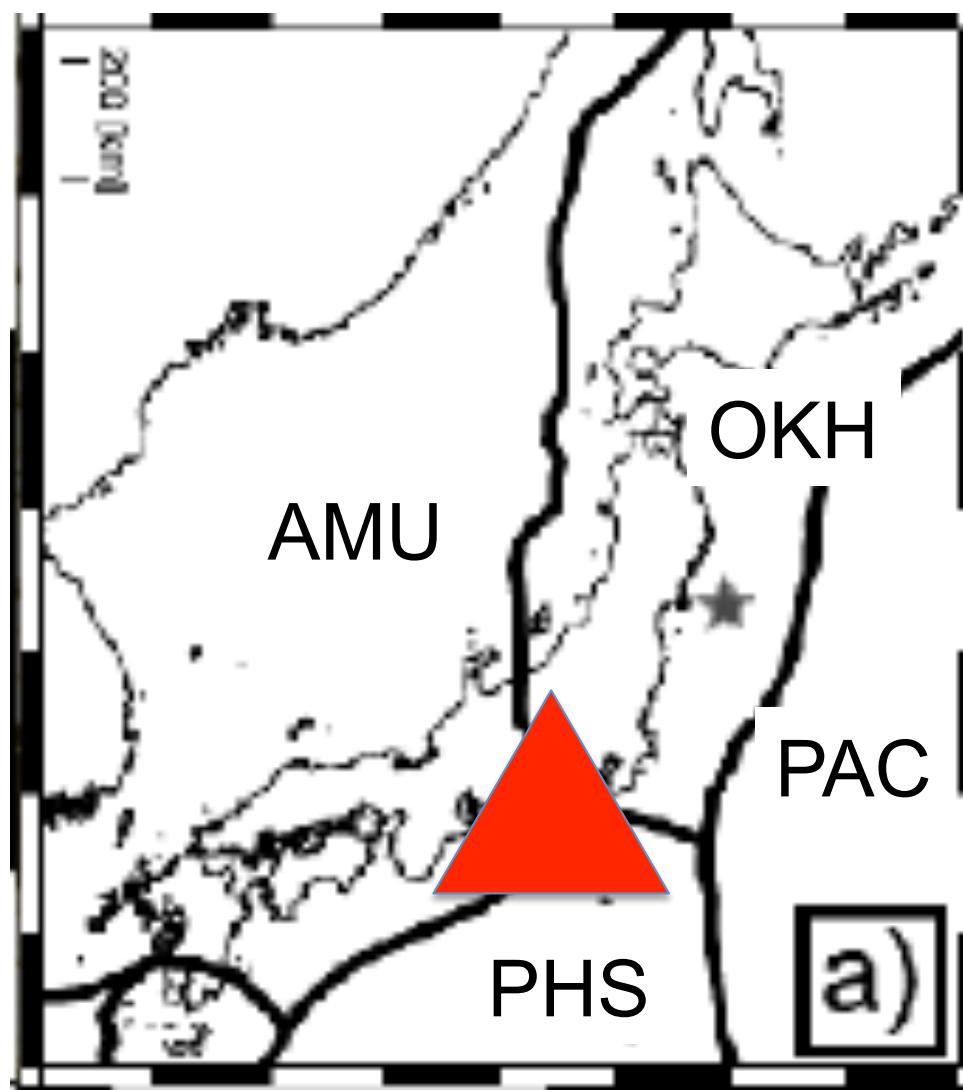
- Seismic Data
- Seismic Anisotropy: many processes
- **Scientific Issues:**  
**Seismic monitoring:**  
**Temporal changes of polarization anisotropy in:**
  - seismogenic (Parkfield, Cal., USA; Iwate-Miyagi, Japan)
  - **Volcanic zones (Mount Fuji, Japan)**

# Volcanic zones: after the Tohoku-oki earthquake (11 march 2011)



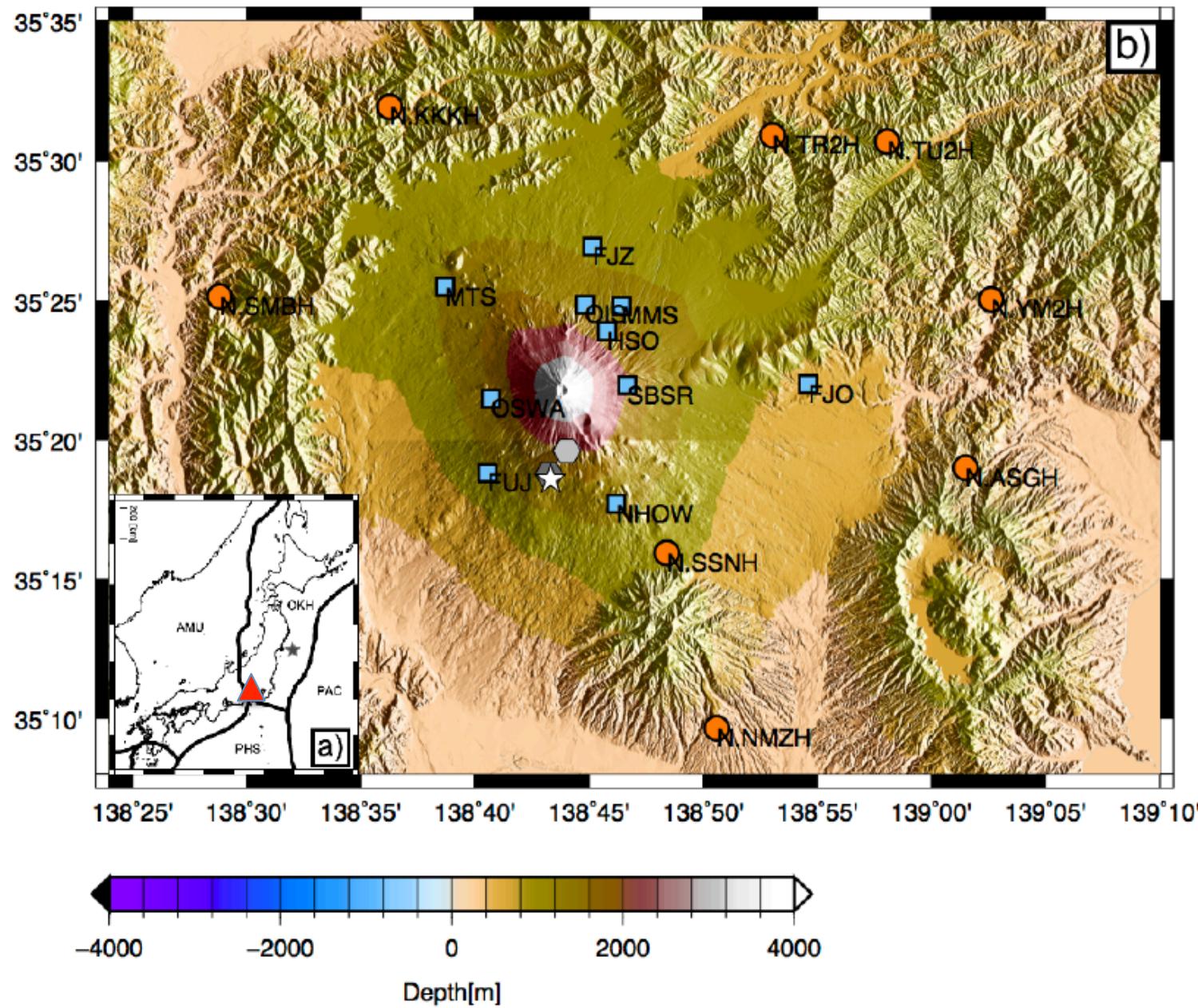
Brenguier et al., 2014

# Monitoring of volcanic zones: Mount Fuji (+Hakone)



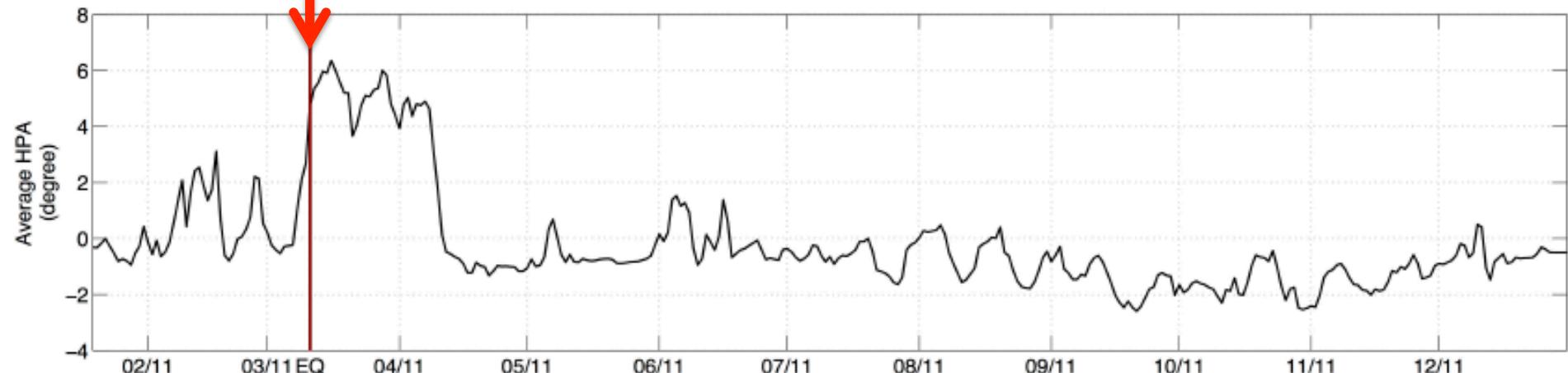
Hiroshige, 1858

# Monitoring of volcanic zones: Mount Fuji

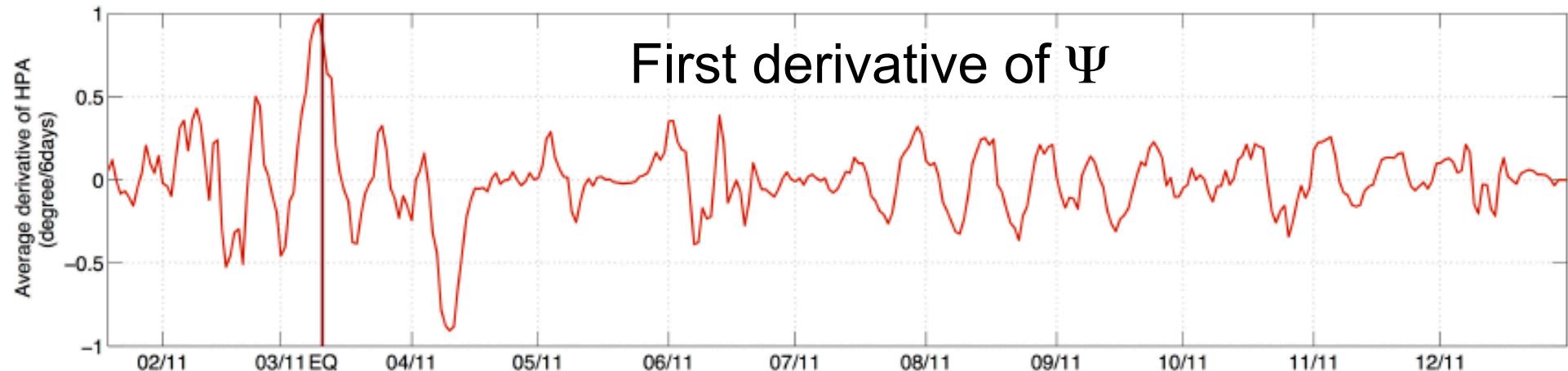


# Monitoring of volcanic zones

Average of the horizontal polarization anomaly  $\Psi$

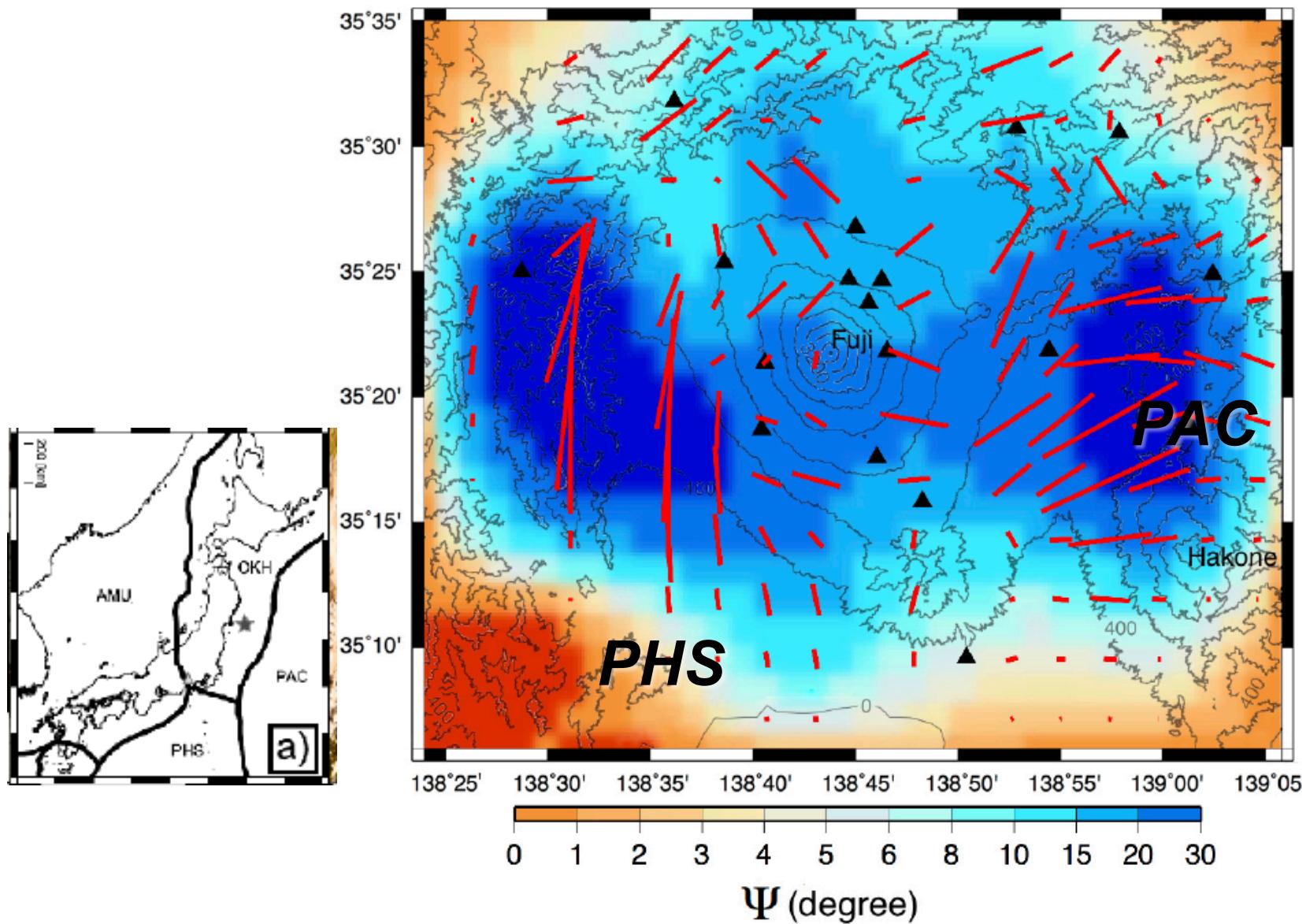


First derivative of  $\Psi$



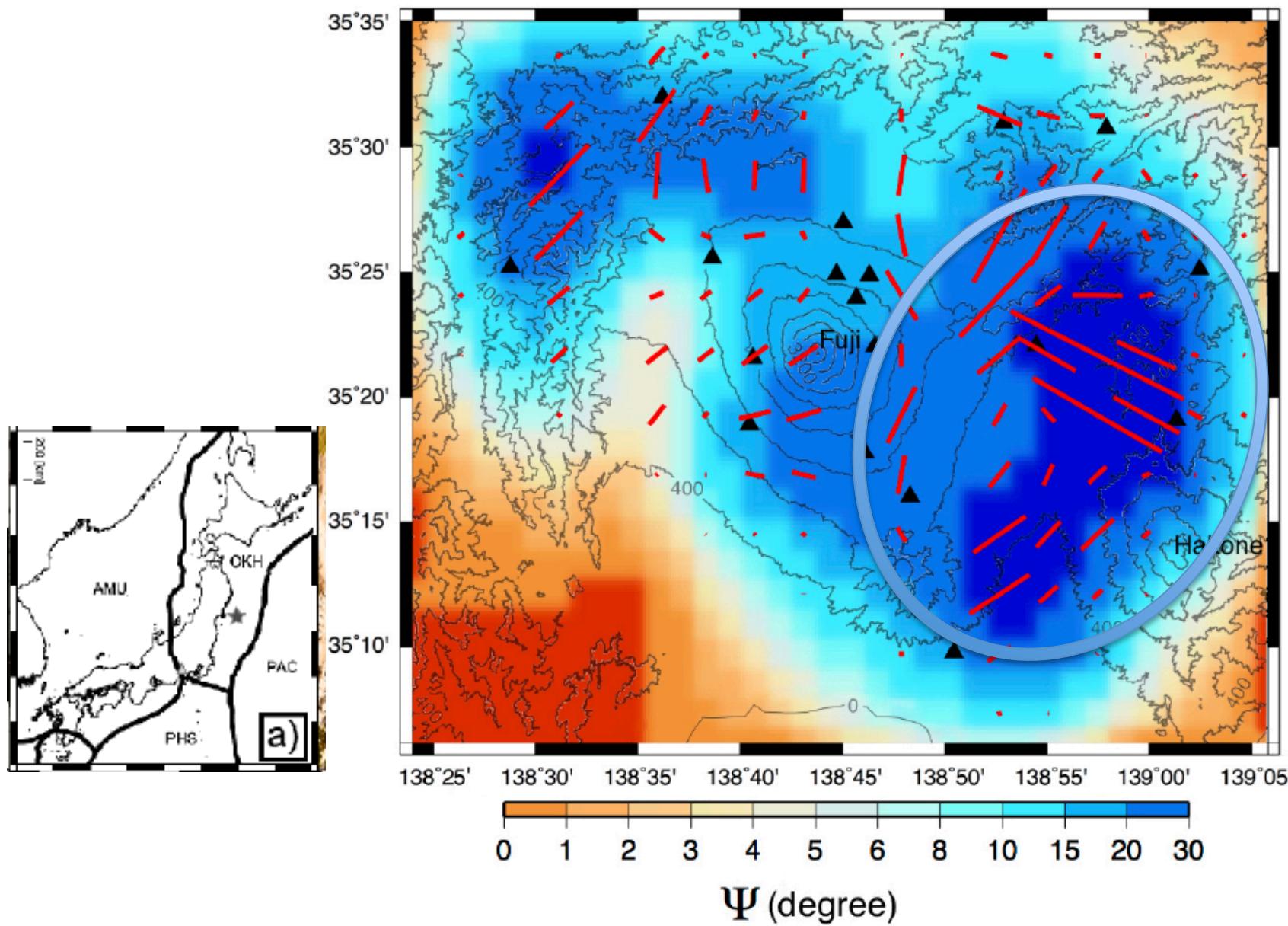
# Monitoring of volcanic zones

Average polarization change + Orientation of anisotropy



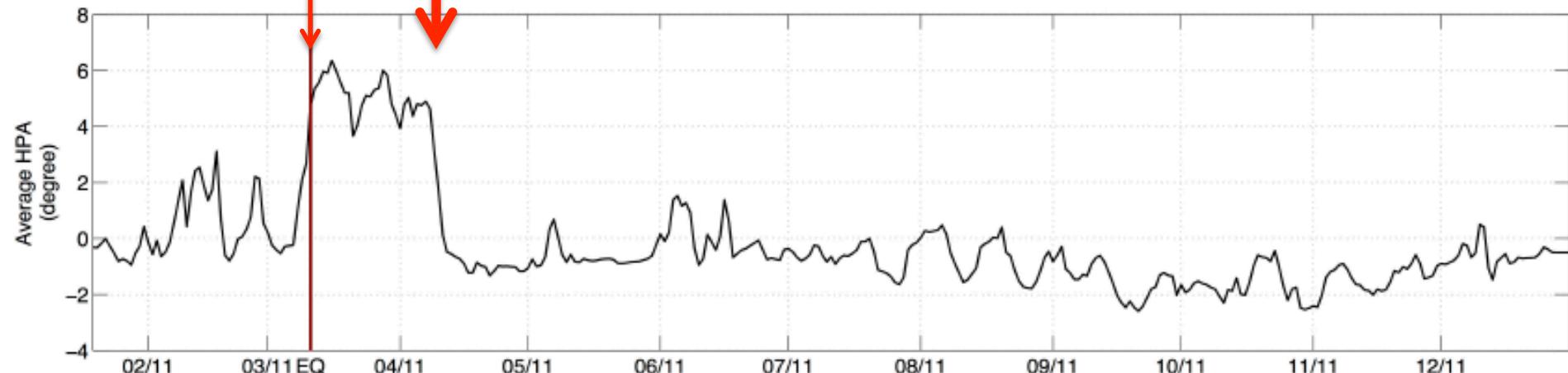
# Monitoring of volcanic zones

Polarization and anisotropy change at the time of the EQ

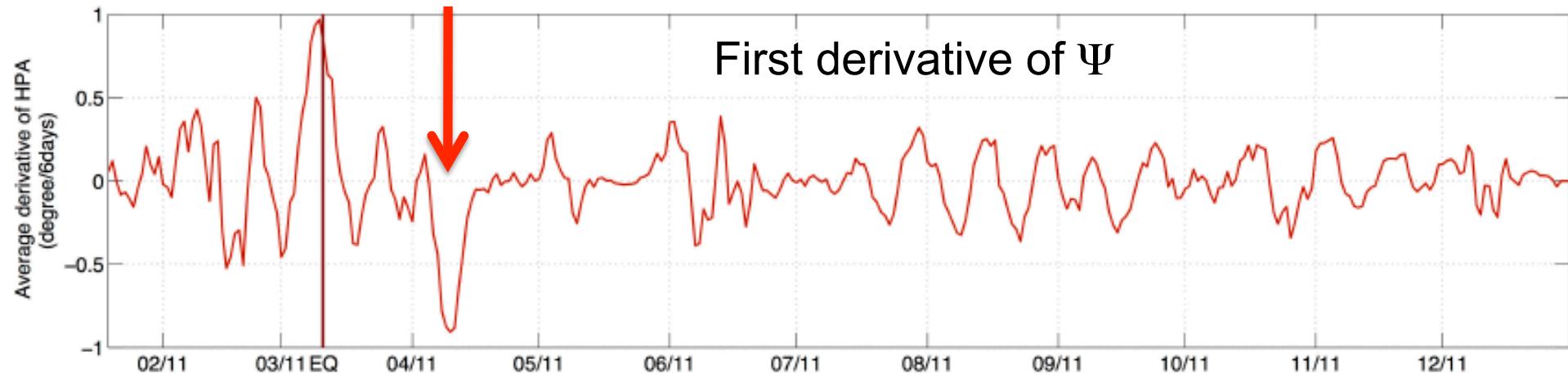


# Monitoring of volcanic zones

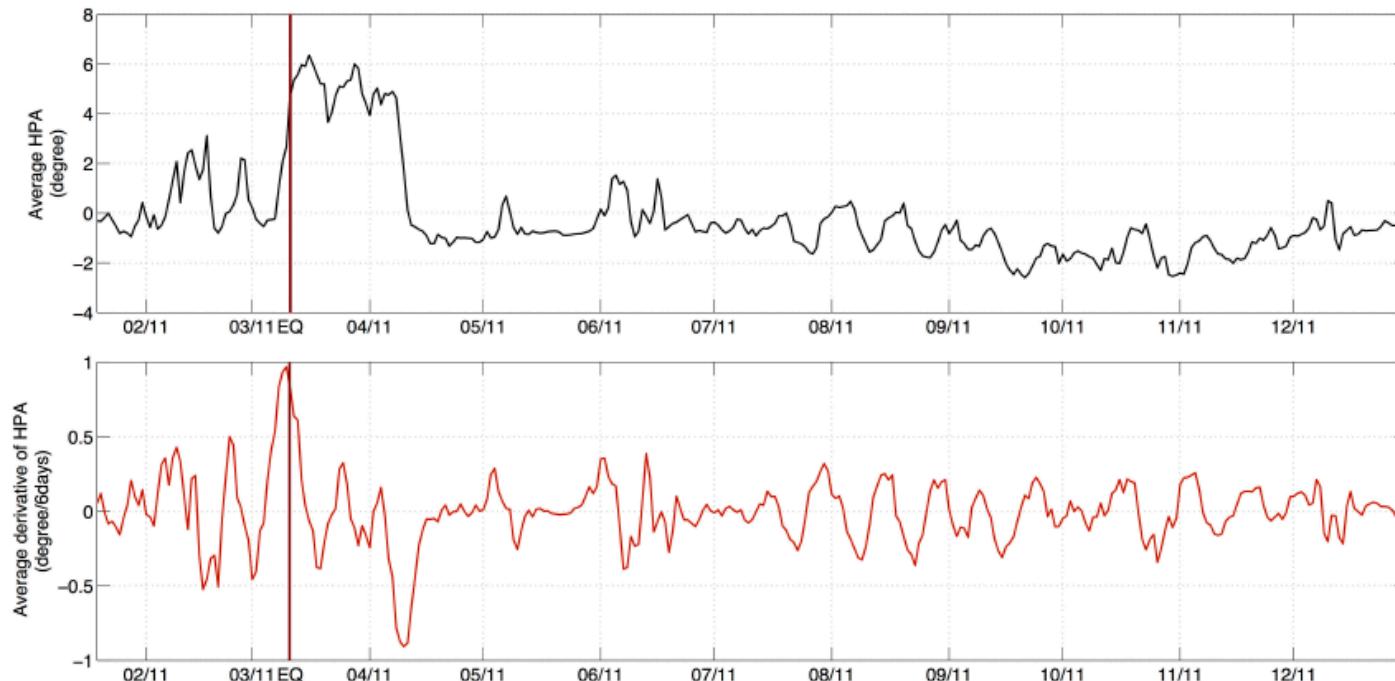
Average of the horizontal polarization anomaly  $\Psi$



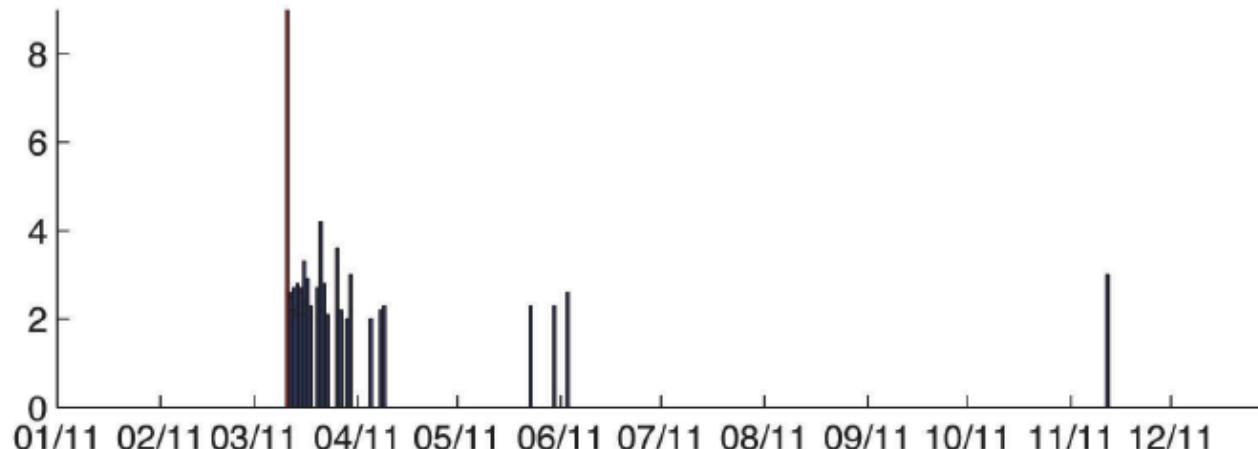
First derivative of  $\Psi$



# Monitoring of volcanic zones

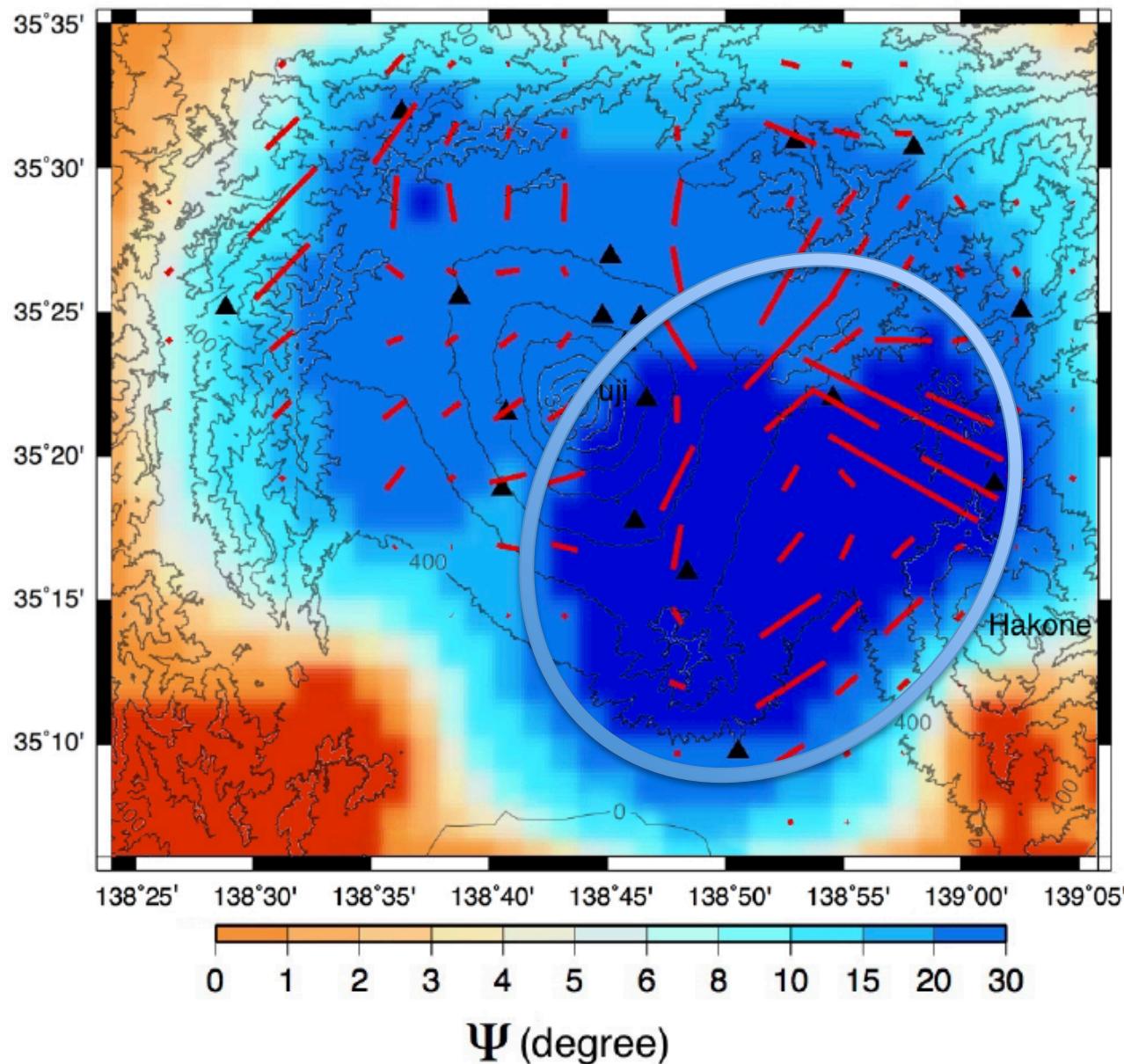


Seismicity in Hakone Area –  $M_w > 2$  & depth < 10km

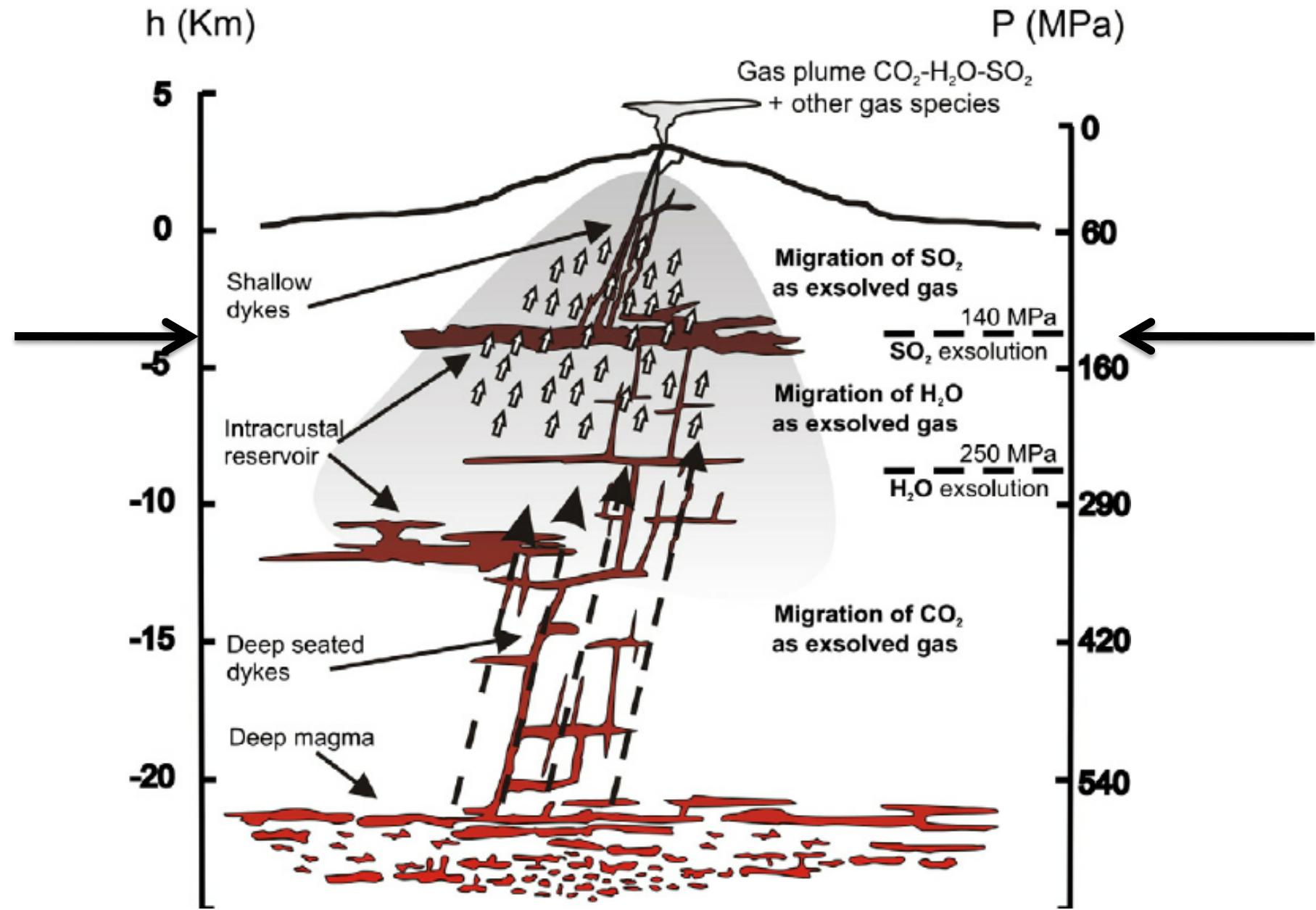


# Monitoring of volcanic zones

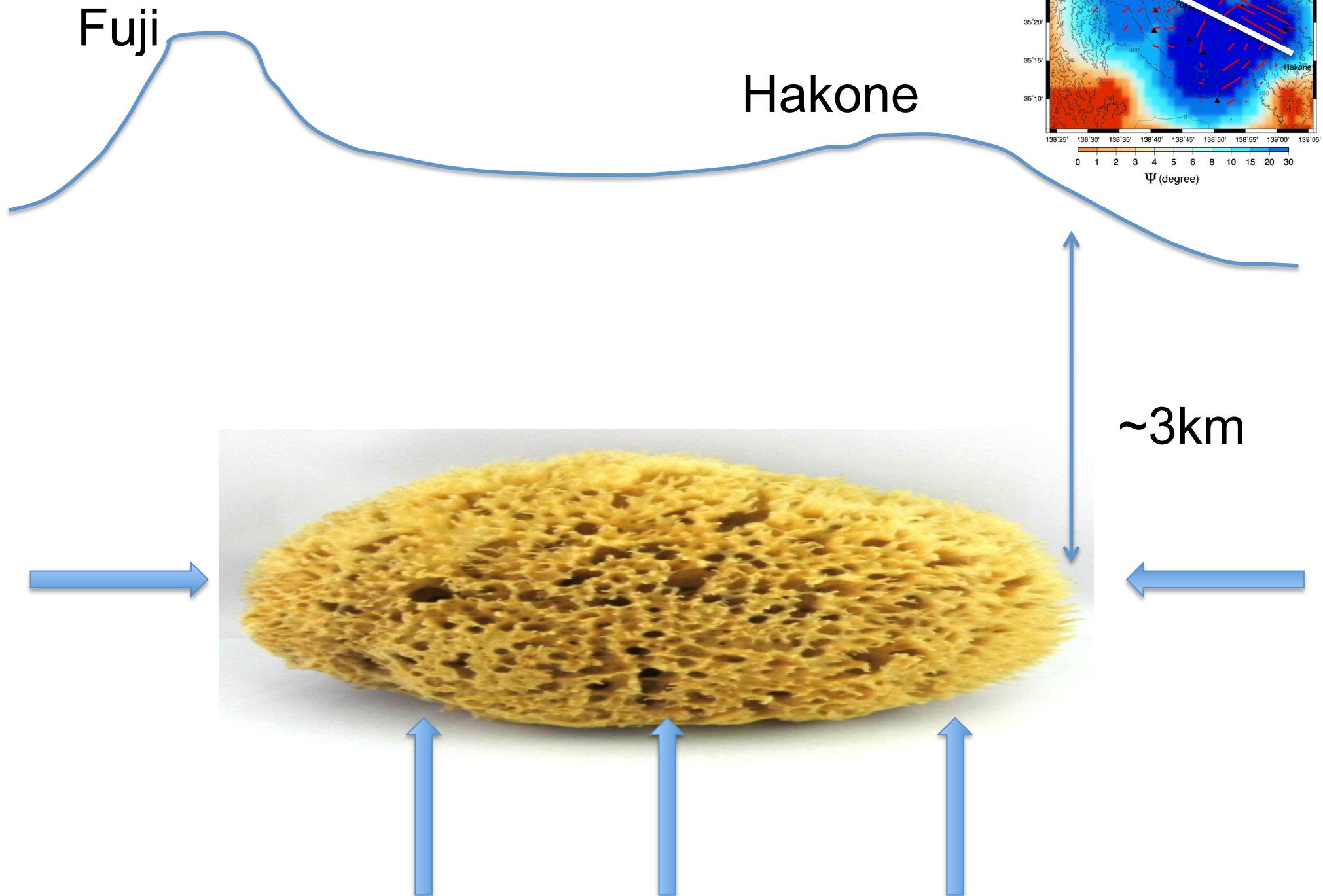
Polarization drop and anisotropy change in April



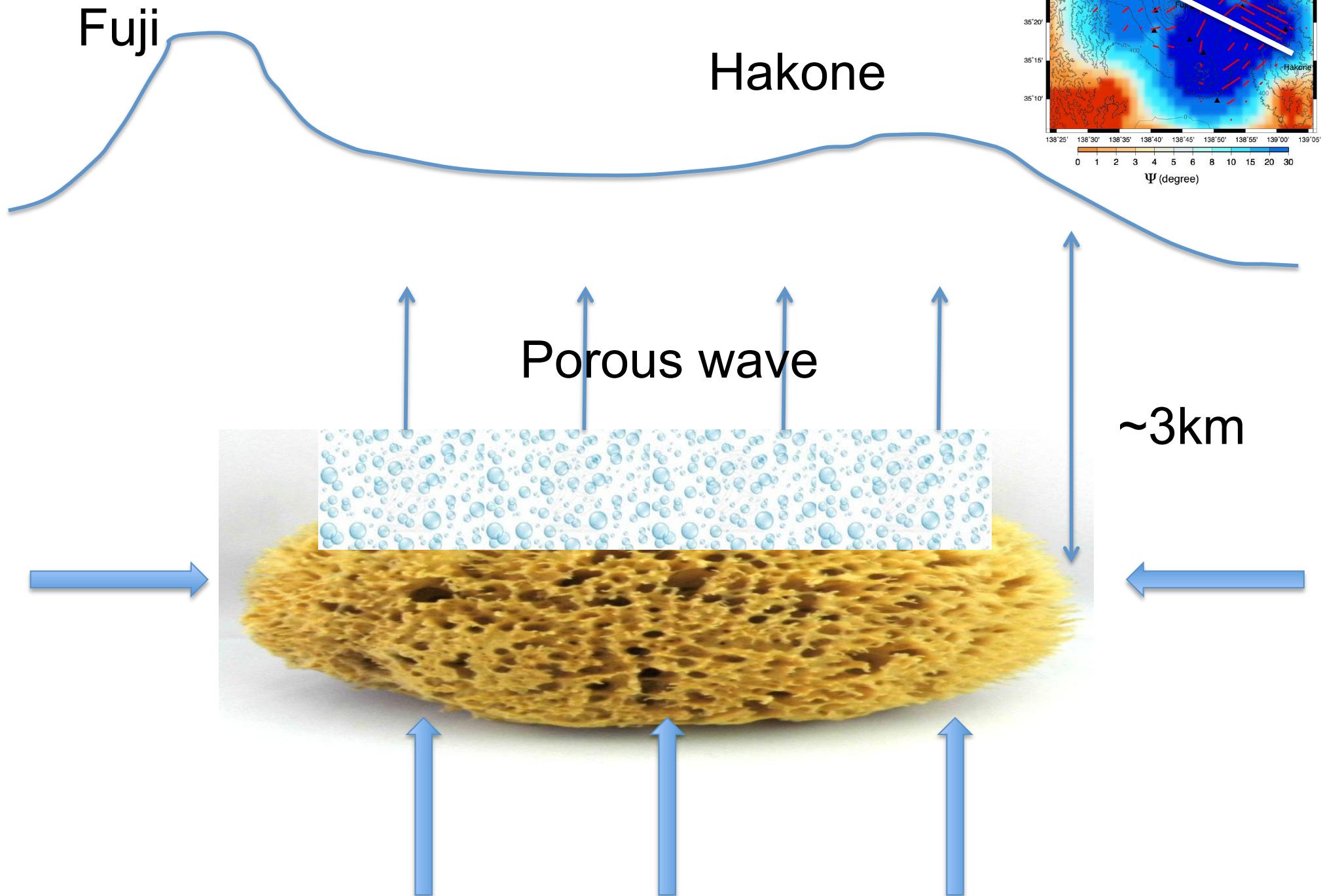
# Plumbing System



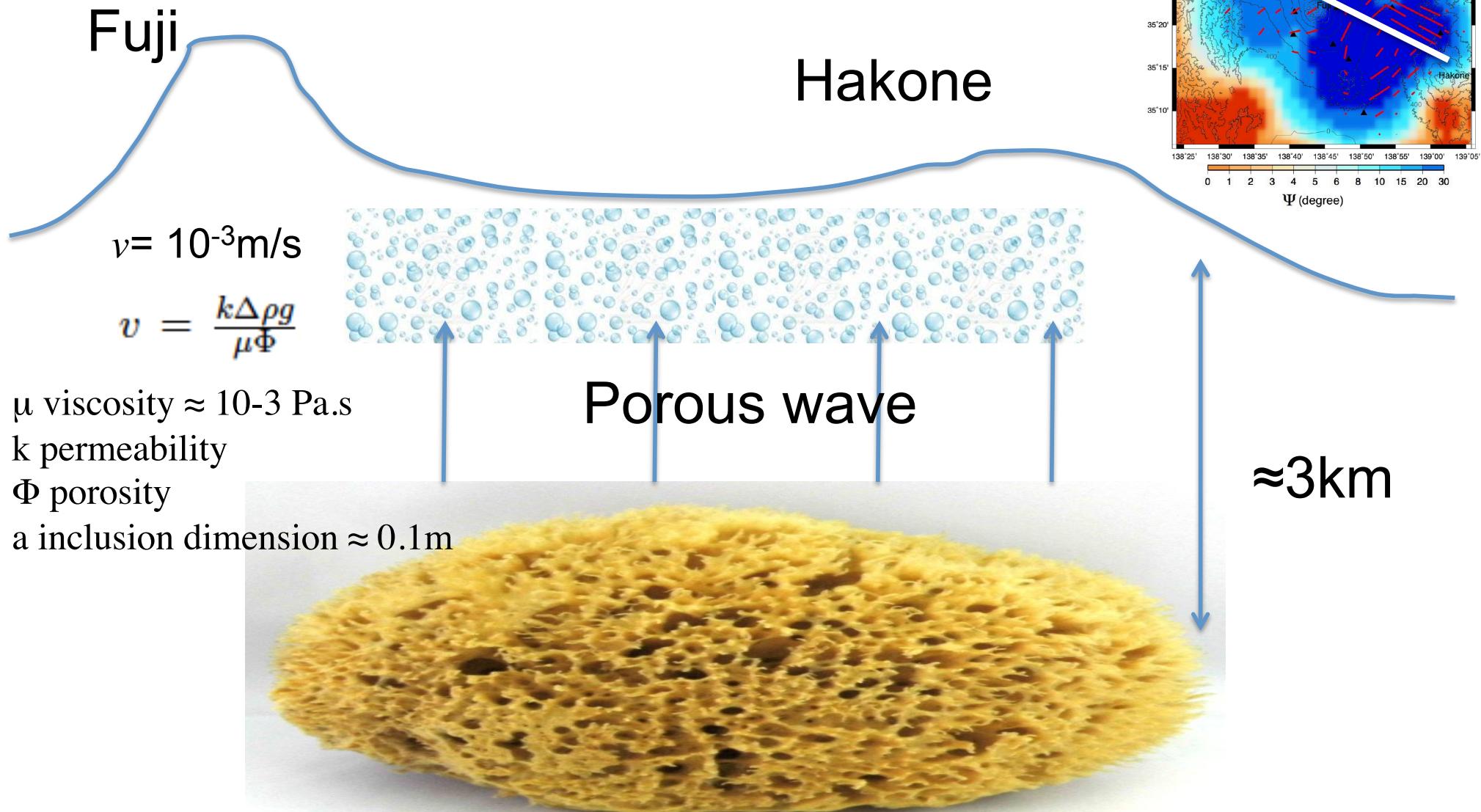
# Tentative interpretation



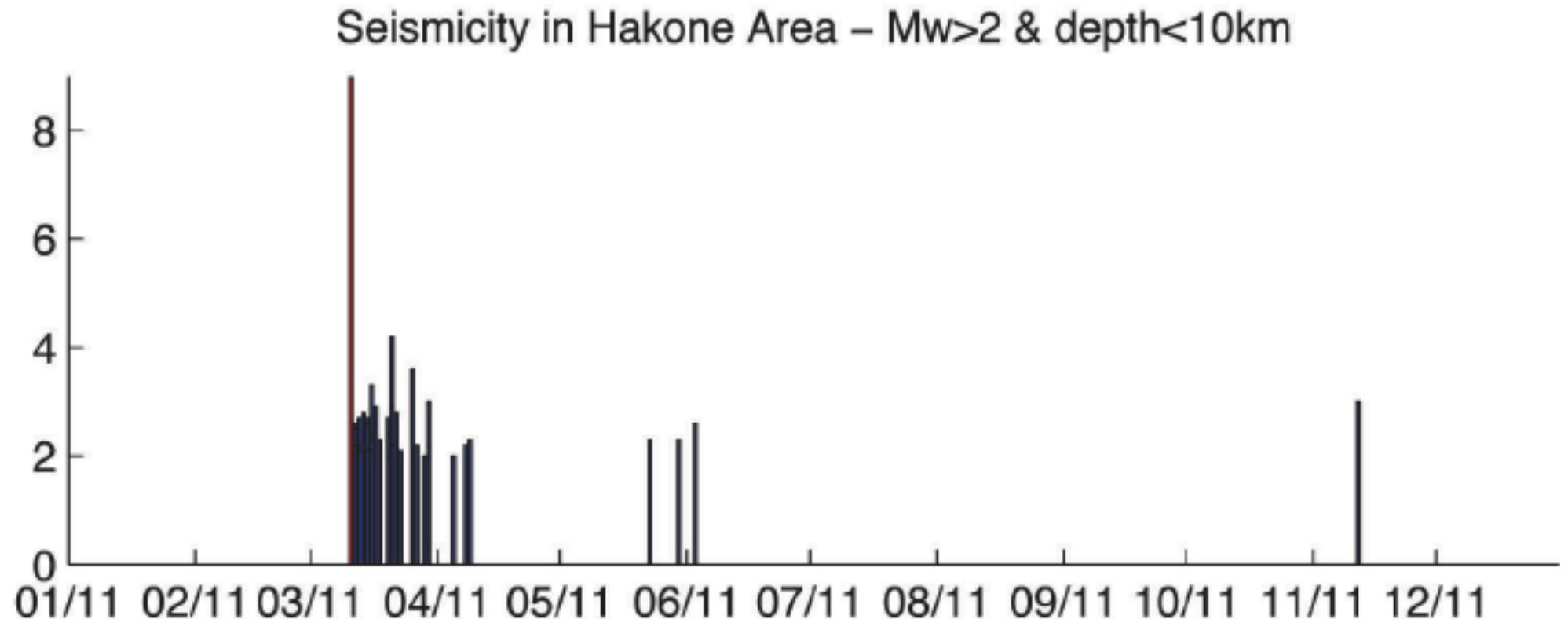
# Tentative interpretation



# Tentative interpretation



# Monitoring of volcanic zones



# Conclusions

Seismic anisotropy is necessary to explain seismic data

It provides new information on many geophysical processes

- New Method for continuous monitoring of the stress field in:

- Seismogenic zones

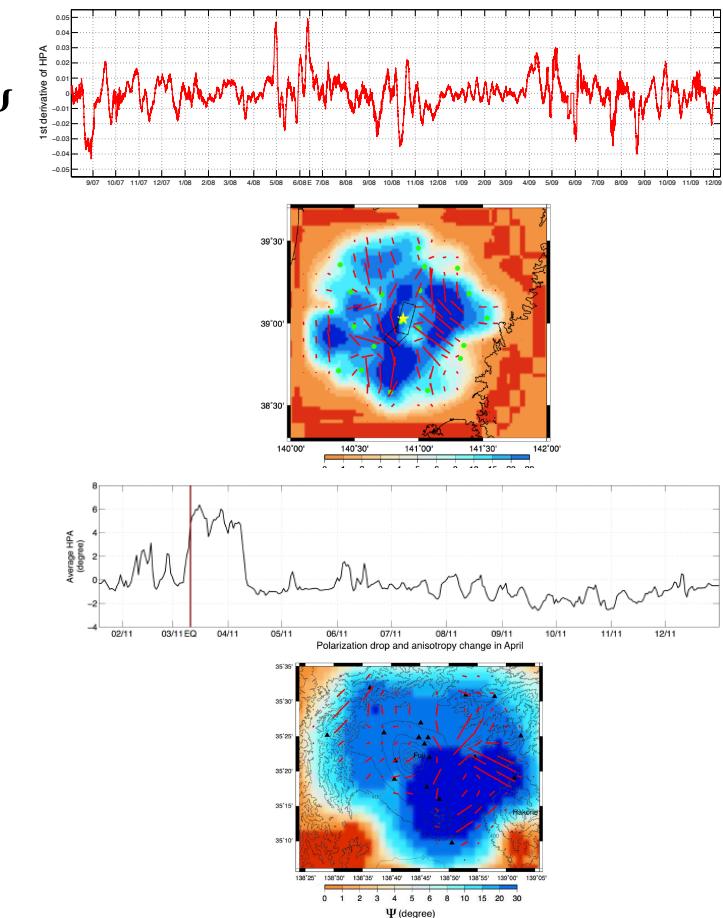
- Significant temporal change of  $\Psi$  observed in parts of the cracked zone

- Volcanic zones: Porous wave

- Interpretation in terms of anisotropy variations and stress changes

- Other applications in oil/gas reservoirs

(Mordret et al., 2013; Tomar et al., 2016)



# THEORY

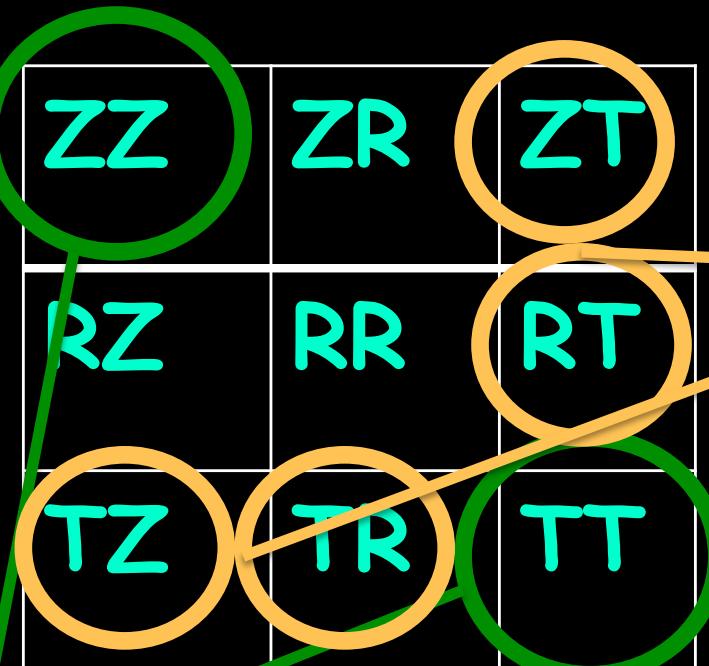
Cross-correlation  
for 2 stations i, j  
and 3 components k, l

$$[C_{ij}(t)]_{kl} = \frac{\int_0^T S_{ik}(\tau) S_{jl}(t + \tau) d\tau}{\sqrt{\int_0^T S_{ik}^2(\tau) d\tau \int_0^T S_{jl}^2(\tau) d\tau}},$$

Azimuthal  
Anisotropy  
of Rayleigh  
waves

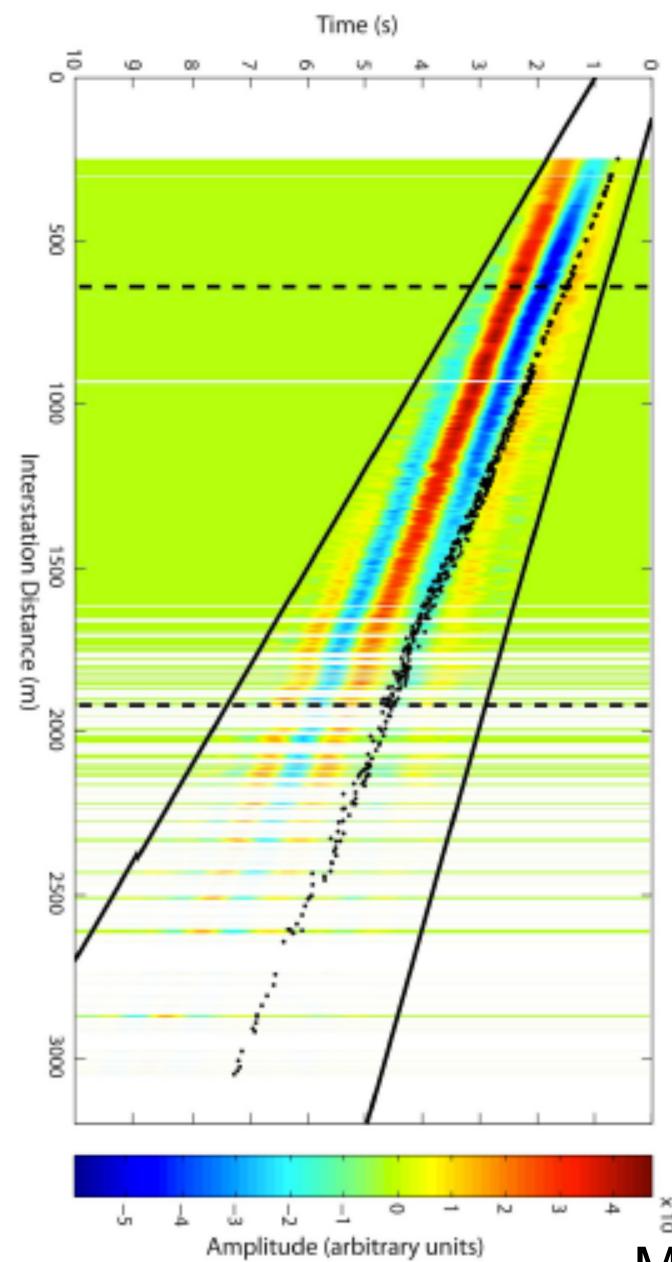
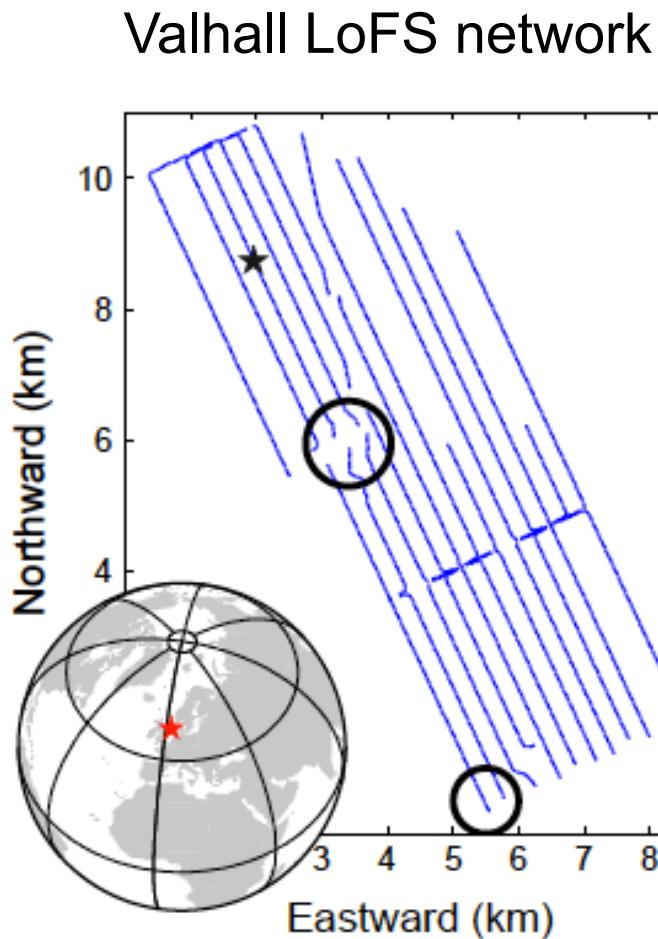
Effect of anisotropy on  $C_{ij}$

Joint Inversion  
of Rayleigh  
and Love waves:  
Radial anisotropy



Quasi-Rayleigh  
Quasi-Love  
waves  
polarization  
anomalies

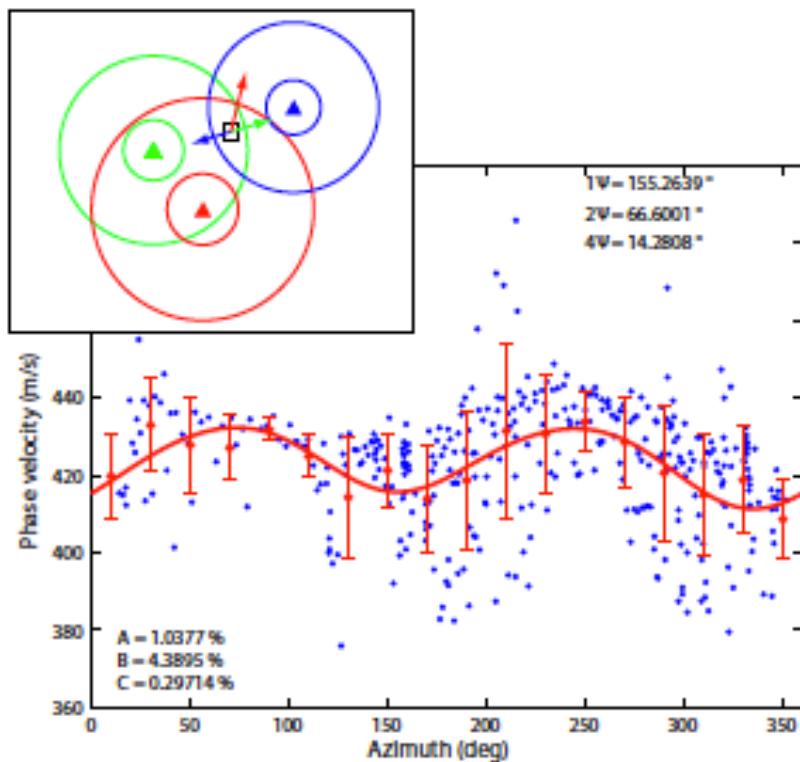
# Rayleigh wave (seismic noise): Azimuthal variation on ZZ-component



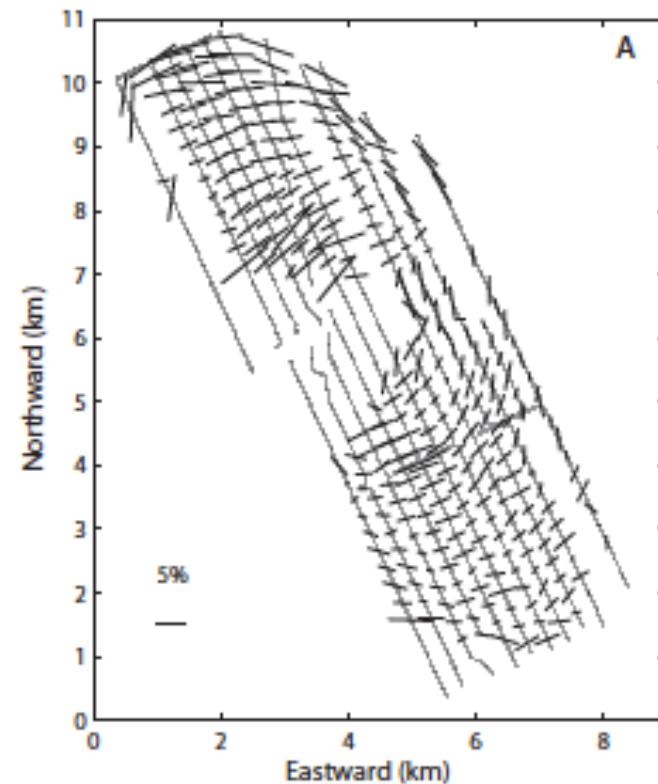
Mordret et al., 2013

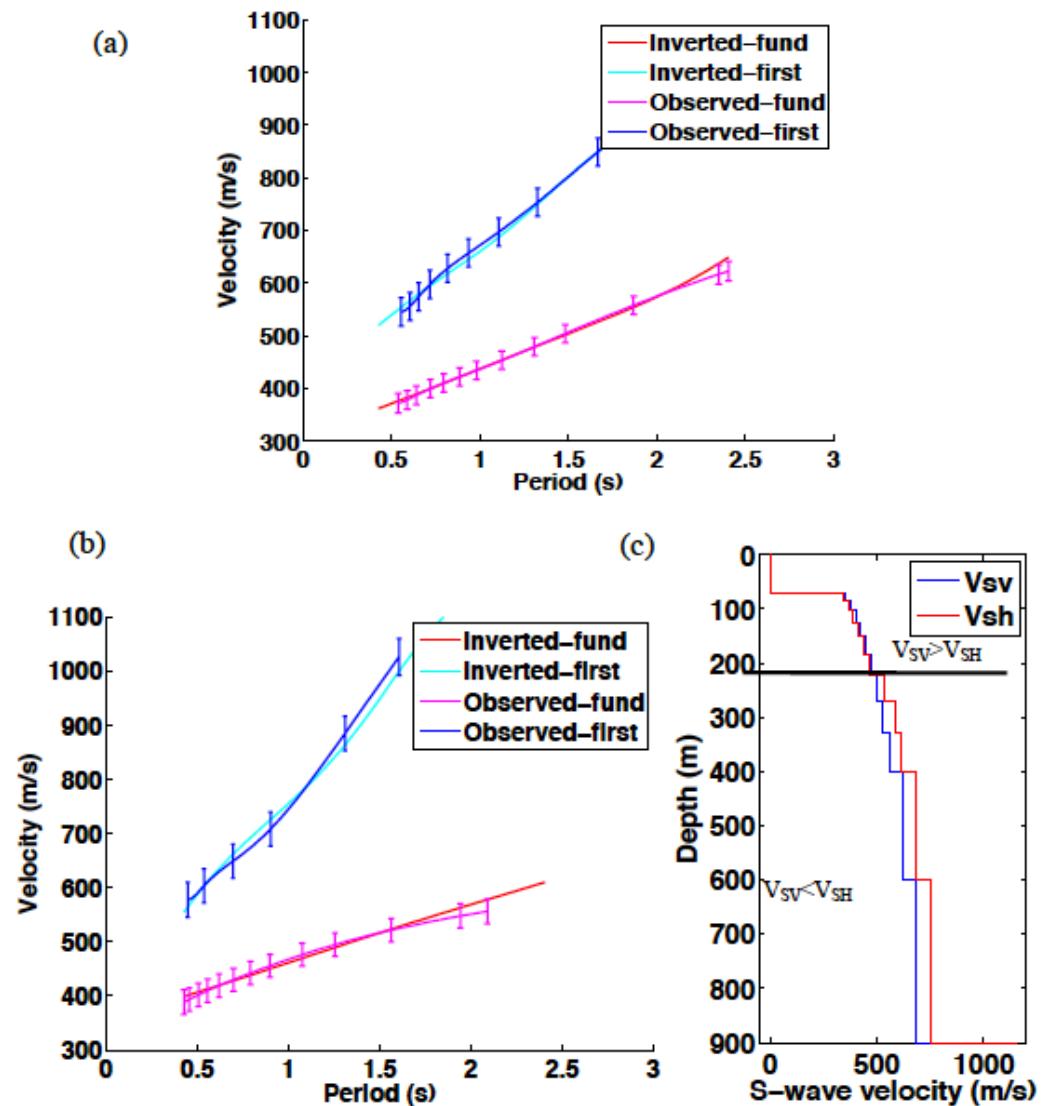
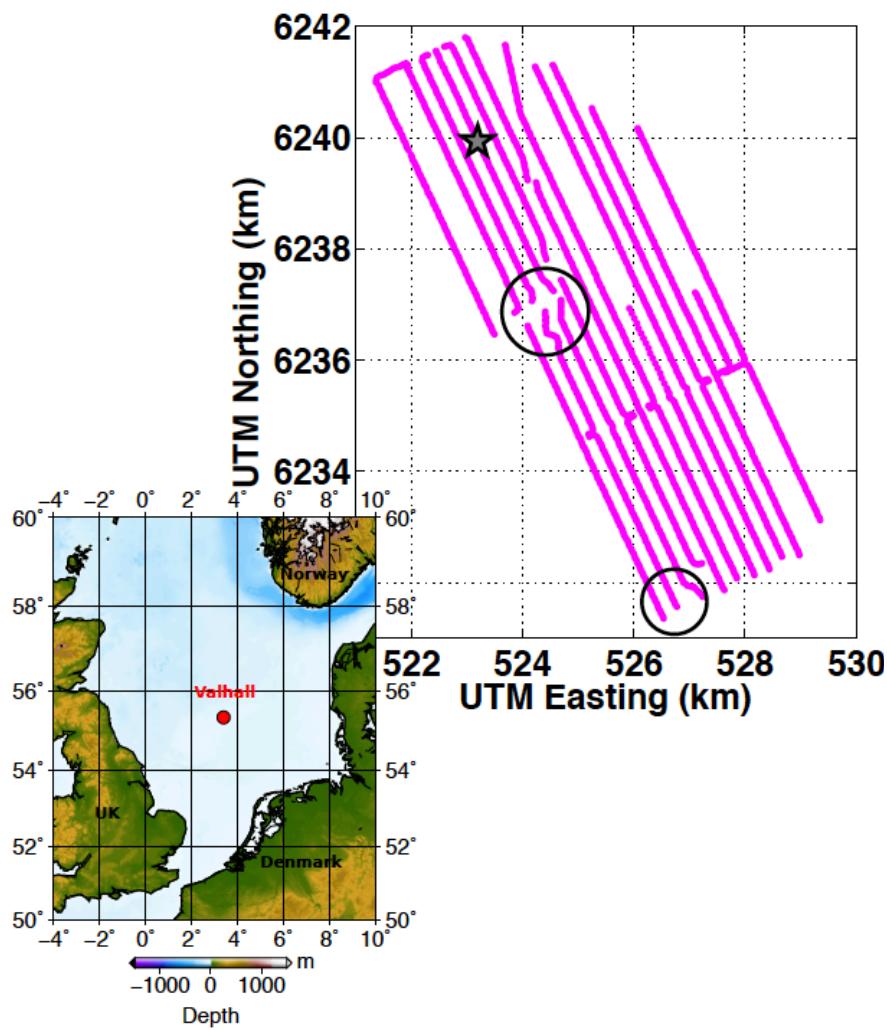
# Rayleigh wave: Azimuthal variation on ZZ-component (1-2-4- $\Psi$ terms)

At T=0.8s



Valhall LoFS: 2- $\Psi$  term





Tomar et al., 2016